

QUANTITATIVE NON-DESTRUCTIVE EVALUATION OF REBAR DIAMETER AND  
CORROSION DAMAGE IN CONCRETE USING  
GROUND PENETRATING RADAR

by

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## Abstract

# QUANTITATIVE NON-DESTRUCTIVE EVALUATION OF REBAR DIAMETER AND CORROSION DAMAGE IN CONCRETE USING GROUND PENETRATING RADAR

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The purpose of this study is to develop new methods for quantitative estimation of rebar diameter and loss of area of rebar due to corrosion using Ground Penetrating Radar (GPR). The existing methods of determining the rebar diameter using GPR are not accurate and the existing methods for evaluating corrosion using GPR are qualitative. The study included in this dissertation uses a 2.6 GHz antenna to estimate the diameter of rebar using two different approaches. The approaches use digital image processing of GPR ragargrams and maximum normalized reflection amplitude from the rebar to estimate the diameter. A novel method to simulate corroded concrete beam specimen in the lab at different level of corrosion using oil water emulsion and accelerated corrosion of rebar in salt water solution.

The results of the diameter estimation using digital image processing shows that the 2.6 GHz antenna can estimate the size of #4 (12 mm) and # 5 (16 mm) rebar with a maximum error of 6.4%. Any diameter that is smaller than #4 (12 mm) and or larger than #5 (16 mm) shows error of at least 18.4%. A relationship between the maximum normalized reflection amplitudes from the GPR signal and the rebar diameter is

established. The relationship was verified using numerical modeling by using the software GPRMAX.

Linear regression equations are developed to find the quantitative loss of area of the rebar at different stages of corrosion from the accelerated corrosion test in the laboratory. The regression equations are developed at three different dielectric constant of the medium and three different depth of concrete cover. A guideline is proposed on how to use the regression equation in the field to estimate the amount of area loss due to corrosion.

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## Chapter 1

### Introduction

#### 1.1 Introduction

Ground Penetrating Radar (GPR) is a non-destructive testing equipment normally used for geophysical investigation. However, use of GPR in concrete structure investigation has progressed substantially. GPR can produce 2D and 3D images of the concrete subsurface and different features, such as rebars, conduits, cracks and voids. Such hidden features in the subsurface can be detected from the GPR data output. As non-destructive testing (NDT) is becoming popular in the field of structural and materials engineering, researchers worldwide are exploring additional usage of GPR. Every year, billions of dollars are being spent on repair and rehabilitation of existing structures, especially highways and bridges. According to ASCE 2013 report card for America's infrastructure, one in nine of the nation's bridges are structurally deficient. Every year 12.8 billion dollars are being spent for the repair and maintenance of the bridges in the U.S.A.. To determine the repair scheme of an existing structure, accurate and robust condition assessment is necessary. The repair cost can be substantially reduced and service life and safety can be increased, if potential damage or failure threat to a structure can be predicted ahead of time .

GPR has been widely used to map concrete deterioration of bridge decks (Parillo and Haggan, 2005). GPR is also used to find location and depth of rebar in concrete. As RADAR wave is very sensitive to moisture, GPR is also used to find location of high moisture content area on a concrete surface. So far, the existing usages of GPR produces mainly qualitative data. Now attention of the GPR practitioners are focused on retrieving more quantitative data from GPR scan to extend its efficiency on NDT of concrete. GPR can easily detect rebar locations embedded in concrete, but more



quantitative information about rebars, such as mass loss of the rebar due to corrosion, cannot be directly measured from direct GPR scan output. GPR can collect data quicker than any other existing NDT methods. If quantitative data, such as amount of corrosion and rebar diameter, can be retrieved from GPR scan, it will be an excellent addition to the usage of GPR in practical applications. When engineers work on addition or renovation projects, the as-built drawings are sometimes not available or reliable. Having additional information on rebars from non-destructive manner would surely be helpful in evaluating the existing strength of the structure.

Concrete structures could be exposed to exterior environment which could be very aggressive due to the presence of high temperature, chloride, carbon dioxide, water, sulphides and other chemicals. These aggressive agents may cause rebar corrosion and ultimately damage the structural integrity. Repair costs of such damages are normally very high. That is why preemptive repair and retrofitting is necessary to prevent the structure from corrosion damage and extend the service life of the structure.

Several rebar locators are commercially available to determine the concrete cover and rebar diameter. These rebar locators are designed according to the magnetic pulse induction method. The application of such techniques are limited to smaller rebar diameters and smaller concrete covers. Moreover, the magnetic pulse rebar locator cannot collect data as quickly as GPR. A few past research studies are concentrated on rebar diameter determination from GPR scan in a number of different ways. Utsi (2004), Leucci (2012) and Zanzi and Arosio (2013) have tried to find rebar diameter in concrete by comparing GPR responses from two orientations of the antenna polarized by 90 degree angle. These methods can predict rebar diameter with an accuracy of 20%. Shihab and Al-Nuaimy (2005) tried to find GPR rebar diameter by mathematical model based on hyperbola fitting to GPR data; this method has limited field application. Chang

(2009) developed an algorithm and tried to find rebar diameter using digital image processing. However, this method is similar to an empirical approach and only limited number of variables were considered. From the existing literature, it is clear that the GPR based method of rebar diameter estimation can be greatly improved by considering a number of variables that can affect calculation. The GPR parameters that affect the diameter of the rebar can be used to study the thinning of the rebar in concrete due to corrosion. In this study, the electrochemical corrosion process will be simulated in the laboratory in an accelerated environment whereas real corrosion takes years to happen. The GPR response from those corroded rebar will be studied to establish a relationship between a GPR parameter and the amount of corrosion.

## 1.2 Problem Statement

Current GPR technology can be used to determine the presence of corrosion. The relation between the corrosion process and GPR response is studied by Lai et al. (2010). GPR parameters, such as two way travel time, maximum rebar amplitude were changed with the progress of corrosion (Lai et al., 2010). GPR had been used to detect the presence of corrosion but the results of such studies were qualitative (Martino et al., 2014). No significant study on the quantitative estimation of corrosion was performed. Moreover majority of the existing study are based on lower frequency antennas, i. e. 1.6 GHz or 2 GHz. It is imperative to determine a quantitative relationship between the GPR parameter and the amount of corrosion using a higher frequency antenna.

### 1.3 Objectives

The main objectives of the study are as follows:

- Determination of GPR parameter that can detect decrease of diameter of rebar due to corrosion induced mass loss.
- Effect of dielectric constant of the concrete on the GPR corrosion parameter
- Effect of concrete cover of the rebar on GPR corrosion parameter
- Perform accelerated corrosion on rebar in salt water tank
- The GPR response of corroded rebar in oil emulsion tank
- Verification of the emulsion tank data by performing corrosion on real reinforced concrete beam
- Proposing a relation between amount of corrosion and corresponding GPR parameter
- Numerical modeling of the experimental data to verify the performance in the experimental phase

### 1.4 Scope of the study

The results presented in this study have some limitations. The only antenna used in the study is GSSI (Geophysical Survey System, Inc.) 2600 MHz antenna. So the effect of antenna frequency on GPR response is not included in this study. The amount of energy dissipated by an antenna depends on the design of the antenna, which is designer specific. So, two antennas of same frequency from different providers can produce differences in output. This study is only valid for the antenna manufactured by GSSI. The corrosion study is done based on a number of assumptions which may not be the actual scenario. GPR wave can illuminate only one side of the rebar during a scan. So, if the corrosion is present on the other side of the rebar, GPR response will not be

able to detect it. However, in most cases, corrosion is supposed to happen on the side with the least amount of cover, typically facing the GPR. The numerical study was performed to verify the behavior of the experimental results. The numerical models were not calibrated exactly with the experimental model. In this study, the different factors that can be influential in calculating rebar diameter through GPR scan will be studied. The factors that affect the change of size of the rebar will be used to detect the amount of corrosion damage of the rebar.

### 1.5 Organization of the Study

The organization of the remainder of this dissertation is as follows. Theory of GPR and electromagnetic theory is discussed in brief in Chapter 2. The literature review on the usage of GPR on diameter estimation and detection are discussed in Chapter 3. The review of existing work on the application of GPR on detecting and assessing corrosion damage is also discussed in Chapter 3. In Chapter 4, the parameters that affect the diameter estimation of rebar in concrete are presented. In Chapter 5, oil emulsion tanks are presented as a substitute of concrete beams. The emulsion tanks are used to investigate the effect of dielectric property on GPR response. The GPR response from corroded rebar obtained from accelerated corrosion tests are also presented. The changes of GPR response with the progress of corrosion in a real concrete beam are studied as well. Chapter 6 discusses the numerical modeling of a rebar in concrete using Finite Difference Time Domain FDTD method. The electromagnetic simulation of the rebar embedded in concrete is presented in this chapter. The response of the numerical value are used to support the experimental values obtained in Chapter 5. Finally, conclusions and recommendations are presented in Chapter 7.

## Chapter 2

### Theory of GPR and Electromagnetic Theory

#### 2.1 Introduction of GPR

There are several methods to create an image of the subsurface in order to detect and locate buried objects. The methods that are already being used as subsurface detection techniques are seismic, electric resistivity, nucleonic, gravity surveying, thermographic and electromagnetic methods. Among all these methods, GPR is most popular among the engineers and practicing scientists because of its range of specializations. The term GPR refers to a range of electromagnetic techniques which is designed primary for locating objects of interface. The design philosophy primarily depends on type of the target and the material properties. The range of application of GPR is very diverse and the quality of this technique is increasing with the development of more sophisticated signal recovery techniques, system design and operating practices.

GPR can detect dielectric discontinuity and the target can be classified according to the geometry of the target such as planer surface, cylindrical object, cuboidal objects etc. GPR system can be preferentially designed to detect a particular type of target. The signal attenuation and the frequency of the antenna are the two major factors in GPR system design for a particular application. The material that possesses a high magnitude of low frequency conductivity will have higher degree of signal attenuation. The attenuation can be decreased by using a lower frequency but compromising with the resolution. According to Daniels (2004), successful operation of GPR depends on the following factors:

- (a) efficient coupling of GPR waves to the ground
- (b) adequate penetration of the GPR wave to the target with least attenuation
- (c) a significant amount of backscattered signal from the target

(d) an adequate bandwidth of the detected signal for good resolution and low noise levels.

GPR technique is usually used to detect backscattered radiation from the target although forward scattering is also possible in some application but at least one antenna needs to be buried into the ground. The depth and resolution needs to be clearly defined according to the application because this controls the frequency and the bandwidth of the antenna.

## 2.2 System Design

The design of GPR depends on a number of factors that influence the ability to detect and the resolution. For successful operation of GPR, an adequate signal to clutter ratio, signal to noise ratio, adequate spatial resolution and adequate depth resolution must be confirmed. The main factors in system design are range, velocity of propagation, clutter, depth resolution and plan resolution.

### 2.2.1 Range

The range of GPR depends on three factors. They are material loss, spreading loss and reflection loss. The signal that is detected by the receiver antenna goes through several types of losses. For a particular distance from the antenna to the target, the total path loss ( $L_T$ ) is shown in the following Eq. (2.1) (Daniels, 2004).

$$L_T = L_e + L_m + L_{t1} + L_{t2} + L_a + L_s + L_{sc} \quad (2.1)$$

Where,

$L_T$  = antenna efficiency loss

$L_m$  = antenna mismatch loss

$L_{t1}$  = transmission loss from air to material

$L_{t2}$  = retransmission loss from material to air

$L_s$  = antenna spreading loss

$L_a$  = attenuation loss from material

$L_{sc}$  = target scattering loss

### 2.2.2 Velocity of propagation

If the velocity of the propagation of the electromagnetic wave is known, it is possible to measure the depth or thickness of the target. If the material is homogenous and isotropic, the relative propagation velocity  $v_r$  can be found from Eq. (2.2)

$$v_r = \frac{c}{\sqrt{\epsilon_r}} \quad (2.2)$$

The depth or thickness  $d$  can be found from the following Eq. (2.3)

$$d = v_r \frac{t}{2} \quad (2.3)$$

where,  $\epsilon_r$  is the relative permittivity and  $t$  is the two way travel time. The velocity can be measured from a hyperbolic signature or from common depth point method.

Propagation velocity increases with increasing relative dielectric permittivity. The velocity slows down in a material and the wavelength also decreases.

### 2.2.3 Clutter

Clutter is unwanted signals in the GPR scan that have similar scattering characteristics to the real target. Clutter can be caused by breakthrough between the transmitter and the receiver antenna. The multiple reflections between the ground surface and the antenna also create clutter. The amount of clutter varies on the type of antenna configurations.

### 2.2.4 Depth resolution

Depth resolution is important where a number of different types of targets are targeted with the GPR within a given depth. A signal with a wider bandwidth is required to distinguish between the different types of targets. The bandwidth of the received signal is

more important than that of the transmitting signal. The receiver bandwidth can be determined by the power spectrum of the received signal.

### 2.2.5 Plan resolution

Plan resolution of radar is important when there are multiple targets at the same depth. A high gain antenna is needed to get an improved plan resolution. It requires a significant aperture of the antenna at a low transmitting frequency, small antenna dimension and high frequency. Plan resolution improves with attenuation.

### 2.3 Material properties and electromagnetic waves

The electromagnetic wave propagation can be expressed by the following one dimensional Eq. (2.4) where the electrical and magnetic fields work along X and Y axis and the propagation is taken along Z axis.

$$\frac{\partial^2 E}{\partial z^2} = \mu\epsilon \frac{\partial^2 E}{\partial t^2} \quad (2.4)$$

Where, E is electric field,  $\epsilon$  is absolute material permittivity and  $\mu$  is absolute material magnetic permittivity. Both the electrical and magnetic part of the electromagnetic wave goes through losses when it travels through a material which causes attenuation to the original wave. For most engineering material, the magnetic permeability is not a significant factor because the magnetic response is very weak. But the conductivity and the permittivity are very important because these properties are responsible for the losses of the electric field of the wave. It is difficult to differentiate the loss form material conductivity and loss from material dielectric permittivity. The conductivity and the permittivity are both frequency dependent complex numbers. The permittivity  $\epsilon$  and the conductivity  $\sigma$  can be expressed as Eq. (2.5) and Eq. (2.6).

$$\epsilon = \epsilon' - j\epsilon'' \quad (2.5)$$

$$\sigma = \sigma' - j\sigma'' \quad (2.6)$$



Where  $\epsilon'$  and  $\sigma'$  are real parts, and  $\epsilon''$  and  $\sigma''$  are imaginary parts. The first part of Eq. (2.5)  $\epsilon'$  refers to the dielectric constant and the second part  $\epsilon''$  refers to losses due to conductivity and changing frequency.

#### 2.4 GPR antenna

The size of a radar antenna is normally dependent on the wavelength of the wave frequency. The larger is the wavelength, the larger is the size of the antenna. In GPR application, for the sake of portability purpose, the size of the antenna cannot be electrically too big. Because of this limitation on the size, the gain is normally very low in GPR antennas compared to conventional radar antennas. However the bandwidth of GPR antenna is normally much higher than conventional radar antenna. Because of the high bandwidth, the resolution is also much better for GPR antennas. For impulse based radar, the types of antennas are resistively loaded dipole, bow-tie and TEM travelling wave antenna.

## Chapter 3

### Literature Review

#### 3.1 GPR Theory

GPR is a non-destructive electromagnetic technique that is used to investigate the features buried under ground. The operating principal of GPR is similar to conventional radar but it is used in opaque medium such as ground, concrete etc. The propagation of GPR wave into a medium is governed by Maxwell's equations. GPR system normally works using a control unit and a transmitting and receiving antenna. The transmitter sends signal into the ground. The transmitting signal gets reflected from the target and the reflected signal is received by the receiver antenna. The received data is then processed and displayed. A typical GPR system is shown in Fig. 3.1. GPR wave gets reflected if there is a new material in the path of propagation of the wave. The reflection wave is the function of the permittivity ( $\epsilon$ ), the magnetic permeability ( $\mu$ ) and the electrical conductivity ( $\sigma$ ) of the reflection surface (Bostanudin, 2013). A medium with high conductivity reduces the penetration of the GPR wave because it absorbs the radar signal. The magnetic permeability is very low for most of the engineering materials. GPR signal is most susceptible to the permittivity of the medium.

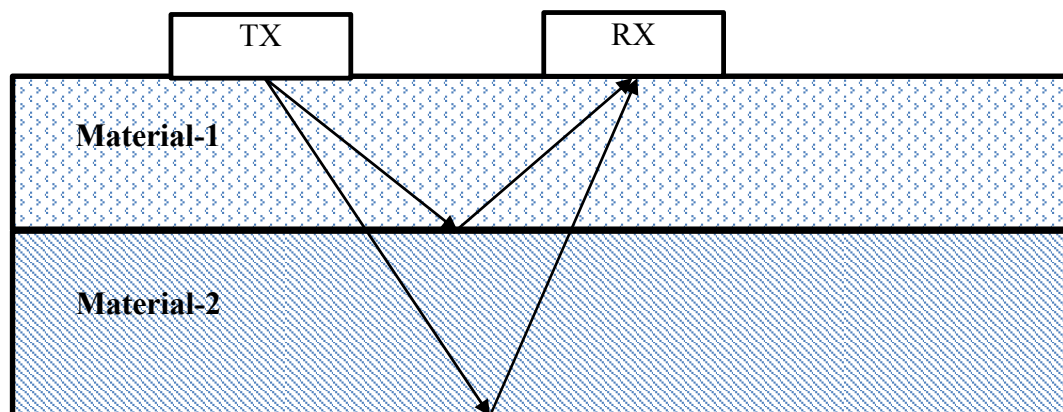


Figure 3-1 Schematic diagram of generic GPR system

When GPR wave encounters a change in the manganite of permittivity in its path of propagation, the following things happen. First, some part of the signal gets absorbed at the surface. Second, some part of the signal travels through the new surface. Third, the remaining part of the signal reflected from the surface. This reflected signal is recorded by the receiver antenna of the GPR system. The amplitude and wavelength and the travel time of the signal is recorded by GPR. This recorded information consists of valuable information about the reflection surface or target.

### 3.1.1 GPR Data Collection

The data collection of GPR on soil or concrete can be done in two different methods depending on antenna position. If the antenna is in contact with the ground or concrete surface, then it is called a ground coupled antenna. If the antenna is positioned at a distance away from the ground, then it is called air-launched antenna. Figure 3.2 shows ground coupled and air-launched antenna.



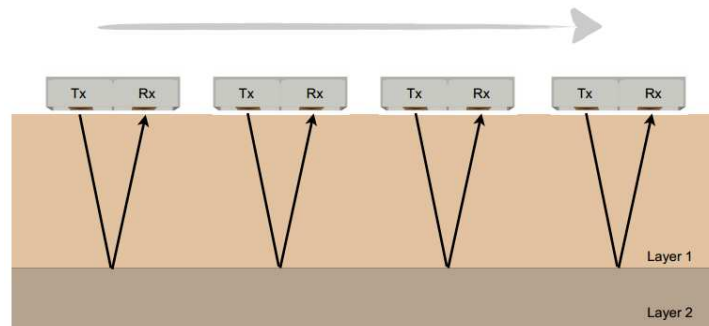
(a) Ground coupled



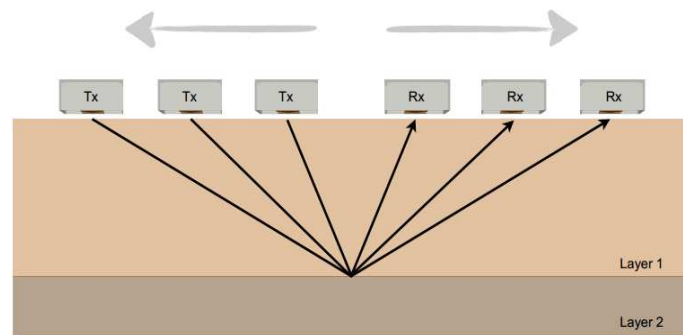
(b) Air-launched

Figure 3-2 Ground coupled and air-launched antenna (GSSI Concrete Handbook, 2015)

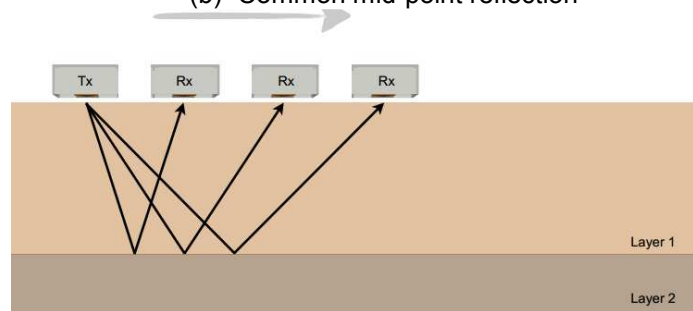
Based on the position of the transmitter and the receiver of the GPR system, there are three different ways of collecting data. They are common offset reflection, common mid-point reflection and wide angle reflection refraction as shown in Fig. 3.3.



(a) Common offset reflection



(b) Common mid-point reflection



(c) Wide-angle reflection-refraction

Figure 3-3 GPR Surveying methods (Warren, 2009)

In common offset method, the antenna travels over the surface to perform a scan and the distance between the transmitter and receiver is constant. The transmitter and the receiver both moves together during a scan. In common midpoint method, a particular point in the subsurface is targeted. The transmitter and the receiver move away from each other at a constant rate. In wide-angle reflection-refraction method, the transmitter is stationary but the position of the receiver is varied and data is collected from each of the positions of the receiver. In this study, the common offset method was used to collect the data.

Data collection can be classified based on the orientation of the antenna as well. Normally in an antenna, the transmitter is positioned at the front and the receiver is positioned at the back. When the transmitter and the receiver are along the line of the scan, then it is called normal orientation of the antenna. When the transmitter and receiver are perpendicular to the direction of scan, then it is called cross-polarized orientation of the antenna. Figure 3.4 shows the normal and cross polarized antenna.

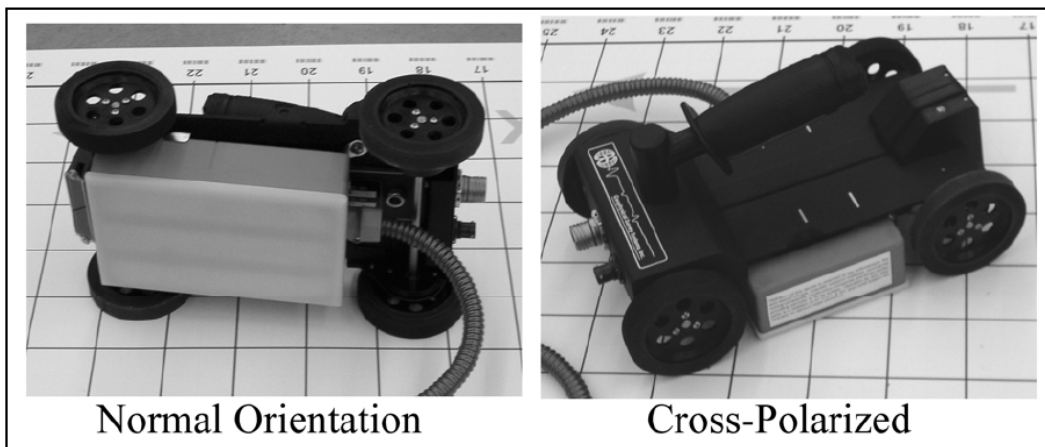


Figure 3-4 Antenna polarization (GSSI Concrete Handbook, 2015)

### 3.1.2 Property of the medium

The propagation of the electromagnetic wave through a medium depends on the electromagnetic constitutive properties of the medium. The constitutive properties are electrical conductivity, magnetic permeability and electrical permittivity. A medium that has high electrical conductivity such as clay attenuates the GPR signal. Presence of water also increases the conductivity and creates absorption of energy from the signal.

The most important material property that controls the speed of radar wave is the permittivity of the medium. The ratio of the permittivity of a material to the permittivity of free space is called the dielectric constant of the material. The higher the dielectric constant of a material, the slower the speed of radar wave through it. If the dielectric constant of a material is known, the depth of the target can be measured. Radar wave travels faster in materials having low dielectric constant. Therefore, to produce a better GPR scan, a low dielectric medium is expected. Table 3.1 show the dielectric constant of some common materials.

Table 3-1 Dielectric constant of common materials (Warren, 2009)

Materials	$\epsilon_r$
Air	1
Clay (dry)	2-20
clay (wet)	15-40
Concrete (dry)	4-10
Concrete (wet)	10-20
Fresh Water	81
Fresh water ice	3-4
Granite (dry)	5-8
Granite (wet)	5-15
Limestone (dry)	4-8
Limestone (wet)	6-15
Sand (dry)	4-6
Sand (wet)	10-30
Soil (average)	16
Iron Oxides	14

### 3.1.3 GPR Scan output

The output signal of GPR scan possesses valuable information about the subsurface. The output of the GPR scan is not the real image of the subsurface. Rather it is a type of signature depends on the size, shape and dielectric constant of the target. The first reflection of the GPR wave is called direct wave or direct coupling. This direct wave indicates the top surface. Figure 3.5 shows a GPR reflection signal with direct coupling at the top of it.

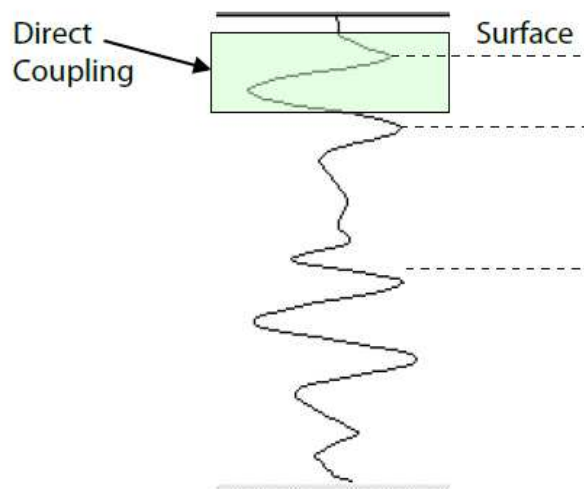


Figure 3-5 Direct coupling or direct wave form the surface  
(GSSI Concrete Handbook, 2015)

GPR scan data can be collected and presented in one, two and three dimensions as discussed below.

#### (1) A-Scan

An A-Scan is a one dimensional scan where the travel time of the GPR wave is in the x-axis and the amplitude of the reflection is in the y-axis. The transmitter and the receiver are both kept to an stationary position. A-Scan is also called line-scan or oscilloscope scan. Figure 3.6 shows an A-Scan.

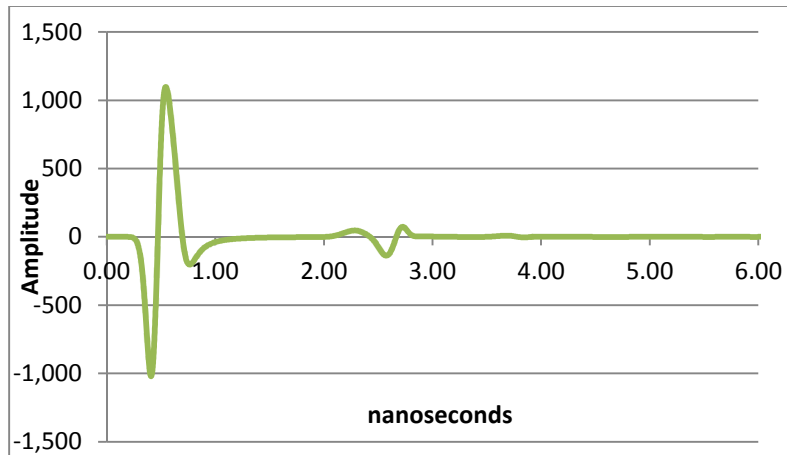


Figure 3-6 GPR A-Scan

(2) B-scan

GPR B-scan is a two dimensional image of the subsurface. When the antenna is moved on the surface, series of A-Scans are recorded by GPR. By combining all the A-Scans side by side, the B-scan is produced. Most GPR scanning is done to produce a B-scan. B-Scans are sometimes called radargram. Figure 3.7 shows a B-scan with a A-Scan on the right. The x-axis can be distance or number of A-Scans and the y-axis is time.

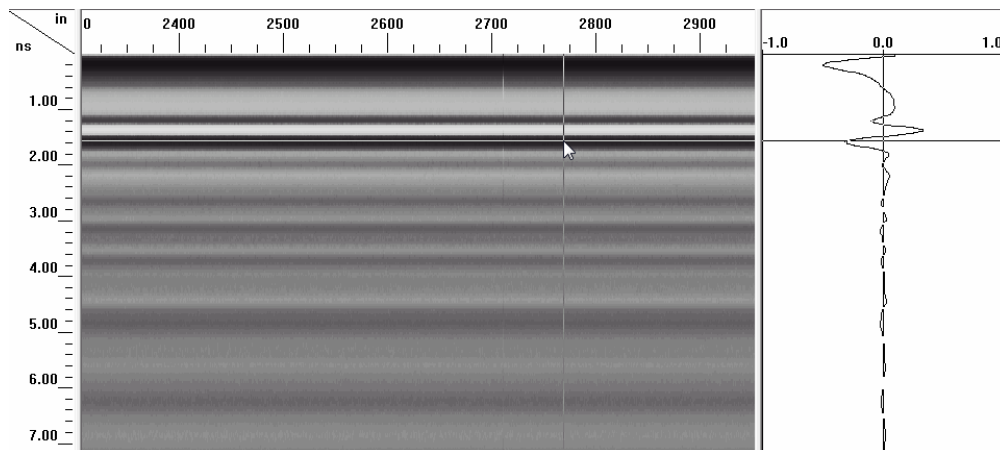


Figure 3-7 GPR B-Scan or radargram



### (3) C-Scan

C-Scan is three dimensional scan. The B-Scans or the radargrams can be collected in a grid and all the B-Scans can be combined together to produce a 3-D map of the subsurface . Figure 3.8 shows a C-Scan of concrete slab. The grid of reinforcement is visible.

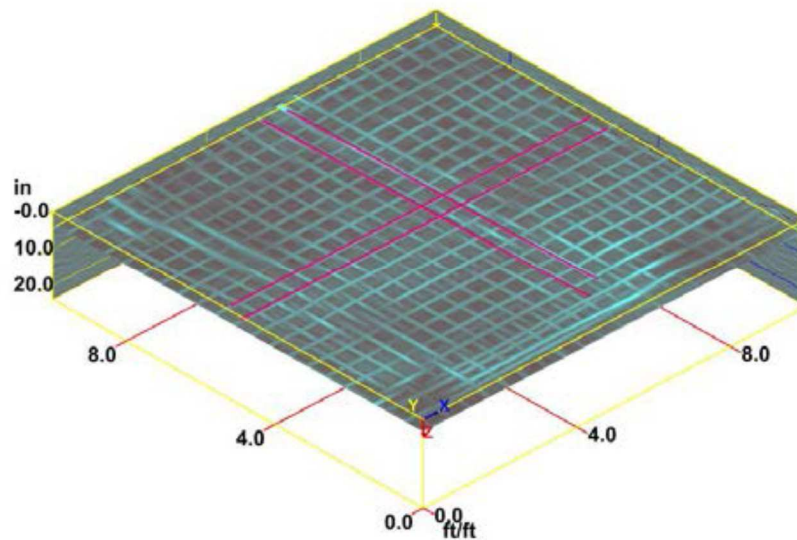


Figure 3-8 GPR C-Scan or 3-D view (GSSI Concrete Handbook, 2015)

#### 3.1.4 Horizontal and Depth Resolution

The number of scans per unit length of the survey direction control the horizontal resolution of the B-Scan or radargram. The vertical penetration depth depends on the frequency of the antenna. The lower is the frequency, the higher the penetration depth. Similarly, the higher is the frequency, the lower the penetration depth. But at the same time, the higher is the frequency, the higher the vertical resolution of the B-Scan. So, selecting an appropriate antenna is very important depending on the type of investigation.

### 3.2 Non-Destructive methods for measuring rebar diameter in concrete

Different types of cover meters are available in the market to determine the concrete cover and the diameter of the rebar. These instruments normally use either the magnetic reluctance method or the eddy current method. The schematic diagram of these methods is shown in Fig. 3.9. In magnetic reluctance meters, AC current produces a magnetic field from one of the two probes. The second probe measures the magnetic flux. The flux is high when the meter is placed over a rebar. This high flux ensures the presence of rebar. In eddy current meters, the coil in the meter produces varying magnetic fields from varying AC currents similar to reluctance method. These cover meters can also estimate the bar size within an accuracy of +/- one bar size. The presence of excessive steel produces excessive magnetic field and gives error in results.

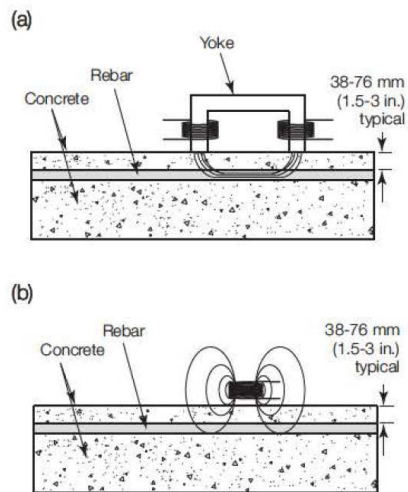


Figure 3-9 Reluctance based and eddy current based cover meters  
(Washer, G. A. 2013)

Another method of finding rebar and its diameter is radiography (Washer, G. A. 2013). Figure 3.10 shows a radiograph of spiral reinforcement in a concrete column. Radiography of concrete can be done using X-rays or gamma rays. Gamma rays can produce 10 in. to 20 in. penetration into concrete based on the source of the isotopes

used to produce gamma rays, which is normally cobalt or iridium. High energy X-rays are used for deeper penetration into concrete, as large as 50 in. The disadvantage of radiography is that both surfaces of the concrete have to be accessible to perform the test. Radiographic plate is also needed to place at the opposite side of the source. Radiography is expensive and has potential for health hazard.

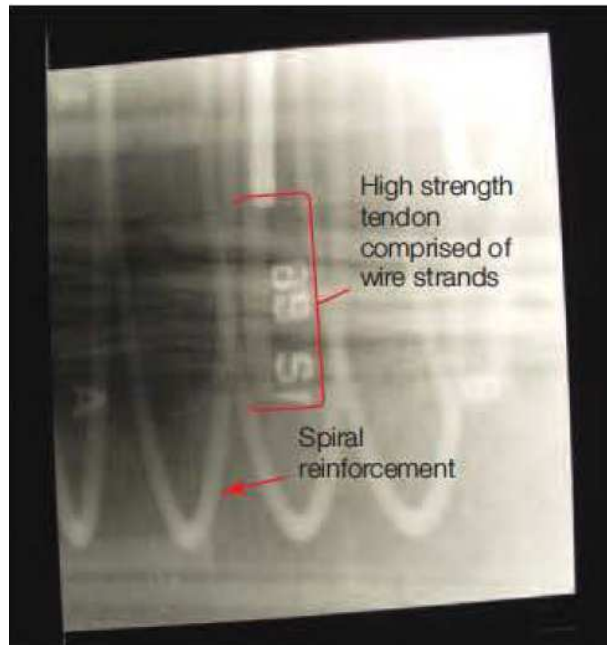


Figure 3-10 Radiograph of spiral steel in concrete encircling high strength tendons

### 3.2 Use of GPR is measuring diameter of rebar

The hyperbola that results from the GPR trace of a rebar embedded in concrete can be represented by mathematical model. Shihab and Al-Nuaimy (2005) demonstrated this by drawing asymptotes on a fitted hyperbola from a rebar, as shown in Fig. 3.11. The hyperbola is shown in Eq. (3.1):

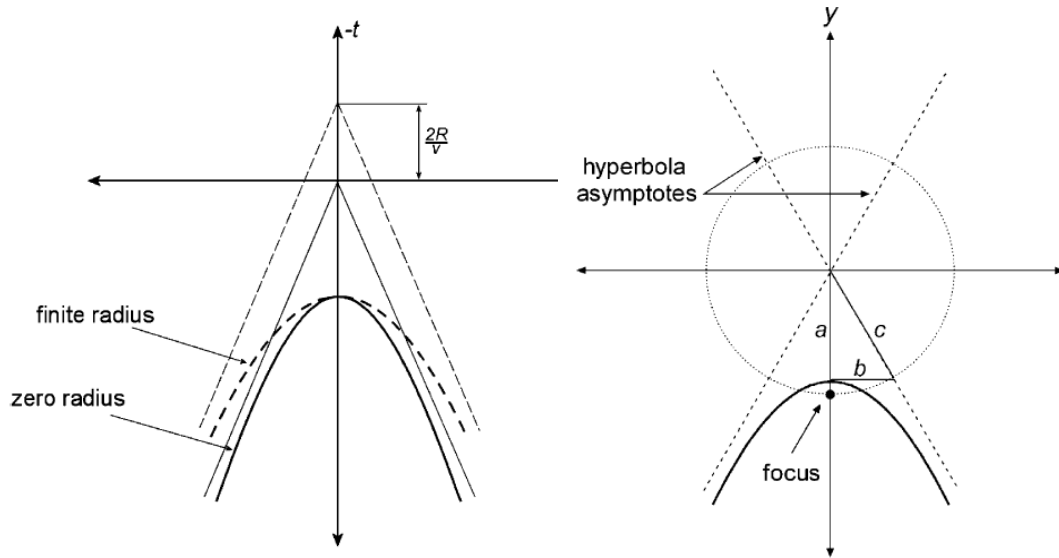
$$\left(\frac{t + \frac{2R}{v}}{t_0 + \frac{2R}{v}}\right)^2 - \left(\frac{x - x_0}{\frac{v}{2}t_0 + R}\right)^2 = 1 \quad (3.1)$$

where,

R = radius of the object,

v = velocity of radar wave and

t = two way travel time.



(a) Effect of changing radius

(b) General hyperbola parameters

Figure 3-11 GPR hyperbola traces (Shihab and Al-Nuaimy, 2005)

The radius can be estimated by the following equations (Eq. 3.2 to Eq. 3.5):

$$a = t_o + \frac{2R}{v} \quad (3.2)$$

$$b = \frac{v}{2} \left( t_o + \frac{2R}{v} \right) \quad (3.3)$$

$$v = \frac{2b}{a} \quad (3.4)$$

$$R = \frac{b(a - t_o)}{a} \quad (3.5)$$

where,

a = distance from the tip of hyperbola to surface,

b = distance from the tip of the hyperbola to the asymptotes as in Figure 3.11,

t = two way travel time of radar wave,

v = velocity of radar wave and

R = radius of the object

Utsi and Utsi (2004) used 2 GHz and 4 GHz GPR antenna and found the correlation between the rebar diameter and the maximum amplitude from rebar with two different antenna orientation. It was shown that the maximum amplitude increased with the increase of rebar diameter as shown in Fig. 3.12.

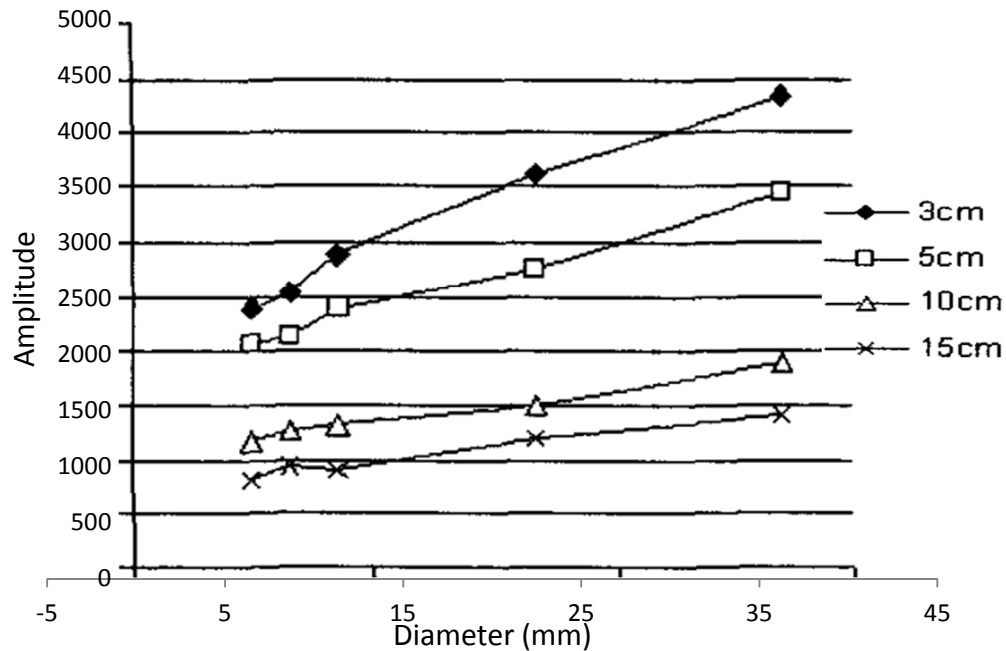


Figure 3-12 Relationship between rebar diameter and maximum normal amplitude at different depths (Utsi and Utsi, 2004)

Chang et al. (2009) proposed a physical model of rebar scanning embedded in concrete with a GPR antenna, as shown in Fig. 3.13. The model considered the radius of the rebar. The power reflectivity from the rebar was plotted against the distance traveled by the GPR antenna. The initiation and the end of power reflectivity along the scan direction were determined from the radargram. The distance between the beginning and end point of power reflectivity was measured by converting the B-Scan of the image to an alpha-numeric code using MATLAB. Once the parameters shown in Fig. 3.13 were determined; the diameter was calculated using Eqs. 2.6 and 2.7. An accuracy of 7% in

calculating rebar diameter using this method was claimed. The validity of this method at different concrete covers was checked. The accuracy decreased with the increase of concrete cover. This was due to the fact that the hyperbolic signature of GPR radargram was less pronounced and the initiation and end point of the rebar power reflectivity could not be measured accurately.

$$S_{cor} = L - E \quad (3.6)$$

$$r = \frac{S_{cor}}{2\pi} = \frac{L - E}{2\pi} \quad (3.7)$$

In Eq. 3.6 and 3.7,

$S_{cor}$  = distance between the energy footprint of the antenna when the footprints are tangential to the rebar as shown in Figure 3.13.

$E$  = energy footprint of the antenna

$L$  = distance between initial and final signal of power reflectivity as shown in

Figure 3.5.

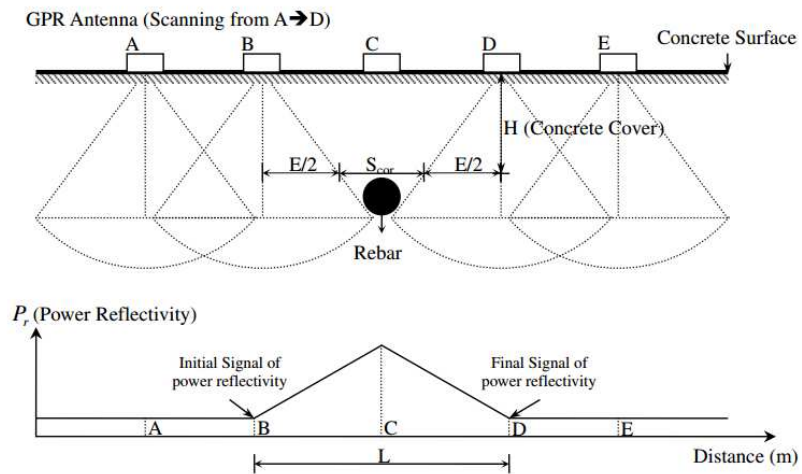


Figure 3-13 Physical model of GPR scan of rebar in concrete (Chang et al. 2009)

Leucci, G. (2012) used two different antenna orientations to scan the rebar in concrete, as shown in Fig. 3.14. First, the transmitter and receiver of the antenna were perpendicular to the rebar during the scan, and second, the antennae were rotated by 90 degrees so that the transmitter and receiver became parallel to the rebar during the GPR scan. It was shown that the perpendicular orientation gave a stronger amplitude response than the parallel orientation of the rebar. A correlation of the ratio of maximum amplitude from the rebar in both antenna orientations was tried, with the diameter of the rebar as shown in Fig. 3.15.

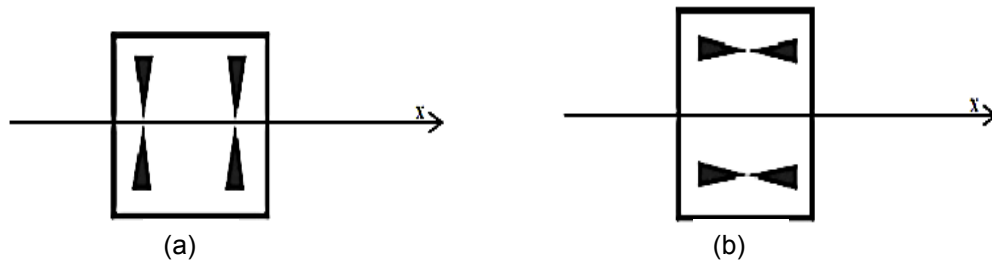


Figure 3-14 Antenna orientations: (a) co-polarized; (b) cross-polarized (Leucci, G. 2012)



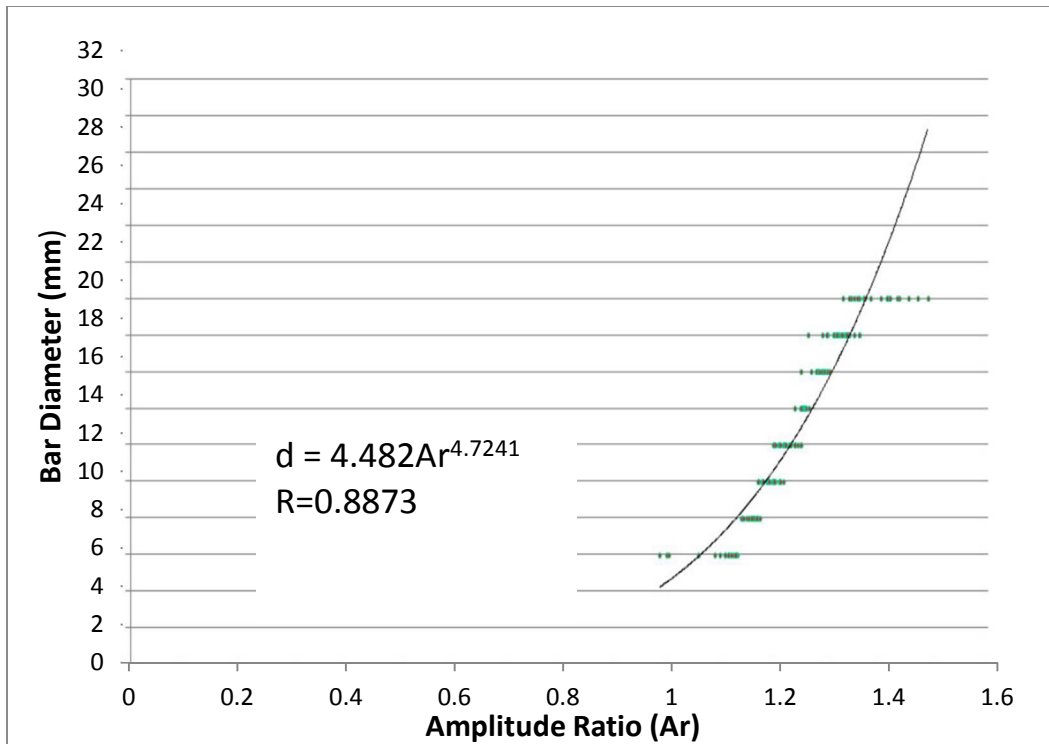


Figure 3-15 Correlation between bar diameter and amplitude ratio (Leucci, G. 2012)

Zanzi and Arosio (2013) used the concept of Radar Cross Section (RCS) of the rebar. RCS is a quantity which indicates the relation between amount of energy going to a target from the GPR antenna and the reflected energy from the antenna. This study showed that the ratio of RCS in co-polar and cross polar direction was related with the rebar diameter. But sensitivity and accuracy of the method was dependent on the frequency of the antenna. It was demonstrated that RCS ratio of different rebar diameters had different sensitive zones based on the frequency of the antenna used in scanning (Fig. 3.16). A finite difference time domain (FDTD) model was established to compare the test results with theoretical results. Figure 3.16 shows that for smaller diameter of rebar, the higher antenna frequency found a steady relation between RCS

ratio and diameter. As the diameter of the rebar increased, the lower frequency antenna was steady but the higher frequency RCS ratios started fluctuating.

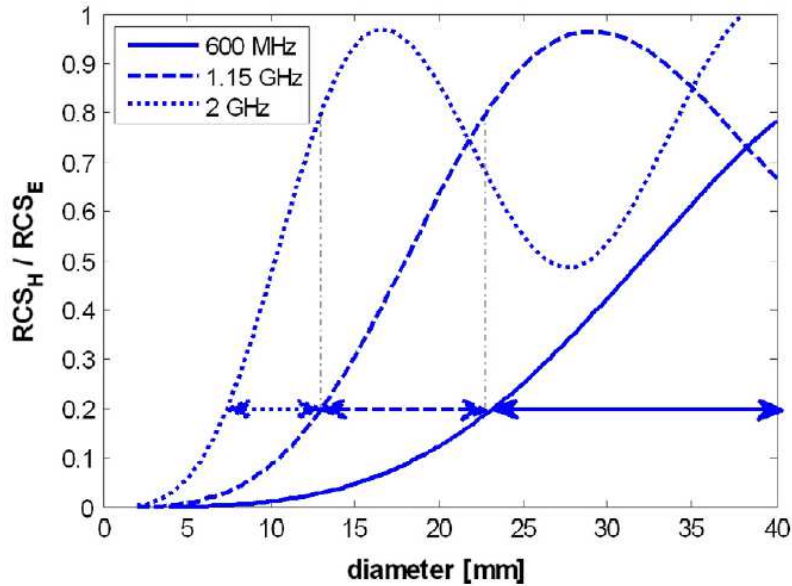


Figure 3-16 RCS ratio for three different antenna frequencies (Zanzi and Arosio, 2013)

### 3.3 Corrosion Background

Corrosion happens when the passive film on the rebar surface in reinforced concrete breaks down mostly by chloride ions (Bertolini et al., 1996). Corrosion is an electrochemical process and electrochemical galvanic cell forms in concrete during corrosion process. The rebars in concrete acts as anode and also as cathode. The pore water in concrete acts as an aqueous medium and carries the chloride ions to the rebar. The pH level of concrete surrounding the rebar is very high (12 to 13) due to the presence of alkaline oxides as  $\text{Ca}(\text{OH})_2$ . Due to carbonation of concrete or ingress of chloride ions, the pH level goes down close to 7 and the anodic and cathodic reactions of corrosion initiates. The following possible anodic reactions (Eq. 3.8 to Eq. 3.13) can happen based on the pH of concrete, presence of aggressive anions, and presence of adequate electrical potentials at the vicinity of steel surface (Ahmad, 2003).



The following are the possible cathodic reactions



The iron oxides and hydroxides form the rust and their volume is two to four times higher than that of steel. The extended volume creates internal tensile stress in concrete and it starts to crack. As corrosion level increases, the cracking may cause spalling of concrete from the surface of the rebar and expose it directly to outside environment. The stages of corrosion buildup are shown in Figs. 3-17 and 3-18.

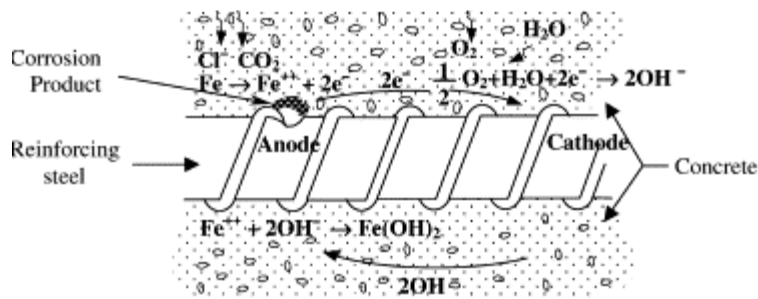


Figure 3-17 Electrochemical Reactions during corrosion of reinforcing steel in concrete (Ahmad, 2003)

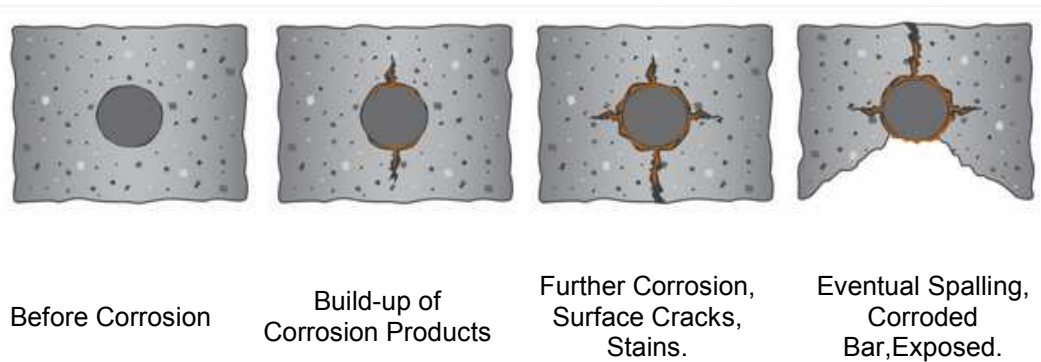


Figure 3-18 Corrosion of steel reinforcement in concrete (The Helpful Engineer, 2010)

The detection of concrete corrosion is very important for the repair and maintenance of an existing structure. It is also important for the strength evaluation and service life prediction of an existing structure. The testing method is desired to be non-destructive in order to ensure minimum physical damage and minimum disruption of service. The purpose of corrosion testing is to determine the presence of corrosion process and also the intensity and rate of corrosion damage. Three main methods of non-destructive evaluation (NDE) of concrete corrosion are currently available: half-cell potential method, concrete resistivity method and the linear polarization resistance method.

### 3.3.1 Half Cell Potential Method (ASTM C876-09, 2014)

The corrosion potential of the steel can be measured from the surface of the concrete using a standard half-cell. The measured potential indicates the probability of corrosion at the point of measurement. No quantitative information can be obtained by this method as the output is probability based. The schematic diagram of the half-cell potential method is shown in Fig. 3.19. This method is not totally non-destructive because it needs at least one rebar to be physically exposed for direct electrical connection.

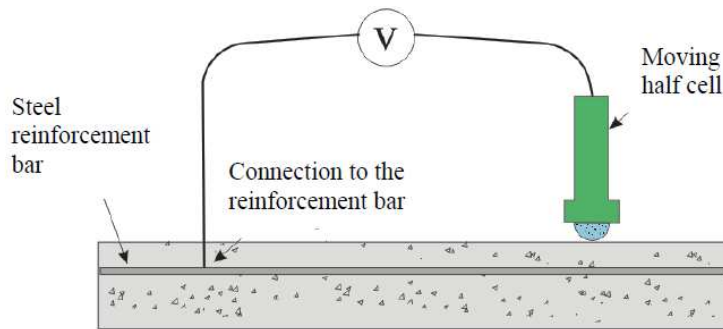


Figure 3-19 Half cell potential mapping (Millard and Sadowski, 2009)

### 3.3.2 Concrete Resistivity Method (ASTM WK-37880, 2012)

This device includes four electrodes. The outer two electrodes generate a small amount of current and the inner two electrodes (Fig. 3.20) measure the potential, which in turns indicates the concrete resistance to corrosion. A high resistivity means corrosion is less likely and a low resistivity means corrosion is more likely. However, like the half-cell potential method, this method also give the probability of corrosion only. No quantitative data on corrosion rate or corrosion state can be obtained. The presence of the rebar affects the readings in this method. The line of the electrodes needs to be perpendicular with the axis of the rebar. If the electrodes are placed along the length of the rebar on concrete, the rebar will create a highly conductive path for the current. As a result the difference of resistivity between the inner and outer electrodes will be negligible and hence incorrect. So, the knowledge on the rebar location is needed to avoid error in the test procedure.

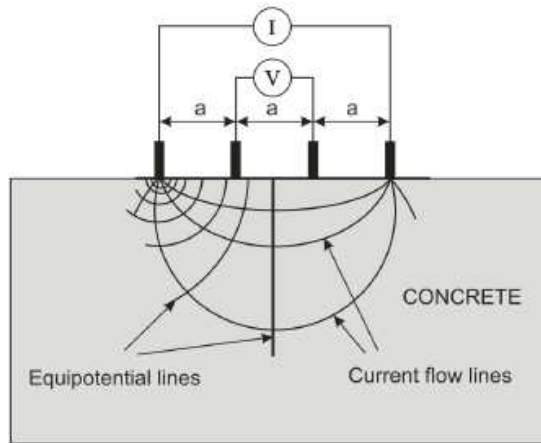


Figure 3-20 Concrete resistivity method (Millard and Sadowski, 2009)

### 3.3.3 Linear Polarization Resistance (LPR) Method (ASTM G59-97, 2009)

A half-cell electrode is used in this method to quantitatively measure the corrosion current. The charge transfer resistance at the steel surface is measured, which is inversely proportional to the corrosion current. A schematic view of the test setup is shown in Fig. 3.21. Like the half-cell potential method, this method needs direct connection to the steel rebar which makes the procedure partially destructive. This method also needs information about the diameter of the rebar to calculate the corrosion current.

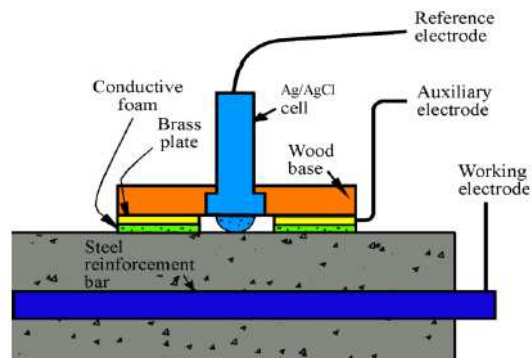


Figure 3-21 Linear polarization resistance measurement (Millard and Sadowski, 2009)

### 3.4 Corrosion Detection with GPR

GPR is widely used to detect reinforcing rebar in concrete. During corrosion, the corrosion products accumulate over the anodic steel rebar. So, the dielectric properties of concrete around the vicinity of the rebar changes. This change in material property also changes the GPR wave parameters. The use of GPR to detect the presence of corrosion is reported by several authors ( Hubbard et al., 2003). Lai et al. (2012) performed an accelerated corrosion test on a rebar embedded in concrete in laboratory environment and found the response of GPR waves at three different levels of corrossions:NaCl contamination of concrete, de-passivation of rebar and starting of rebar corrosion. Concrete specimens were produced with two rebar, an anode and a cathode. The specimens were submerged in NaCl solution and a DC current was passed through the anode and cathode. The experimental set up is shown in Figs. 3.22 and.3.23. GPR antennae frequencies of 1.6 MHz and 2.6 MHz were used. The corrosion monitoring was performed for two different concrete clear covers; 1 in. (25 mm) and 3 in. (75 mm). The maximum amplitude from the rebar was found to change at different stages of corrosion. Before the NaCl contamination, the amplitude was highest. After chloride reached the surface of the rebar and damaged the passive alkaline layer with a significant reduction in pH in the surrounding areas, the maximum amplitude from the rebar decreased. But as the corrosion process started, the maximum amplitude from the rebar started increasing with time. Figure. 3.24 shows the corresponding amplitude vs two way travel time plots of different stages of corrosion. In both cases, the behavior of maximum amplitude from the rebar surface followed the same pattern.

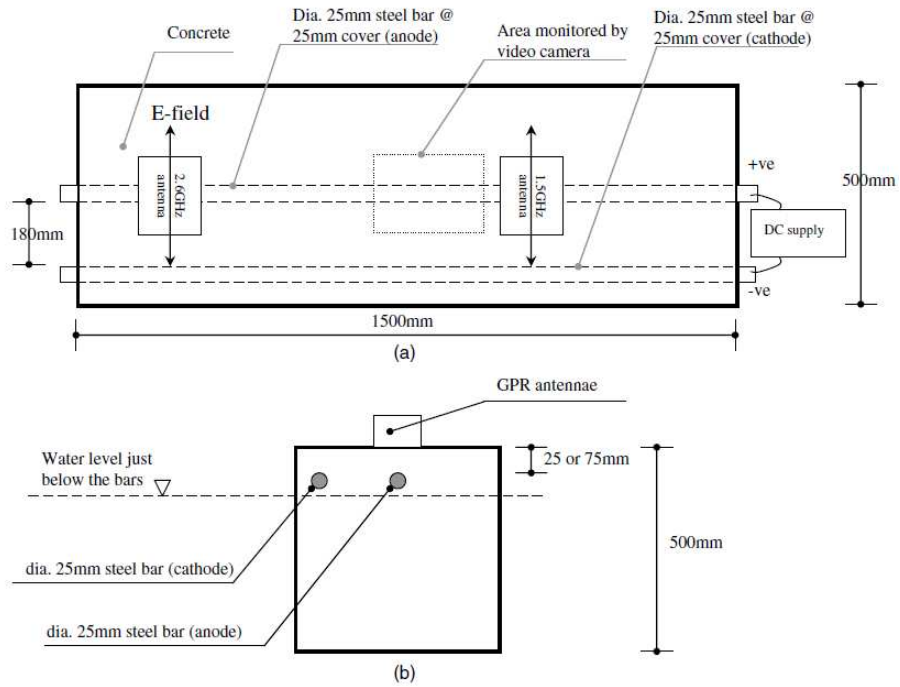


Figure 3-22 Accelerated corrosion set up, (a) plan, (b) section (Lai et al. 2012)

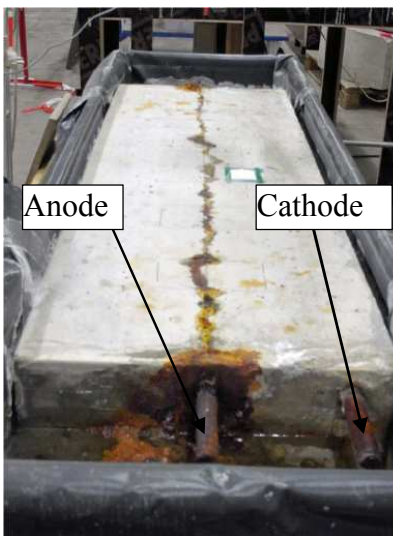


Figure 3-23 Specimen in corrosion tank with anode and cathode rebars (Lai et al. 2012)



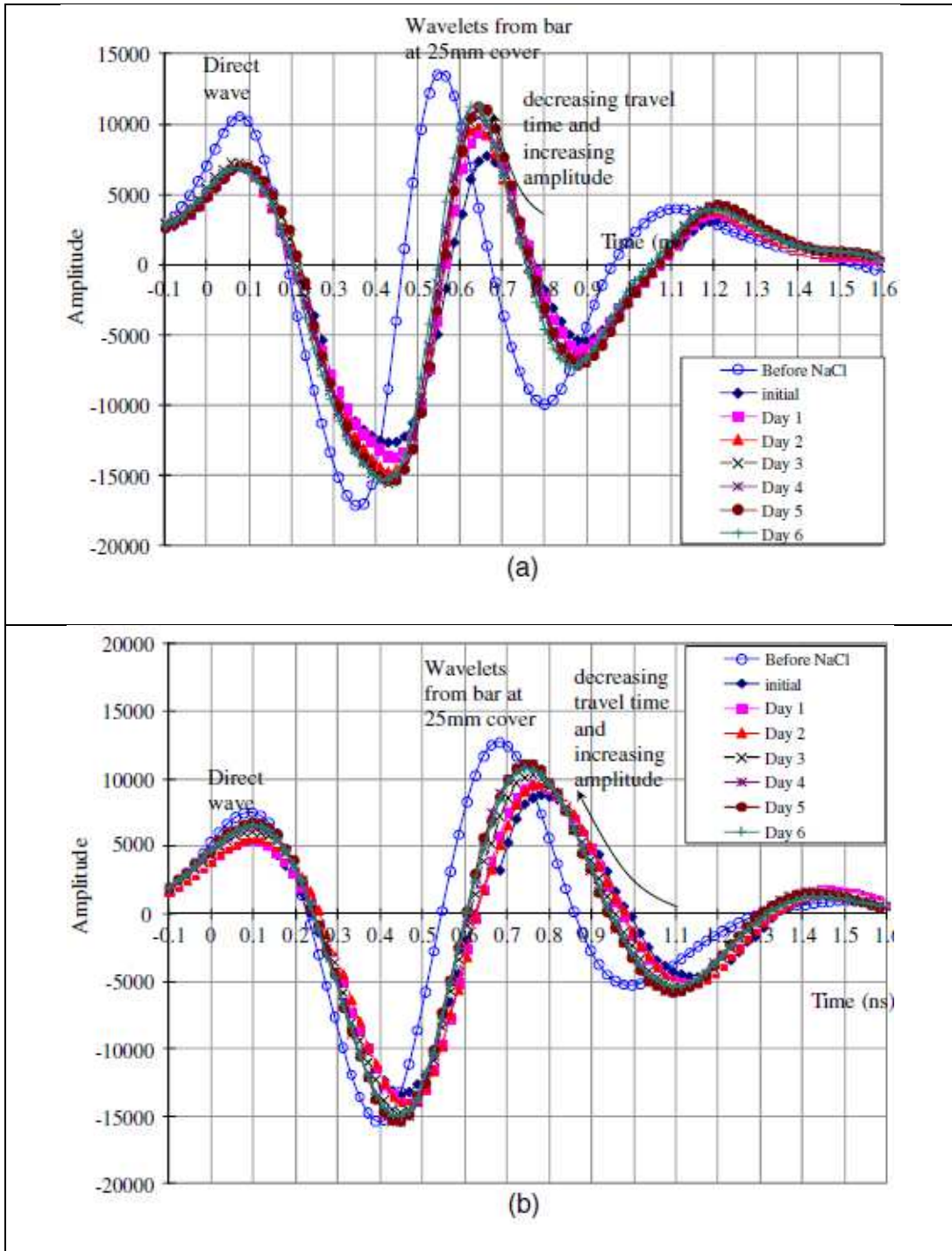


Figure 3-24 GPR A-Scan in time domain with one in. (25 mm) concrete cover: (a) 2.6 GHz antenna; (b) 1.5 GHz antenna (Lai et al. 2012)

Lai et al. (2012) also plotted the increase in amplitude from the rebar with the progress of corrosion time, as shown in Fig 3.25.

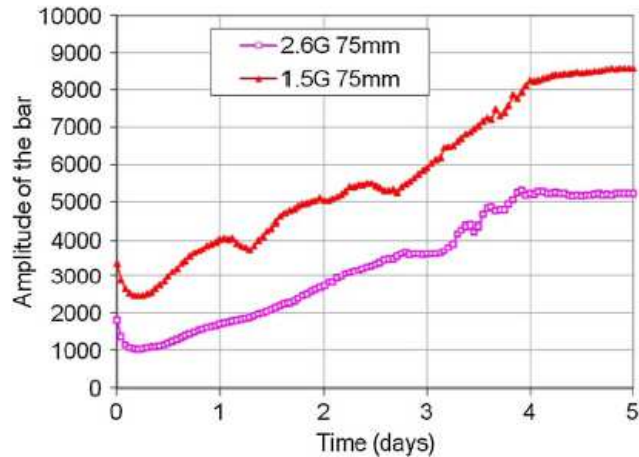


Figure 3-25 Increase in rebar amplitude with time (Lai et al., 2012)

Hong et al. (2014) performed a similar study on accelerated corrosion. The peak to peak amplitude of the direct wave (DW) and the reflected wave (RW) were taken as GPR parameters, as shown in Fig. 3.26. The change of peak to peak amplitude of DW and RW was monitored with the progress of corrosion in the specimen. It was observed that the peak to peak amplitude was increased with time, as shown in Fig. 3.27. As shown in Fig. 3.27, the changes in amplitude in anode rebar were found to be more prominent than in the cathode rebar. This is reasonable because all the corrosion products accumulated around the anode.

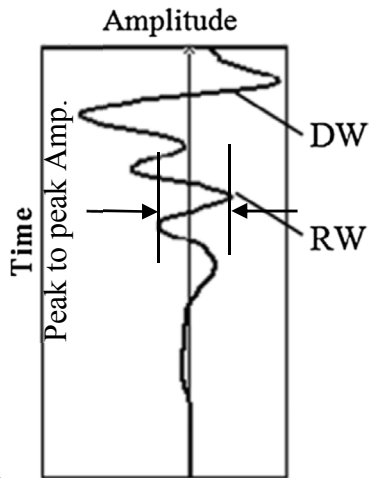


Figure 3-26 DW, RW and peak to peak amplitude (Hong et al., 2014)

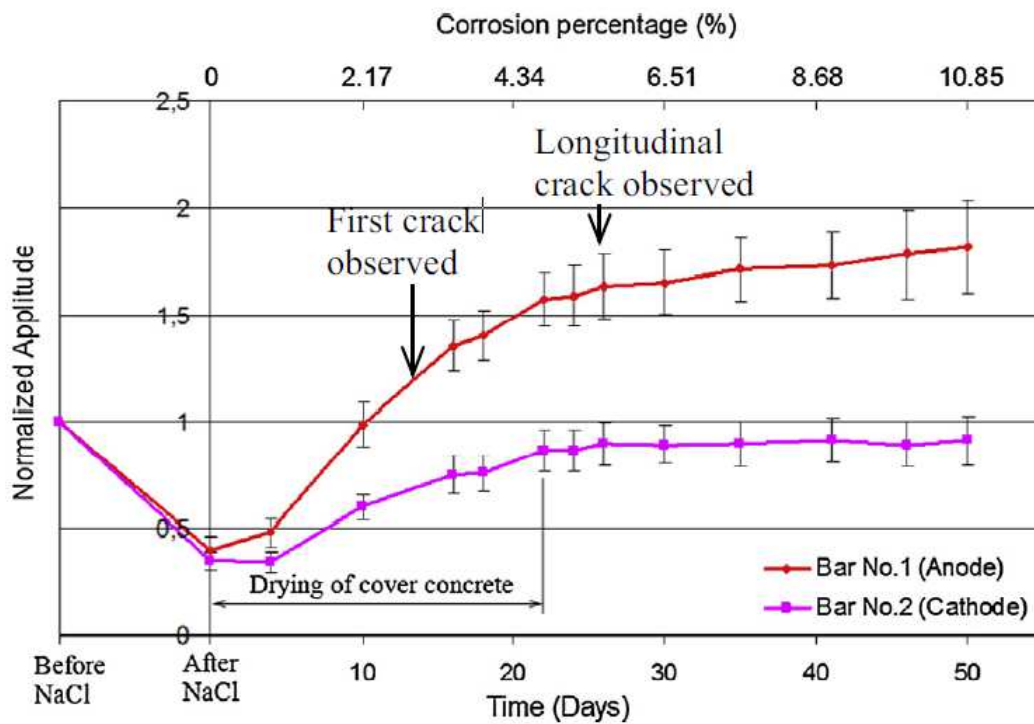


Figure 3-27 Changes in peak to peak amplitude for RW from rebar (Hong et al., 2014)

Zhan et al. (2011) performed accelerated corrosion testing using a one GHz antenna and 20 mm (0.80 in.) diameter steel rebar embedded in concrete. A test matrix

was developed where GPR reading was taken on a particular day and the corresponding mass loss due to corrosion was measured by breaking the sample following ASTM G1-03 specifications (ASTM G1-03, 2003). A relation between loss of mass due to corrosion and the change in maximum amplitude from the rebar was established, as shown in Fig. 3.28. This study is very significant; however, it did not employ a higher frequency antenna where the waveform is significantly smaller, and it did not consider the effect of dielectric property and diameter of the rebar on the GPR response.

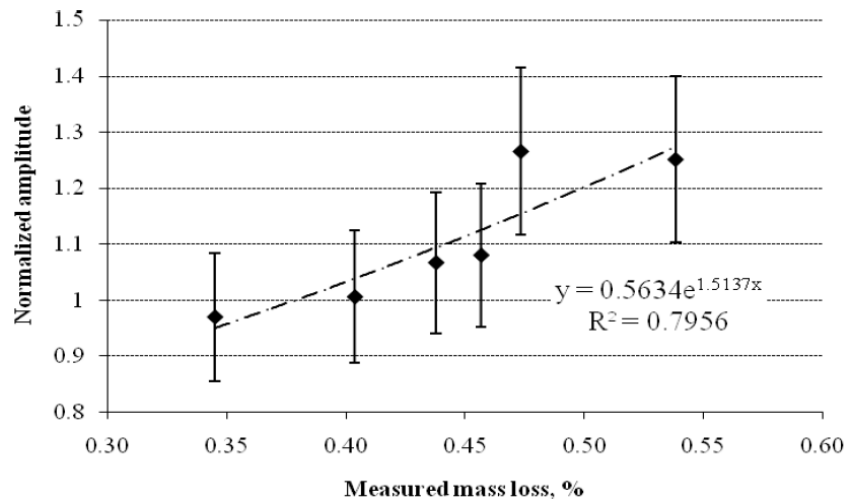


Figure 3-28 Correlation between normalized amplitude and the amount of mass loss (Zhan et al. 2011)

### 3.5 Other methods on corrosion detection

Duffo et al. (2015) found the relationship between applied current density and the amount of corrosion by using optical microscopy, scanning electron microscopy, gamma ray radiography and gravimetric measurements in an accelerated corrosion experiment on cement mortar at the laboratory. They found that gamma ray radiography may be used to detect localized corrosion in reinforced concrete. Zou et al. (2015) used fiber optic photoacoustic ultrasound generator to detect corrosion in rebar. Garboczi et al. (2010) used

electromagnetic wave on the order of 100 GHz or higher to detect two different types of corrosion product on the surface of the rebar.

Kim et al. (2011) used four different types of corrosion products and tested their permittivity and magnetic permeability with increasing frequency of the electromagnetic wave ranging from 1 GHz to 6 GHz. Figure 3.29 shows the change in dielectric permittivity of different corrosion products with increasing frequency. It was observed that the dielectric permittivity of the corrosion products do not significantly change with frequency.

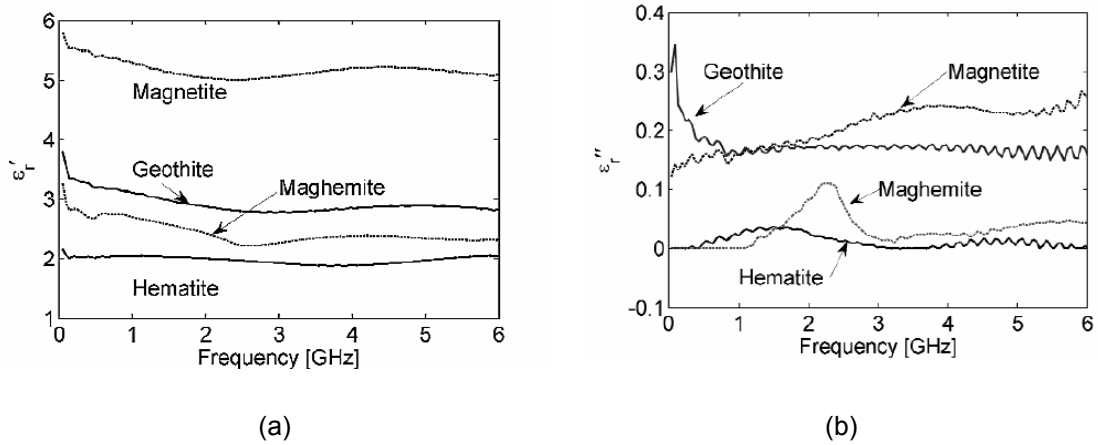


Figure 3-29 Change of dielectric permittivity  $\epsilon'$  (a) and  $\epsilon''$  (b) of different corrosion product with increasing frequency (Kim et al., 2010)

Figure 3.29 shows the change in magnetic permeability of different corrosion products with increasing frequency. It was observed that the magnetic permeability of the corrosion products significantly change with frequency especially in the range of 0 to 2 GHz. This change can be used to detect the presence of corrosion in the rebar.

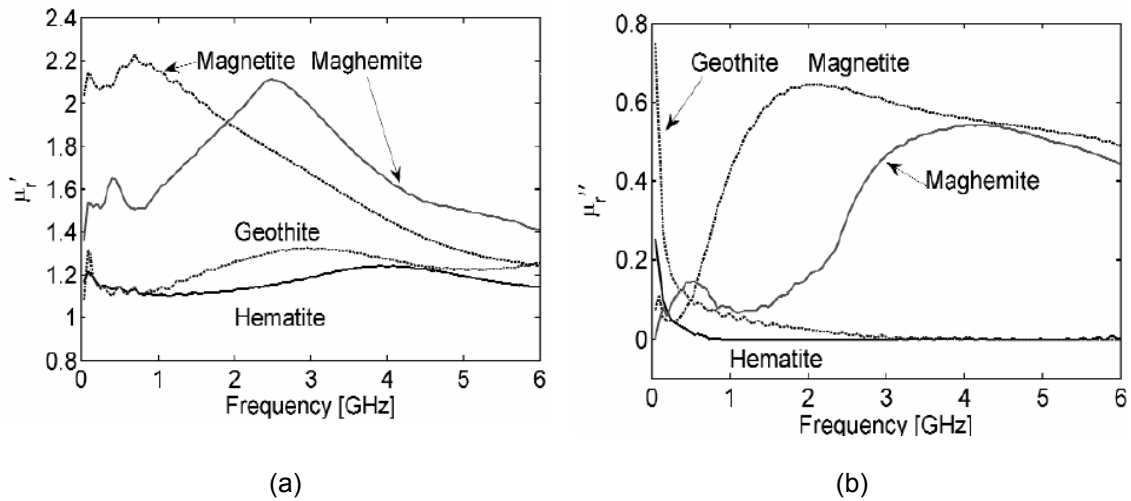


Figure 3-30 Change of magnetic permeability  $\mu'$  (a) and  $\mu''$  (b) of different corrosion product with increasing frequency (Kim et al., 2010)

### 3.6 Limitation of previous study and significance of the research

Corrosion of rebar in concrete is the one of the most significant reasons that is responsible for the reduction of design service life of the structure. Corrosion process reduces the effective area of the rebar and results in reduction of design strength of the structural component. Early detection of corrosion can significantly reduce the repair cost. When corrosion appears visually on the surface on the concrete, then it is very difficult to avoid expensive and time consuming repair scheme. Currently there is no NDT method that can provide quantitative data on corrosion. Using GPR to investigate quantitative data on corrosion will be an excellent addition to the existing usage of GPR.

In order to determine the loss of rebar area due to corrosion, it is needed to measure the reduced area of the rebar. Existing NDT methods of measuring the rebar size are not accurate enough to detect the corrosion induced change in rebar area. Existing NDT methods to detect corrosion such as half-cell potential, concrete resistivity and linear polarization can not give quantitative information on corrosion. Though GPR

has been used to detect the presence of corrosion, it has not been used to quantify loss of area or mass due to corrosion.

Currently GPR is used extensively to locate rebar and detect deteriorated area of concrete especially on a bridge deck. The same data for locating rebar and detecting concrete deterioration can be used to perform the quantitative measurement of corrosion in concrete. If done so, significant amount of time and resources can be saved. Collecting data using GPR is much quicker than any existing method of detecting corrosion such as half-cell potential. GPR is also totally non-destructive whereas half-cell potential is partially destructive.

In this research a higher frequency GPR antenna was used which is not used previously to study the quantitative measurement of corrosion. No study is done so far to relate the GPR parameters to actual physical loss of mass of rebar. A novel approach to use in oil-emulsion tank with submerged rebar as a substitute of actual reinforced concrete is used in this study. Existing studies to detect corrosion using GPR do not consider the effect of dielectric permittivity of the medium. In this study, the effect of dielectric permittivity on corrosion data of GPR is addressed. Finally a method is proposed to determine the amount of corrosion using GPR.

## Chapter 4

### Effect of various GPR parameters on rebar diameter estimation

#### 4.1 Introduction

In this chapter the effect of various GPR parameters on the diameter of rebar in concrete are tested and the results are discussed. The size of the rebar was estimated based on the GPR parameters. The size of the rebar or rebar diameter is a function of number of GPR parameters and number of physical parameters associated with the rebar. Currently there are no well-established methods to determine the diameter of rebar using GPR with expected degree of accuracy. In this phase of the study, six different diameters of rebar were used to make the concrete beam sample. Concrete beam specimens were cast and subsequently scanned by GPR. The GPR readings were then taken into post-processing software called RADAN (RADAN 7, 2014). Basic post processing of raw GPR data were done using RADAN and the important parameters related to rebar diameter were retrieved from the processed data. The parameters were plotted against rebar diameter and discussions were made on the observed results. The GPR scans and the parameters were used to estimate the rebar diameter and the accuracy of the methods were discussed.

#### 4.2 Materials and Equipment Used

Commercially available deformed steel rebars were used in this study. The concrete beams were made of plain concrete with no admixtures with ordinary Portland cement. The GPR system was acquired from Geophysical Survey System Inc. (GSSI).

##### 4.2.1 Rebars

Six different diameters of rebars were selected for the study. The diameters were ranging from #3 (10 mm) to #11 (36 mm) as showed in the following Table 4.1. Figure 4.1 shows the different diameter of rebars that were used in this study before casting them



into concrete beam. The diameters of the rebars were measured with slide calipers to confirm the actual diameters. The average diameter of with and without the rib of the rebar were taken.

Table 4-1 Different diameters of rebars

Rebar used	Diameter in in. (mm)
#3	0.375 (10)
#4	0.5 (13)
#5	0.625 (16)
#6	0.75 (19)
#8	1.0 (25)
#11	1.41 (36)



Figure 4-1 Different diameters of the rebar

#### 4.2.2 GPR System

The GPR system used in this study was made of three components; the SIR-30 main frame, 2.6 GHz frequency antenna and the hand cart with wheels having DMI (Distance Measuring Instrument). This equipment was acquired from GSSI by the Civil

Engineering Department of UT Arlington. The SIR-30 main frame was made of radar boards and operating computer to generate the radar wave through its channels. The SIR-30 had four channels for antenna output which means four antennas can be connected with it at a time. The SIR-30 was able to generate a wide range of frequencies depending on the antenna connected to it. The frequency of the antenna used in this study was 2.6 GHz. This was the highest frequency that was commercially available in the GPR industry. As per GPR theory, the resolution of a GPR subsurface image is proportional to the magnitude of the frequency of the antenna. So this antenna was supposed to give the best resolution of GPR image for our study. The penetration depth of this antenna was 1 ft. (0.3 m) which was adequate because most rebars normally locate within a few inches from the surface of the concrete. The antenna was attached with the hand cart which can measure distance. The SIR-30 can simultaneously collect the scan form the antenna and the distance reading from the cart wheels. A total GPR system is shown the following Fig. 4.2.

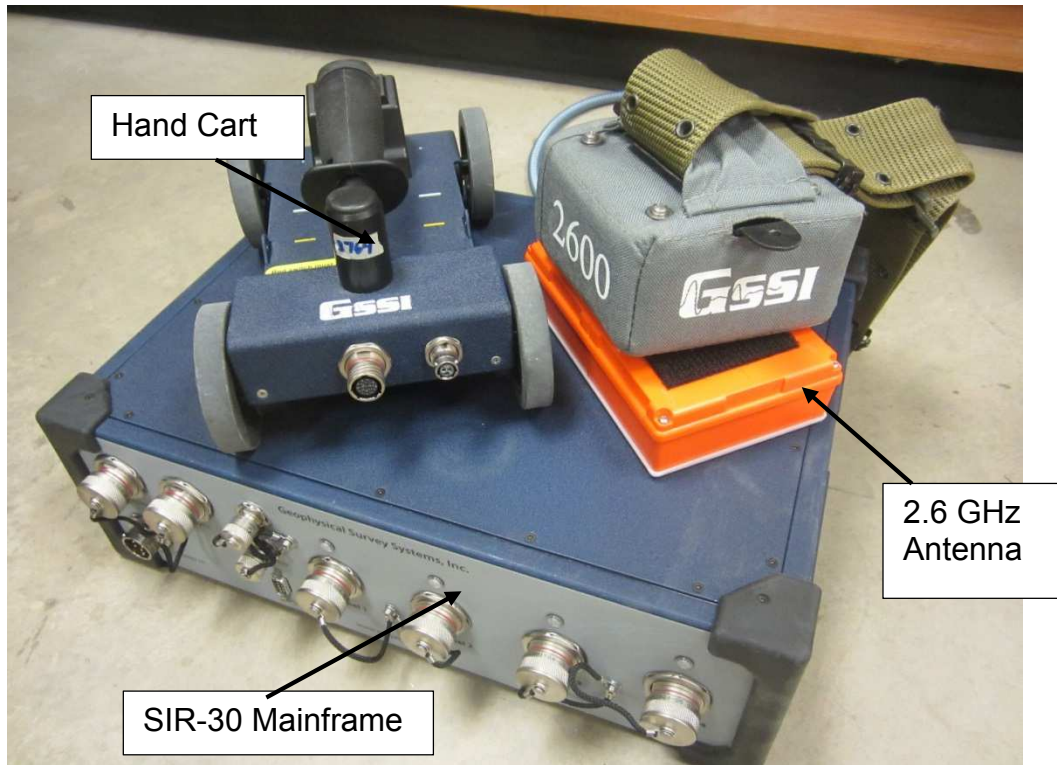


Figure 4-2 GPR System used in this study

#### 4.3 Casting of the Beams

Six beams were constructed using normal weight concrete with a water cement ratio of 0.40 and a maximum aggregate size of  $\frac{3}{4}$  in. (19 mm) with a target 28-day compressive strength of 4000 psi (27.5 MPa). All beams were casted at the same time to ensure homogenous property in all the six samples. According to theory of electromagnetic waves, the dielectric constant of concrete is the most important parameter that affects the propagation of the radar wave through a lossy media. I was seen that, hardened concrete when it is new has a dielectric constant of about 4 to 6. The beams dimensions were 54 in. (137.1 cm) long, 10 in. (25.4 cm) wide and 6 in. (15.2 cm) deep. The length of the beams was chosen to ensure that there were enough concrete at the end of the rebar to accommodate the antenna. The width of the beams was chosen

as 10 in. (25.4 cm) which is enough to accommodate the wheels of the hand cart for the scanning. The depths of the specimens were 6 in. (15.2) so that the antenna could reach the bottom of the beam to indicate it in the scan output. The spacing of the rebar was 15 in. (38.1 cm) so that the GPR response from one rebar would not interfere with the GPR response of an adjacent rebar. Three different concrete covers were used [1 in. (25 mm), 2 in. (50 mm) and 3 in. (75 mm)] in the beams to see the variation of GPR response with the depth of rebar in concrete. A schematic diagram of the concrete beam sample is shown in Fig. 4.3.

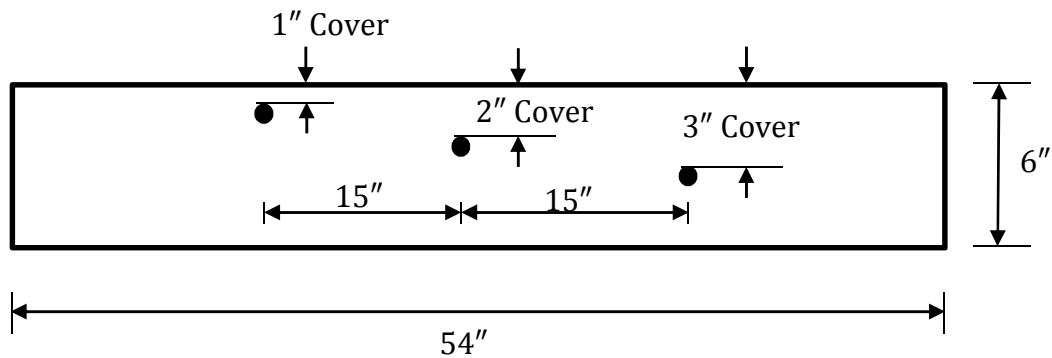


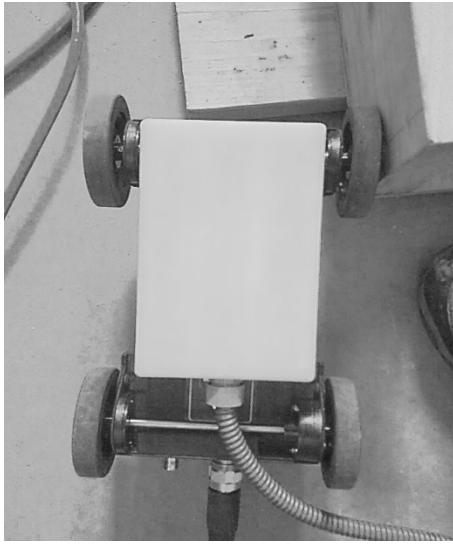
Figure 4-3 Schematic diagram of the beam specimen

The concrete were mixed according to the mix design. After the mix was ready, the concrete was immediately poured into the forms as shown in Fig. 4.4. After the casting was done, the beams were placed in a 100% humidity chamber for 28 days to finish the hydration process and to get ready for scanning with the GPR.

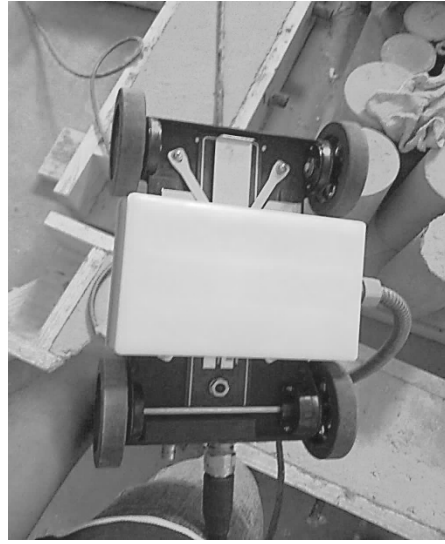


Figure 4-4 Casting of the beam specimens  
4.4 GPR scanning and data collection

The beams were ready for GPR scanning after 28 days of curing. As all the beams were made of same concrete, the dielectric constants of all the specimens were expected to be the same. The SIR-30 was set to collect 256 scan per foot of scan and the antenna were set to collect 200 samples per second. According to electromagnetic theory, the orientation of the GPR antenna influences the response form a target. GPR scans were performed with two different antenna orientations to understand the effect of antenna orientation as shown in Fig 4.5. First, the antenna axis was perpendicular to the direction of scan and second, the antenna axis was parallel to the direction of the scan. For each orientation of the antenna, three sets of data were collected. Figure 4.6 shows a data collection set up of one of the beam specimens.



(a)



(b)

Figure 4-5 Antenna orientation, (a) Normal, (b) Parallel

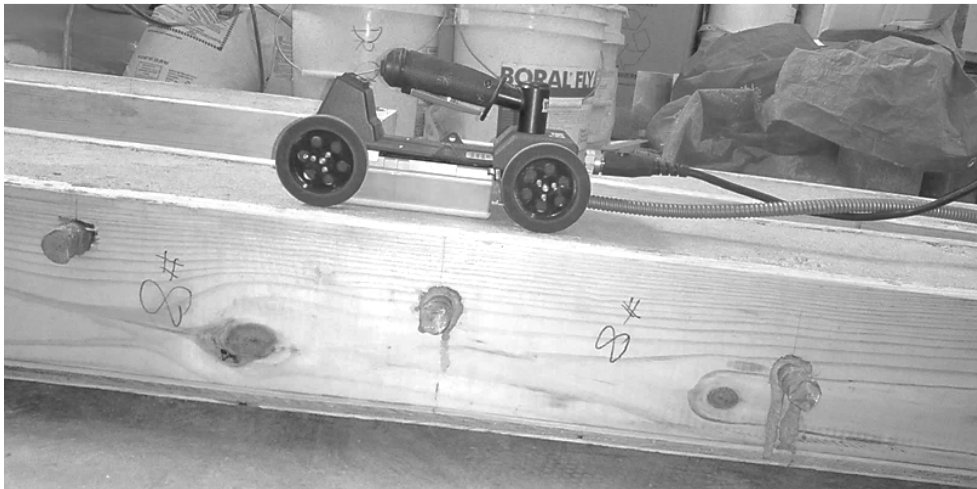
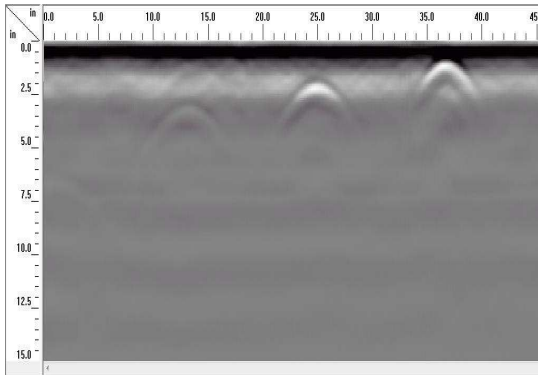
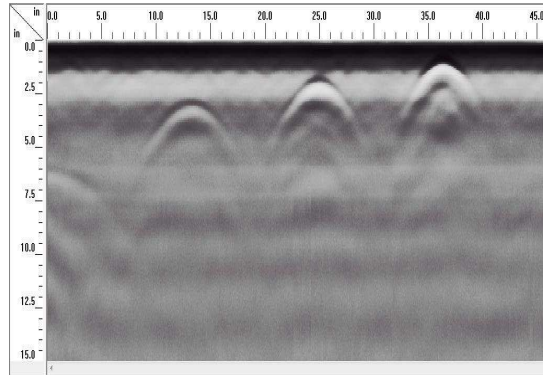


Figure 4-6 GPR scanning of beam specimen with #8 (25 mm) diameter rebar

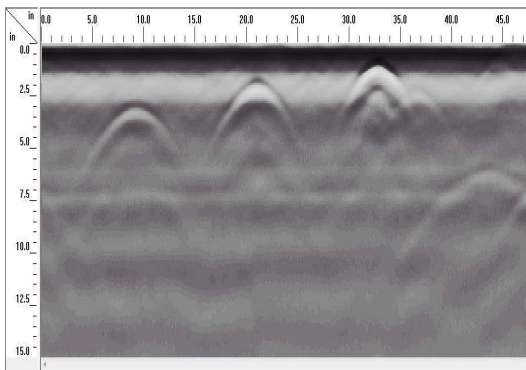
The radargram data that was collected from different rebar diameters are presented in Fig. 4.7.



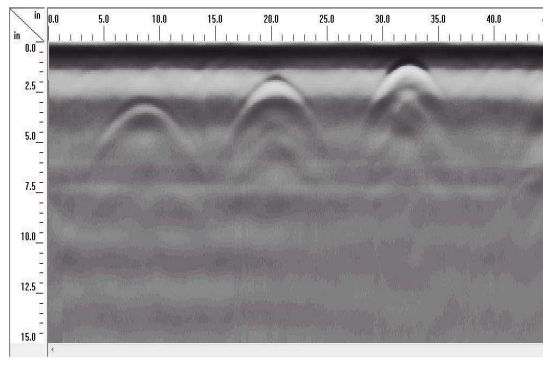
(a) GPR scan of #3 (10 mm) rebar



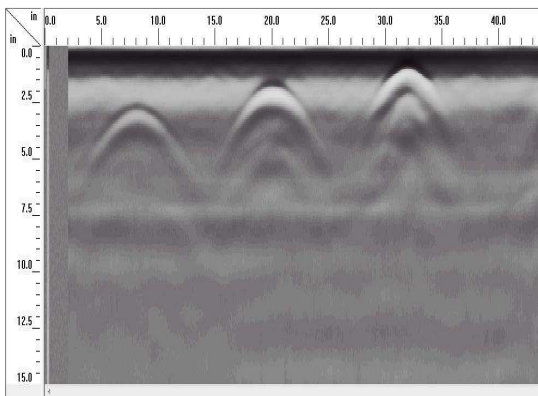
(b) GPR scan of #4 (12 mm) rebar



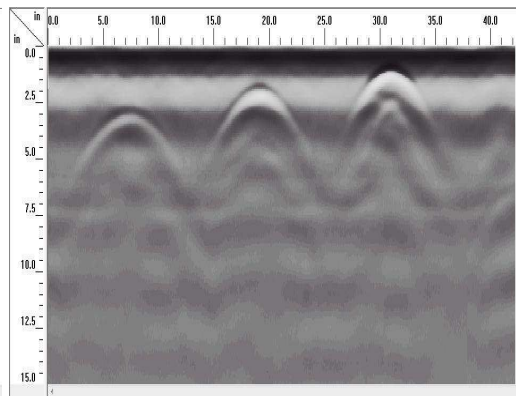
(c) GPR scan of #5 (16 mm) rebar



(d) GPR scan of #6 (19 mm) rebar



(e) GPR scan of #8 (25 mm) rebar



(f) GPR scan of #11 (35 mm) rebar

Fig. 4.7 GPR Scan of rebar of different sizes for normal antenna orientation

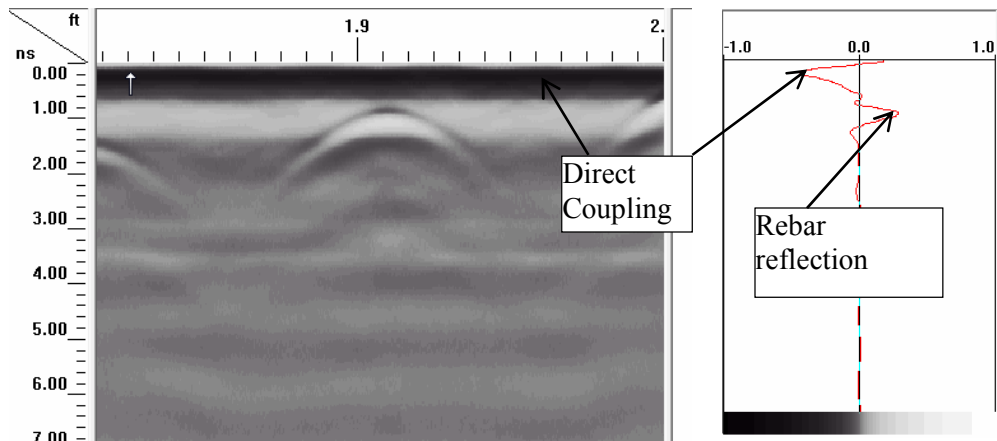
#### 4.5 GPR Data Processing

From the GPR scan of the beams in Fig. 4.7, it was seen that the rebars in the concrete were showing up as hyperbola. When the diameters were larger, the hyperbolic signatures from the rebar became brighter. However it was very difficult to differentiate among these hyperbolas without further processing. To harvest more information, the collected data were taken into post-processing software RADAN by GSSI. RADAN can improve the quality of the data as well as it can look into other parameters of GPR scan. The following three easy steps were performed on the collected data.

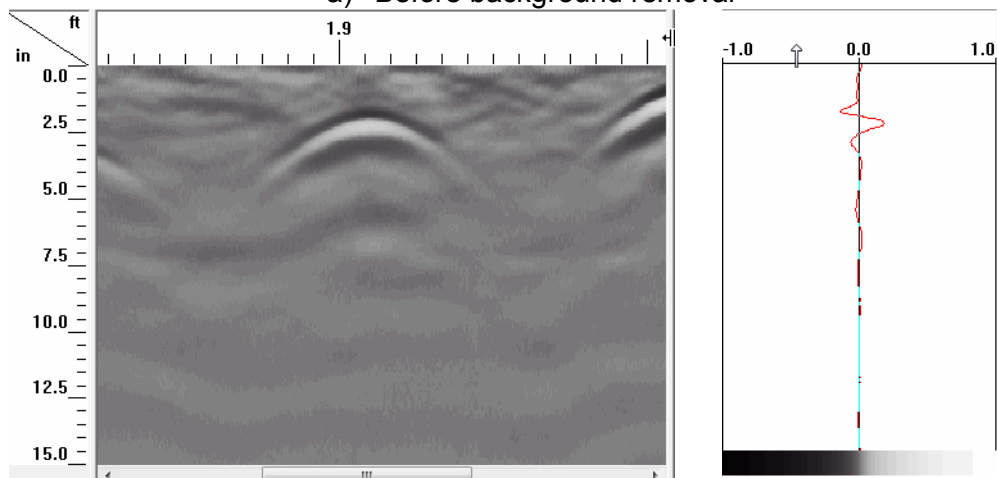
- a) Time Zero (to locate the top surface of concrete)
- b) Background Removal ( to remove noise from the scan background)
- c) Applying filter ( to remove further noise form the data)

The time zero correction for ground coupled data was not significant. Because the antenna was already in contact with ground and the gap between the antenna and the ground was negligible. Time zero correction is very important step when the data is collected with an air launched antenna. The GPR data processing using RADAN is shown in Fig. 4.7. Figure 4.7(a) shows the raw GPR radargram without any processing. The normalized amplitude of the maximum reflective amplitude of the rebar is also shown with the radargram. Figure 4.7 (b) shows the data after background removal filter was applied. Background removal eliminated the noise generated by direct coupling at the interface of concrete and air. The first peak that is observed near the surface is called direct coupling. It is shown in Fig. 4.7 (b) that the direct coupling was removed after background removal filter was applied. The data was further smoothed and the brightness of parabola was amplified by applying FIR (Finite Impulse Response) filter as shown in Fig. 4.7 (b)

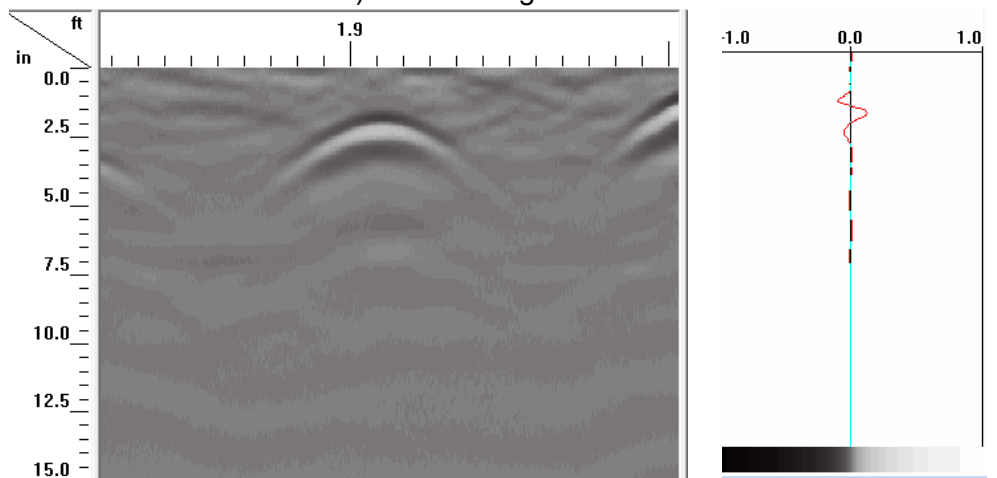




a) Before background removal



b) After background removal



c) After applying FIR filter

Figure 4-7 Steps of GPR data processing in RADAN

Each hyperbolic signature of the GPR data was consisted of many information about the embedded rebar. When the antenna was not exactly above the rebar, the amplitude of the reflected signal was smaller. But when the antenna was directly above the rebar the amplitude of the reflected signal was the maximum. This observation indicated that the diameter of the rebar was related to the maximum reflected amplitude of the GPR wave. This maximum amplitude was taken as a main parameter affecting the size of rebar in concrete in this study. As mentioned previously, each data was taken three times, therefore the maximum amplitude from a rebar was taken from the average of three scans for the same beam.

#### 4.6 Effect of maximum amplitude on rebar diameter

The maximum amplitude data were collected from data processing through RADAN. Table 4.2 shows the collected data from all of beams. These data were plotted to understand the effect of maximum amplitude on rebar size. The unit of the amplitudes in the table was GSSI specified data units.

Table 4-2 Maximum amplitudes from rebars of different sizes at different depths

Dia	Cover Depth (in.)	Normal Amp	Polarized Amp	Normal vs Polarized Ratio
#3	3	141763	497653	0.2848
	2	1867737	1014792	1.8405
	1	2705771	1697363	1.5941
#4	3	229560	561986	0.4085
	2	1940846	1232674	1.5745
	1	2715313	1993648	1.3619
#5	3	694691	806327	0.8615
	2	1752673	1511943	1.1592
	1	2116602	2884789	0.7337
#6	3	226166	791981	0.2855
	2	2455797	1634993	1.5020
	1	2861853	2569244	1.1138
#8	3	554706	984783	0.5633
	2	2635761	2083280	1.2652
	1	2496558	3013644	0.8284
#11	3	382871	840632	0.4554
	2	2810811	2243191	1.2530
	1	3235239	3711821	0.871604261

From radar theory, the ratio of maximum amplitude form two different antenna orientation can be related to the diameter of the target rebar. The effect of the ratio of maximum reflected amplitude of two different antenna orientation differed by 90° angle, is discussed in the following section for different concrete covers.

#### 4.6.1 Effect of maximum amplitude on rebar diameter

The maximum amplitudes reflected from the rebars of each of the beam specimens were plotted against the corresponding diameters for different clear cover. Figure 4.8 showed the variation of maximum amplitude of two different antenna orientations with the rebar size at a concrete cover depth of 1 in. (25 mm). The amplitude was increasing with the rebar diameter in both antenna orientation. It was observed that the amplitudes from polarized orientation of the antenna were more sensitive to change of diameters as opposed to normal orientation of the antenna.

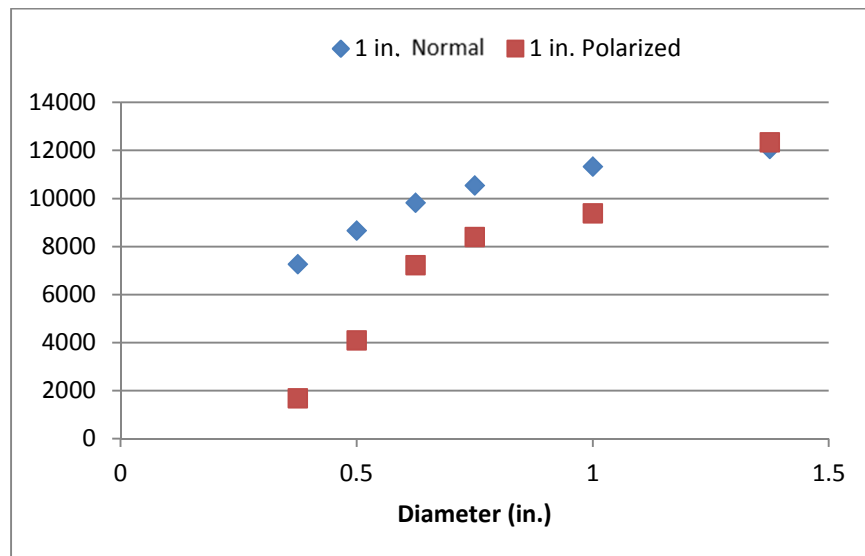


Figure 4-8 Amplitude vs rebar size at 1 in. (25 mm) cover

Figure 4.9 showed the variation of maximum amplitude of two different antenna orientations with the rebar size at a concrete cover depth of 2 in (50 mm). The amplitudes were increasing with the rebar diameters in both antenna orientation. It was observed that the amplitudes from normal orientation of the antenna were more sensitive to change of diameters as opposed to polarized orientation of the antenna. The results of amplitude vs diameter at a concrete cover of 3 in. (75 mm) did not show any consistency. This was

attributed to the high frequency of the GPR antenna. A lower frequency would have been better for a cover depth of 3 in. Furthermore the depth of the sample might not be enough. The inadequate depth of the sample created reflection of GPR wave at the bottom of the beam and that reflected waves from the bottom of the slab interfered with the reflected wave from the rebar.

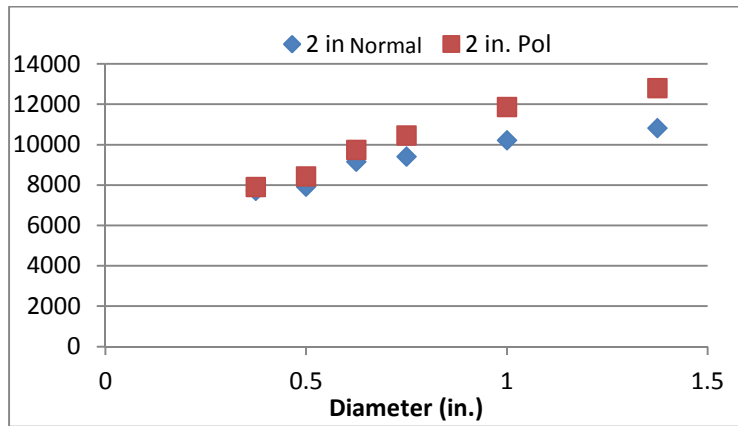


Figure 4-9 Amplitude vs rebar size at 2 in. (50 mm) cover

#### 4.6.2 Effect of maximum amplitude on rebar diameter at different depth

Figure 4.10 shows the variation of amplitude with diameter at two different concrete cover of 1 in. (25 mm) and 2 in.(50 mm). The amplitudes that are obtained from a normal orientation of the antenna were used. It was seen that rebars at 1 in. (25 mm) depth reflected higher magnitude of amplitude than rebars at 2 in. (25 mm) depth. This difference was more prominent as the diameter of the rebar increased. The amplitude vs diameter relation at 3 in. (75 mm) levels was inconclusive.

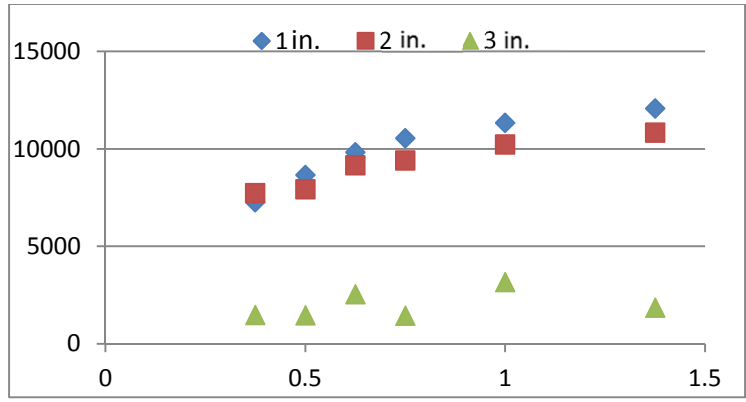


Figure 4-10 Amplitude vs rebar diameter at different depths [1 in. (25 mm), 2 in. (50 mm), and 3 in.(75 mm)]

4.6.3 Effect of maximum amplitude ratio on rebar diameter

The variation of maximum amplitude ratio from two different antenna orientations is shown in following Fig. 4.11. It was seen that the ratio gradually decreased for rebar diameter was 1 in. (25 mm) or smaller. The ratio started increasing when the rebar diameter was greater than 1 in. (25 mm) Therefore, without a prior knowledge about the diameter, this curve will not be useful to find the relation between diameter and amplitude.

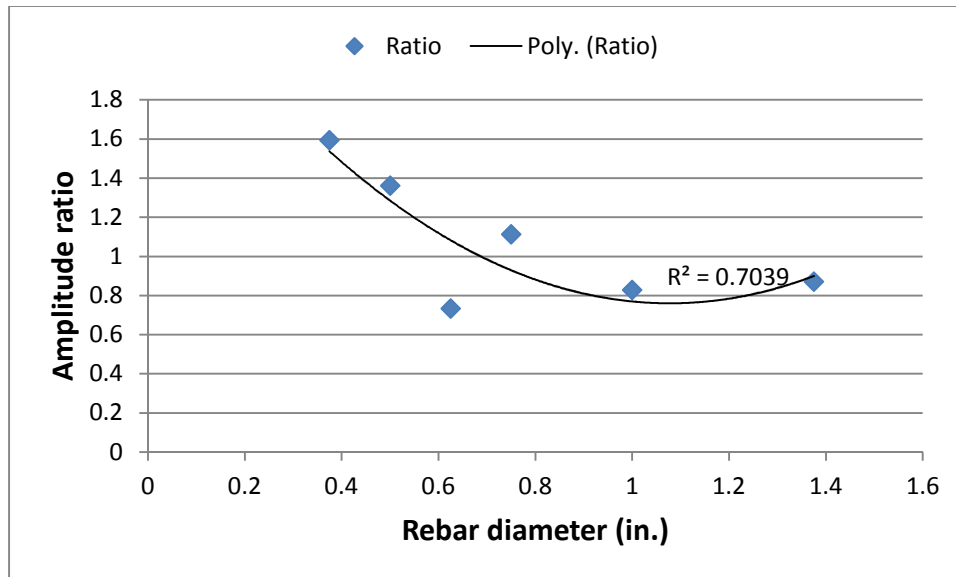


Figure 4-11 Amplitude ratio vs rebar diameter for 1 in. (25 mm) concrete cover

The variation of maximum amplitude ratio from two different antenna orientations is shown in following Fig. 4.12. It was seen that the ratio was gradually decreased for rebar diameter of 1 in. (25 mm) or smaller which was similar to the previous case of 1 in.(25 mm) concrete cover. The ratio started increasing when the rebar diameter was greater than 1 in. (25 mm). Therefore, without a prior knowledge about the diameter, this curve will not be useful to find the relation between diameter and amplitude. Similarity of the above two results indicated that the frequency of this antenna was suitable only for rebar diameter of 1 in. or smaller. To get better results with rebar diameter greater than 1 in. (25 mm), we probable need to use an antenna of different frequency.

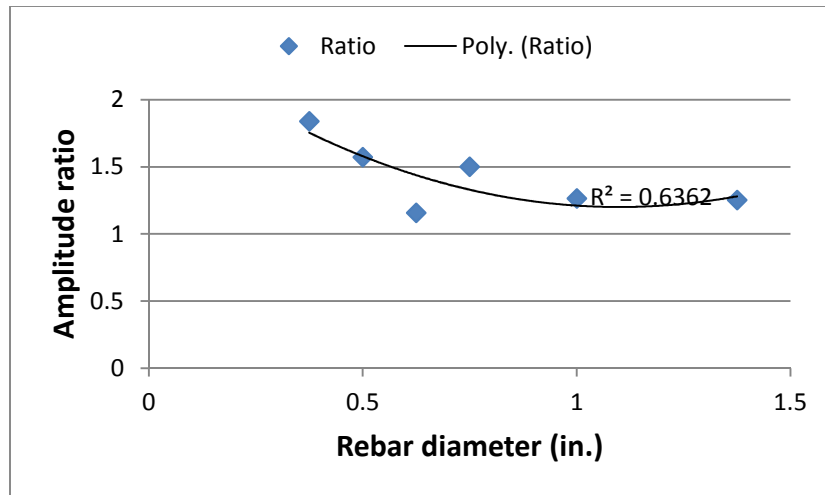


Figure 4-12 Amplitude ratio vs rebar diameter for 2 in. (50 mm) concrete cover

The variation of maximum amplitude from two different antenna orientations is shown in following Fig. 4.13. This figure did not support the results the data for the previous two concrete covers. But the direction of the curve still changed at 1 in. (25 mm). The shape of the graph indicated that the 2.6 GHz antenna used in this study was not suitable for this application when the concrete cover in 3 in. (75 mm). The graph showed a very poor correlation as well.

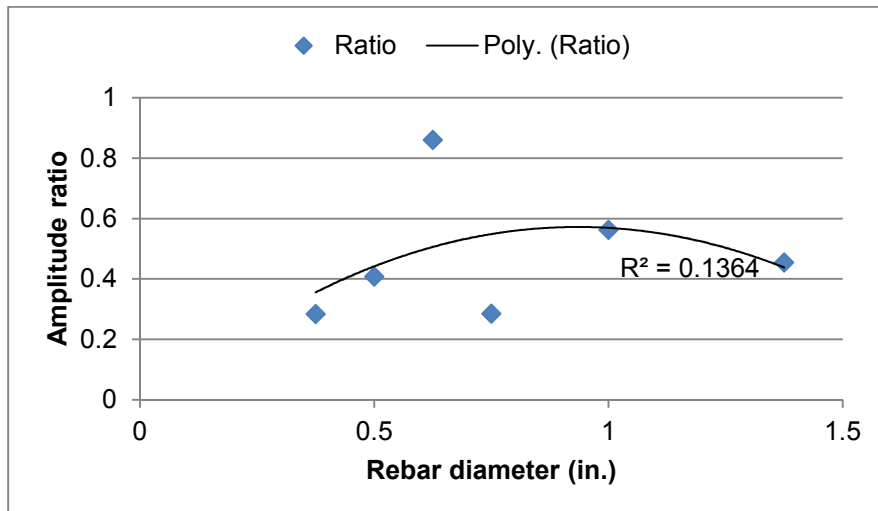


Figure 4-13 Amplitude ratio vs rebar diameter for 3 in. (75 mm) concrete cover



#### *4.6.4 Diameter Estimation from maximum positive amplitude*

The maximum positive amplitude from the normal orientation of the antenna can be used to estimate the diameter of the rebar. The maximum positive amplitude from the 90° polarized position of the rebar cannot be used as a parameter to estimate rebar because of its change of behavior with cover depth was not consistent as shown in Fig. 4.8 and 4.9. The ratio of maximum amplitude also cannot be used as a parameter to estimate the rebar diameter due to inconsistent shape of the amplitude ratio vs diameter curve as shown in Fig. 4.10, 4.11 and 4.12. Utsi et al. (2004) used numerical model to establish a relationship between the maximum amplitudes and the diameter of the rebar but their numerical model were not verified by experimental data. They also did not consider the effect of changing dielectric constant on amplitude vs diameter relationship.

A numerical model was developed to establish a relationship between the maximum positive amplitude and the rebar diameter. Six different numerical models were run to obtain maximum positive amplitude from six different diameters that were used in the beam specimen. GPRMAX 2D (Giannopoulos, 2003) was used as a software package to run the electromagnetic simulation. The model was run with a dielectric constant of 7 which was similar to the beam specimen. The rebar were placed at a cover depth of 2 in. (50 mm) in the numerical model. The normalized maximum positive amplitudes were recorded from the numerical modeling data for each different diameter of the rebar. The raw GPR data were taken into RADAN and only background removal filter were applied on the data. After applying the background removal filter, the maximum positive normalized amplitudes were recorded from RADAN for each of the different diameters of the rebars at 2 in. (50 mm) concrete cover. The normalized amplitudes were collected in a scale between 0 to 1. A normalized amplitude of 0.15 means that the maximum positive amplitude from the rebar is 15% of the overall maximum amplitude of

the scan. The normalized amplitudes were also converted to normalized decibel using the equation  $\text{dB}=20\log_{10}(\text{Normalized Amplitude})$ . Table 4.3 shows the experimental and the numerical data of maximum positive amplitudes. It was observed that the numerical values of maximum amplitudes very close but less than the experimental values of maximum amplitudes. The minimum change in normalized dB was 2.96% for #5 rebar and the minimum change in normalized dB was 12.32% for #8 rebar. Both the experimental and numerical values of maximum normalized amplitudes were increasing with the increase in rebar diameter. The detail information of numerical modeling of GPR wave is discussed in chapter 5.

Table 4-3 Comparison of experimental and numerical data

Rebar Dia	Dia (in.)	GPRMAX Data	GPRMAX (dB)	Experimental Data(RADAN)	Experimental Data (dB)	% dB Change
#3	0.375	0.1335	-17.4904	0.149108	-16.53	5.81
#4	0.5	0.15332	-16.2878	0.161808	-15.82	2.96
#5	0.625	0.1714	-15.3198	0.201372	-13.92	10.06
#6	0.75	0.19607	-14.1518	0.231473	-12.71	11.34
#8	1	0.23741	-12.49	0.277971	-11.12	12.32
#11	1.375	0.30972	-10.1808	0.298882	-10.49	2.95

The maximum normalized positive amplitudes from the rebars from numerical model and the experimental data are plotted in Fig. 4.14.

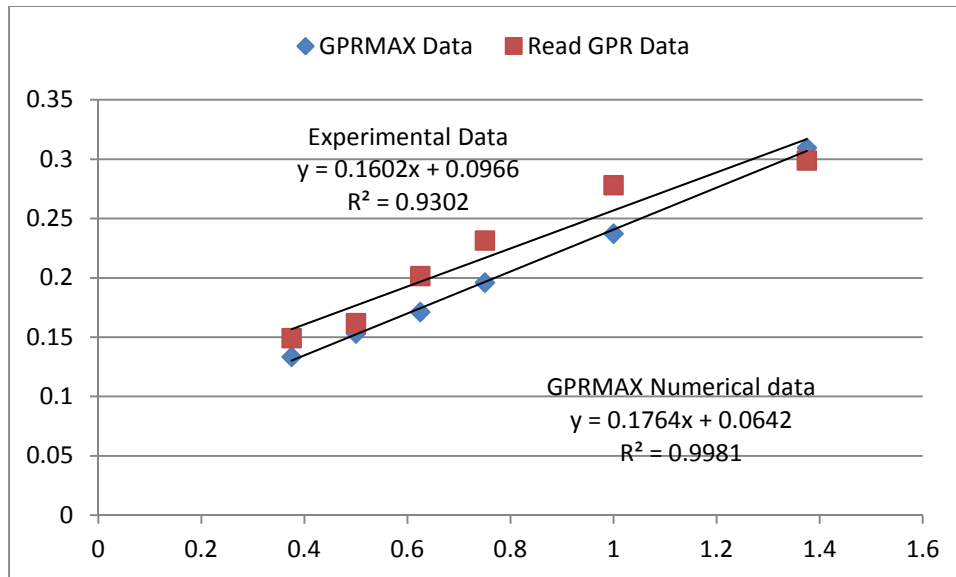


Figure 4-14 Rebar diameter vs maximum normalized amplitude for numerical and experimental data

In Fig. 4.14, the linear regression equations for both numerical and the experimental data for rebar diameter vs maximum normalized amplitudes are shown. The numerical data was showing a correlation of 99.81% which indicated an almost perfect linear correlation between the rebar diameter and the maximum positive amplitude. The experimental data were very close to numerical data with a correlation coefficient of 93.02%. The linear regression equation for experimental data were also developed and shown on Fig. 4.14. The numerical and the experimental regression curves, both can be used to estimate the rebar diameter within an accuracy of 20%.

#### 4.7 Diameter Estimation using Empirical Approach

The existing techniques of diameter estimation using GPR are discussed in chapter 2. In this part of the study, the empirical approach using digital numeric image by Chang et al. (2009) was used to estimate the diameter of the rebar. According to Chang

et al. (2009), the diameter of a rebar embedded in concrete can be estimated by the following Eq. 4.1.

$$r = \frac{L-E}{2\pi} \quad (4.1)$$

Where,

r = diameter of the rebar,

L = length of power reflectivity zone from the rebar, and

E = Energy footprint at the antenna at concrete cover depth.

Generally, a GPR antenna emits electromagnetic wave in to a medium in a conical eclipse shape. The apex of this cone is at the transmitter of the antenna as shown in Fig. 4.15 by Chang et al. The length of area of power reflectivity is shown in Fig. 3.13 in chapter 3.

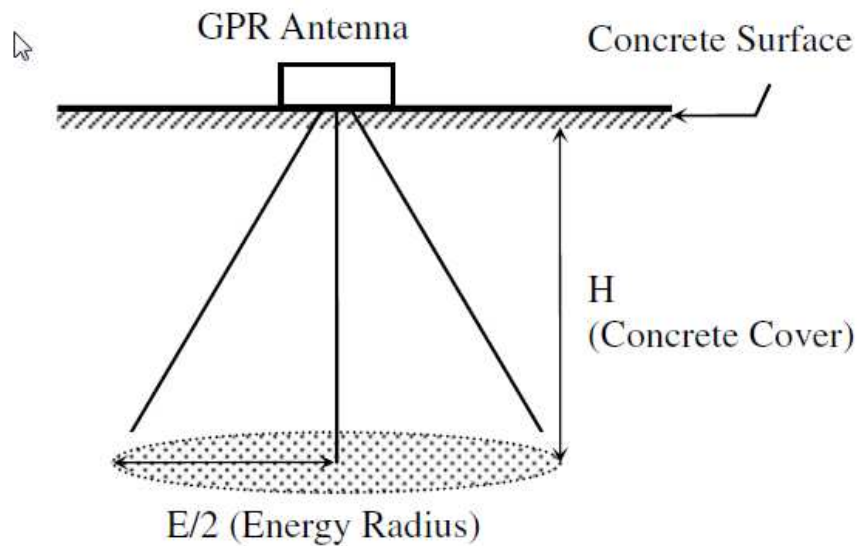


Figure 4-15 Elliptical cone and the radius of energy footprint E (Chang et al. 2009)

The energy footprint width, E , can be calculated by the following equation 3.2.

$$\frac{E}{2} = \frac{\lambda}{4} + \frac{H}{\sqrt{\epsilon+1}} \quad (3.2)$$

Where,

$\lambda$  = the wavelength from the center frequency of the antenna,

H = concrete cover depth,

$\epsilon$  = dielectric constant of the medium.

Chang et al. (2009) used 2 different diameters [#6 (0.75 in) and #10 (1.25 in)] of rebar at different cover depths. They used an antenna with a center frequency of 1 GHz. They claimed the accuracy of this method as low as 7%.

In this part of the study, six different diameters of rebars were used to verify the effectiveness of Chang et al. (2009) method for smaller diameters of bar. A different antenna having a frequency of 2.6 GHz was used which was higher than 1 GHz that was used by Chang et al. The method was also applied to GPR scans taken at different dielectric medium.

In this method, The GPR radargrams as shown in Section 3.4 were used. The GPR radargrams for each of the six different diameters were converted to digital images after initial processing. Background removal and peak extraction filter were applied to the raw GPR data as initial processing. After the converting the radargrams into digital image of jpg format, the images were opened into Matlab as shown in Fig. 4.16.

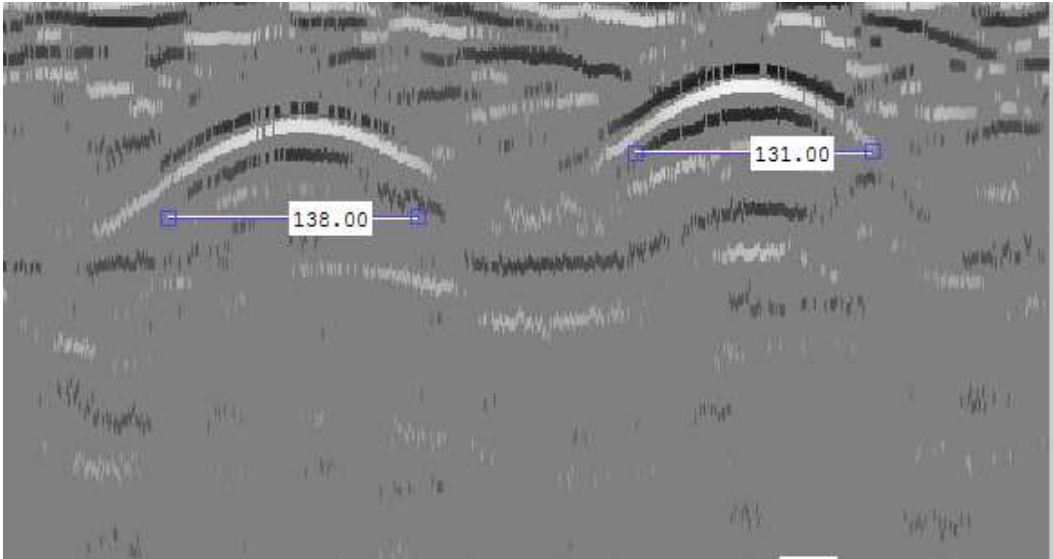


Figure 4-16 GPR radargram in Matlab

The GPR images were converted in to alpha numeric code as shown in Fig. 4.17.

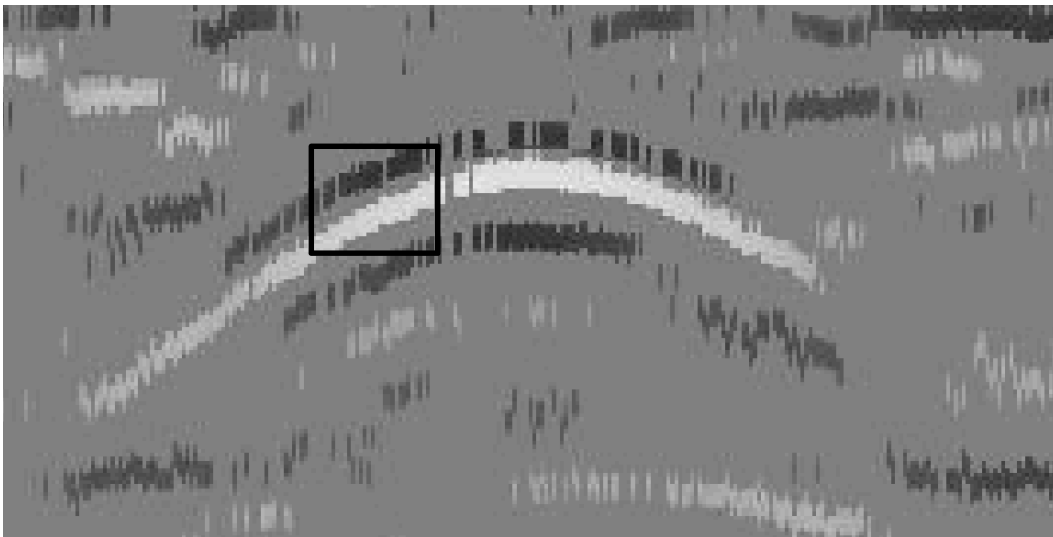


Figure 4-17 Digitized image in Matlab

The box area as shown in Fig. 4.17 was zoomed out to see the numeric codes as shown in Fig. 4.18. These numeric codes were used as the basis of estimating the initial point of power reflectivity. Where there was a significant difference in the numeric values

at the starting region of the hyperbola, that point was considered as a starting point of the length of power reflectivity. The distance between the starting and end point of the parabola was the distance L.

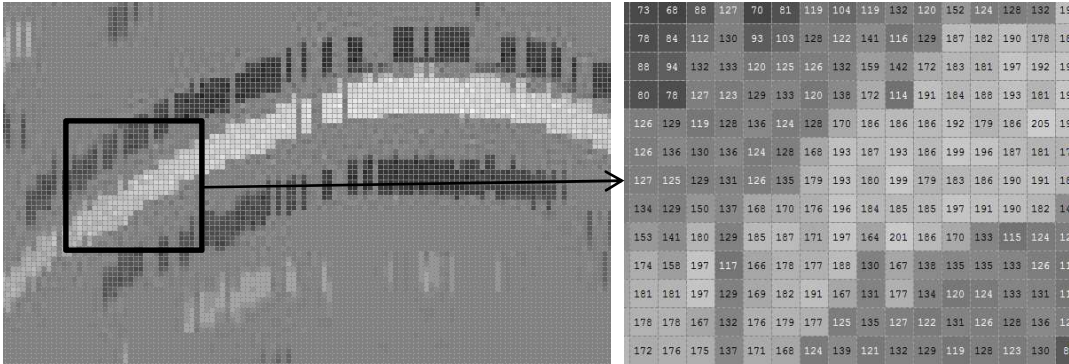


Figure 4-18 Conversion of digital image to alpha numeric codes

The diameters of the rebars that were used in this study were #3 (10 mm), #4 (12 mm), #5 (16 mm), #6 (19 mm) , # 8 (25 mm) and #11 (35 mm). Diameters were measured at cover depths of 1 in. (25 mm), 2 in. (50 mm) and 3 in. (75 mm). The diameters are listed in Table 4.1. The percentage of error of estimating the diameter were also calculated and presented in Table 4.4.

Table 4-4 Estimation of rebar diameter by Chang et al. (2009) method

Rebar Dia	Cover (in.)	E (in)	L (in)	Dia (in.)	Error(%)
#3	1	1.139	4.03	0.46	22.7
	2	1.944	4.6	0.42	12.7
	3	2.7	4.7	0.32	15.1
#4	1	1.139	4.41	0.52	4.1
	2	1.944	5.28	0.53	1.5
	3	2.7	6.52	0.61	5.4
#5	1	1.139	4.8	0.58	6.8
	2	1.944	5.86	0.62	0.3
	3	2.7	6.75	0.64	3.1
#6	1	1.139	6.72	0.89	18.4
	2	1.944	7.2	0.84	11.5
	3	2.7	7.39	0.75	0.5
#8	1	1.139	5.95	0.77	23.4
	2	1.944	7.77	0.93	7.3
	3	2.7	8.35	0.90	10.1
#11	1	1.139	7.3	0.98	28.7
	2	1.944	8.06	0.97	29.2
	3	2.7	9.6	1.10	20.1

Table 4.4 showed that for #3 (10 mm) rebar, the error of estimating the diameter was 22.7%. For #4 (12 mm) and #5 (16 mm) rebar, the error was 5.4% and 6.8% respectively. But for #6 (19 mm), #8 (25 mm) and # 11 (35 mm) rebars, the error percentages were 18.4%, 23.4% and 29.2% respectively. From the above data, it was concluded that the 2.6 GHz antenna was useful for estimating diameter for #4 (12 mm) and #5 (16 mm) dia rebars. Any diameters greater or less than these two diameters were not accurate enough. Chang et al. (2009) found a good accuracy of 7% for #6 (19 mm) and #10 (32 mm) rebars using 1 GHz antenna. So, to estimate diameter of rebars greater than #5 (16 mm) dia, 1 GHz antenna was the better option. For diameters of #3 (10 mm) and smaller bars, a higher frequency greater than 2.6 GHz is recommended.



The diameter of #5 (16 mm) rebar were estimated in the three different emulsion tanks with three different dielectric constants to investigate the effect of dielectric constant on estimating diameter by Chang et al. (2009) method. The results are presented in Table 4.5.

Table 4-5 Rebar diameter estimation by Chang et al. (2009) method at different dielectric medium.

Rebar Dia	Dielectric	Cover (in.)	E (in)	L (in)	Dia (in)	Error(%)
#5	Tank-1 $\epsilon=2.73$	1	1.139	5.85	0.749777	-20.0
		2	1.944	5.85	0.621658	0.5
		3	2.7	6.81	0.654125	-4.7
	Tank-2 $\epsilon=5.47$	1	1.139	5.66	0.719538	-15.1
		2	1.944	5.76	0.607334	2.8
		3	2.7	6.72	0.639801	-2.4
	Tank-3 $\epsilon=9.30$	1	1.139	5.08	0.627228	-0.4
		2	1.944	5.85	0.621658	0.5
		3	2.7	6.52	0.60797	2.7

From Table 4.5, at 2 in. (50 mm) and 3 in. (75 mm) cover depths, there were no major changes in percentage of error in estimating diameter with the change of dielectric constant. These results were better than the results from the real concrete samples because the medium was homogenous for the oil emulsion tanks. This homogeneity created a better GPR reading with minimal amount of noise. In tank-1 and tank-2, at a cover depth of 1 in. (25 mm), the error was as high as 20%. These errors can be attributed to improper positioning of the antenna or rebar during data collection. Overall, the dielectric constants of the medium had no effect on estimating diameter of the rebar in this method.

#### 4.7 Discussion

In this chapter, first, three GPR parameters were investigated and their effect on the size of the rebar was studied. The three parameters were:

- a) Maximum positive reflection amplitude of GPR wave form normal antenna orientation,
- b) Maximum positive reflection amplitude of GPR wave form 90° polarized antenna orientation,
- c) Ratio of amplitude mentioned in (a) and (b) above.

The results presented in this chapter showed that the normal antenna orientation displayed a steady relation between the maximum amplitude and the size of the rebar at 1 in. (25 mm) and 2 in. (25 mm) depth. The polarized orientation of the antenna showed inconsistent response at 1 in. (25 mm) and 2 in. (25 mm) depth. The parameter of ratio between maximum amplitude in two perpendicular antenna orientations was not suitable for the ranges of diameter that was used. It was showing consistent behavior at deeper concrete cover.

The diameter of the rebar was estimated using two different methods. First, the rebar diameters were measured by establishing a relationship between the maximum positive amplitude from the rebar and the rebar diameter. Both the numerical and experimental data were very close and showed good correlations. Second, the rebar diameters were measured using an empirical approach using digital image processing. It was observed that this method is sensitive to the antenna frequency and the antenna used in this study was good for the diameter of #4 (12 mm) and #5 (16mm). For rebar diameter greater than #5 (16mm), a lower frequency antenna was recommended. For rebar diameter less than #4 (12 mm), a higher frequency antenna was recommended.

In next phase of this study, the change in cross sectional area in a rebar due to corrosion is investigated using GPR. Based on the results shown in this chapter, the maximum positive amplitude of the reflected wave from rebar was taken as the principal GPR parameter that was sensitive to size of the rebar.

## Chapter 5

### Effect of various GPR parameters on corroded rebar in concrete

#### 5.1 Introduction

In this phase of the study, the variation of GPR response over the different corrosion state of rebar embedded in concrete was investigated. Rebars were corroded in an accelerated environment and a novel method of simulating the corrosion in laboratory using oil tank was developed. The effect of concrete dielectric constant on GPR response was also investigated. The dielectric constant of concrete at different stages of its service life was also simulated in the laboratory using oil water emulsions as a substitute of concrete. Eventually the amount of loss of mass from rebar due to corrosion was related to maximum amplitude of GPR response from the corroded bar.

#### 5.2 Oil Tank as a substitute of concrete beam specimen

In the previous chapter, the change of GPR response for different diameter of rebars was discussed. But one parameter was not investigated, which was the electromagnetic property of concrete. According to RADAR theory, speed and characteristics of the propagation of electromagnetic wave through any medium depends on the dielectric constant of the medium. The value of dielectric constant of a medium can range from 1 (air) to 81 (water) and every other material falls in between. The dielectric constants of normal cooking oils (canola, vegetable, sunflower seeds etc.) are close to dielectric constant of concrete. Maser (2003) showed in a study that an oil tank with a particular thickness could be used as a substitute of a concrete sample with equivalent thickness. Moreover the dielectric constant of the oil could be manipulated by adding water to the oil with the help of emulsifying agent.

### 5.2.1 Preparation of oil tank

Three oil tanks were made to conduct this study. The dielectric properties of oil of these three tanks were different. This first tank was filled with oil only. The second and third tank was filled with oil water emulsion of different proportions to simulate different dielectric property. The emulsion of tank-3 had more water content than tank-2, which made the tank-3 dielectric constant higher than that in tank-2. The thickness of the oil and emulsions in the three tanks was 5 in. (125 mm). A plexiglas cover was placed over the oil surface of each tank to facilitate the movement of radar antenna and to make the antenna ground coupled with the oil surface. An oil tank, representative of a 5 in. (125 mm) thick concrete beam is shown in Fig. 5.1.

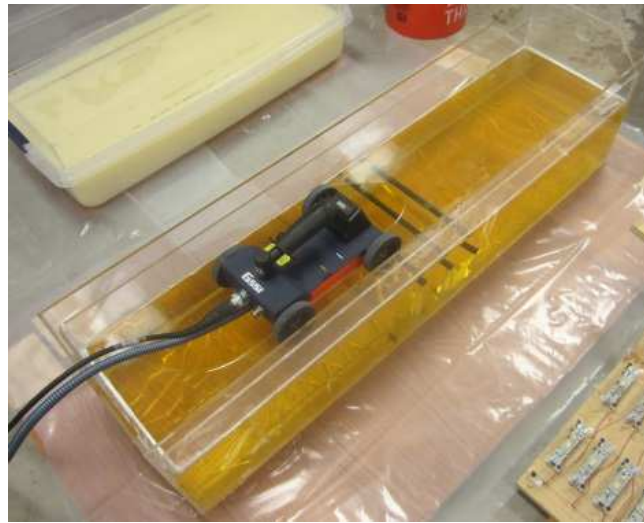


Figure 5-1 Oil tank as a substitute of concrete beam

An arrangement was made, as shown in Fig. 5.2, to support the plexiglas cover over the oil surface and to accommodate the rebars into the oil tank at a different depth. Three different depth of 1 in. (25 mm), 2 in. (50 mm), and 3 in. (75 mm) were taken as concrete clear cover as it was for the real concrete beam specimen in the previous chapter.



Figure 5-2 Arrangement to hold rebars in oil tank to simulate concrete cover

Two other tanks were prepared using oil emulsion. The emulsions were made by adding water with the oil. Water has a very high dielectric constant of 81. So adding a small amount of water could increase the dielectric constant of the emulsion by a significant amount. When concrete is dry and sound, amount of free water in concrete is almost zero, and the concrete has a very high resistivity resulting in a very low dielectric constant. As concrete gets older, water can enter into the interstitial spaces into concrete through cracks or damages caused by weathering and deteriorating effects. This presence of water into concrete increases its dielectric constant. So if an oil-only tank represents a dry concrete beam, then an oil water emulsion tank with particular consistency will be representative of old concrete. When GPR scan is performed to investigate an old structure, it is important to know how the behavior of GPR response change under this variable dielectric constants of the concrete.

In this study, sodium loryl sulphate was used as an emulsifying agent. A series of trials was performed to find the appropriate amount of water to be added with the oil so that the resulting emulsion had an appropriate and practical dielectric constant. Adding too much water would increase the dielectric beyond the limit of practical dielectric constant of concrete. Table 5.1 shows the amount of water and sodium loryl sulphate (SLS) that was used to prepare the emulsion tanks. Figure 5.3 shows an example oil water emulsion in a tank. It is noted that the transparent oil turned into a white colored liquid after water and the emulsifying agent were added.

Table 5-1 Components of the oil and emulsion tanks

Tank No.	Water Volume (ml)	SLS Volume (ml)	Total Volume (litres)
Tank-1	0	0	41.6
Tank-2	300	100	41.6
Tank-3	500	150	41.6



Figure 5-3 Oil water emulsion tank

### 5.2.2 Dielectric Constant of Different Tanks

The 2.6 GHz antenna was used to determine the dielectric constants of oil in each tanks. The data were collected in time mode. A steel plate was place at the bottom of the tank, as shown in Fig. 5.4. The radar wave from the antenna at the top surface of the oil tank travelled through the oil and reflected back from the steel plate. The time required by the radar wave to finish this two way path was recorded by the GPR. This time is termed as Two Way Travel Time (TWTT). These data were taken in RADAN7 and the dielectric constant were measured after basic processing of the data. Equation 4.1 was used to find the dielectric constant from the TWTT.

$$\epsilon = \frac{c^2 t^2}{d^2} \quad (4.1)$$

Where:

$\epsilon$  = the dielectric constant or relative permittivity of the medium

$c$  = velocity of light,

$t$  = TWTT,

$d$  = distance travelled by radar wave.

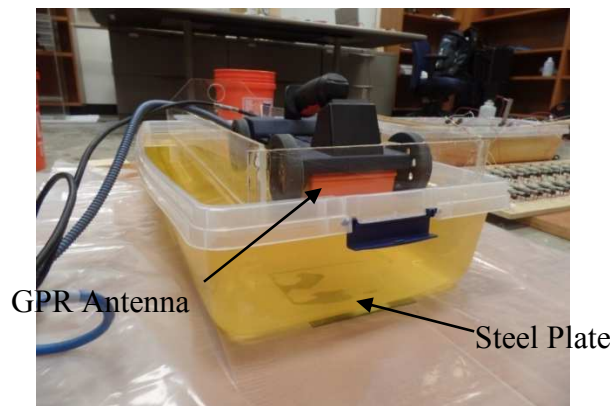


Figure 5-4 Determination of Dielectric Constant of oil tank with steel plate



In Fig. 5.5, the radargram of the three tanks are shown. The horizontal axis is the number of scans and the vertical axis is the two way travel time. The bright reflection in each of the radar gram was the reflection from the steel plate. It is obvious that the radar wave was taking more time to travel the same distance as it proceeded from tank-1 to tank-3. So it is obvious that the velocity of GPR wave was highest in tank-1 because the TWTT for the GPR wave is lowest. Similarly the speed of radar wave was slowest in tank-3 because the TWTT was highest. The TWTTs for the tanks were converted to dielectric constants using the conversion equation. The values are listed in Table 5.2.

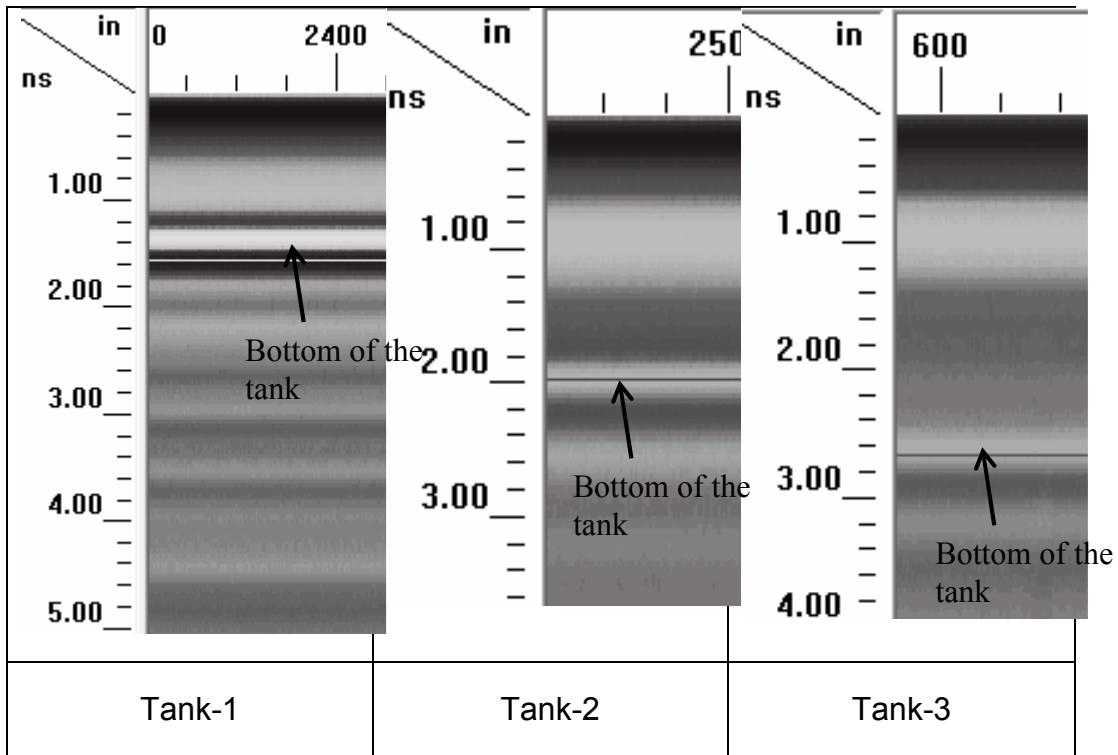


Figure 5-5 Radargrams of the three tanks

Table 5-2 TWTT and dielectric constant of different tanks

Tank	TWTT (nS)	Dielectric Constant
1	1.4	2.73
2	1.98	5.47
3	2.58	9.3

### 5.3 Validation of oil tank as a substitute of concrete beam

The three oil tanks were representative of concrete beams with dielectric constants of 2.73, 5.47 and 9.3, respectively. Steel rebars of three different diameters were placed in each tank. The diameters of the rebars were #3, #4 and #5 (10, 12 and 16 mm dia). The rebars were placed at three different depths of 1 in. (25 mm), 2 in. (50 mm), and 3 in.(75 mm) in the liquid. GPR scans were performed for each depth of the rebar into the tanks. It was expected that the GPR radargram of the rebar in oil tank would be similar to GPR radargram of rebar embedded in real concrete beam, as observed in the previous phase of this study.

There were two major advantages of using the oil tanks instead of real concrete beam. First, it is really difficult to make concrete with variable dielectric constants. So, using water emulsion was very helpful to see the effect of dielectric constant on GPR response. Second, concrete is a heterogeneous material and its dielectric constant is not exactly same everywhere. The dielectric constant of concrete is the resultant of the dielectric constants of its components, which are coarse/fine aggregates and cement paste. Using oil or oil-water emulsion was helpful to eliminate the uncertainty due to spatial variability of dielectric constant of concrete. Third, there was great flexibility of placing the rebar of different diameters and for different cover depths in a single water

tank. If concrete sample were made, lots of beams should have been constructed. The oil tanks eliminated the use of additional time and resources for making real concrete samples. So, the repetitive use of the tank for different rebar size and different cover depth was a great advantage. Figure 5.6 shows a GPR plot that was collected from the oil tank-1 with a #4 (12 mm dia) rebar at 2 in. (50 mm) depth from the top surface of the oil. It is observed that the radargram is exactly similar to a radargram of a real concrete specimen. The oscilloscope view was also obtained for the trace having maximum amplitude. As oil was a homogenous material, the amount of noise in the data was much less compare to data collected from real concrete sample. Therefore, it was validated that the oil tanks could be used as a substitute of concrete beams.

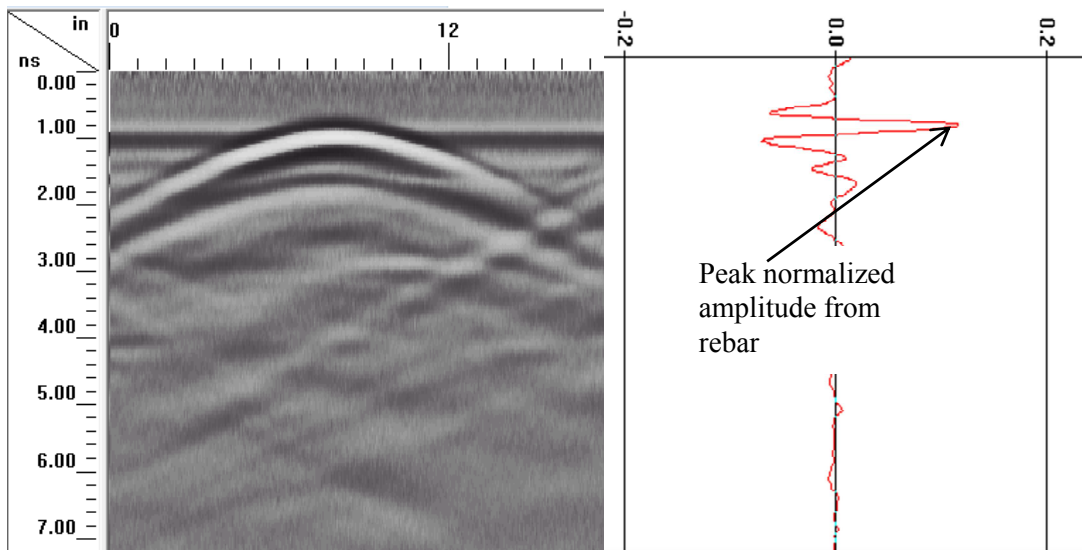


Figure 5-6 GPR Radargram data collected form oil tank.

#### 5.4 Plot of the collected data to verify the performance of the oil tanks

As mentioned earlier, three different diameters of rebars were used in each of the three tanks at three different cover depths. The maximum amplitudes from the radargram were recorded. Figure 5.7 shows the rebars that were used in the tank to record the GPR

data. The GPR parameters of data collection are listed in Table 5.3. The collected data are tabulated in Table 5.4.

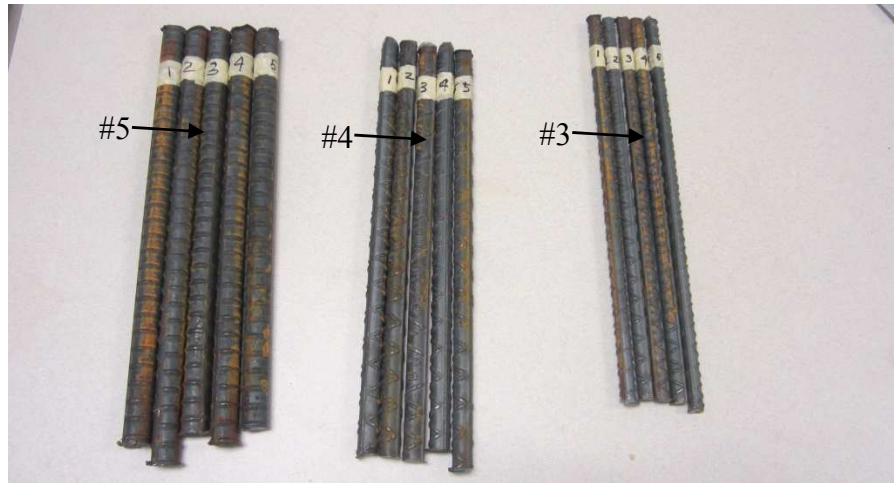


Figure 5-7 Rebars used in the oil and emulsion tanks

Table 5-3 GPR parameters for data collection

Scan per second (horizontal direction)	325
Scan per unit inch (horizontal direction)	20.38
Sample per scan (vertical direction)	256
Time range in vertical Direction	7 nS

Table 5-4 Maximum amplitudes form rebars in different tanks

Rebar Dia	Cover (in.)	Maximum Amplitude		
		Tank-1	Tank-2	Tank-3
#3	1	8936	7790	6489
	2	8381	6364	5912
	3	7269	3914	1802
#4	1	8328	7538	6929
	2	8089	7088	6919
	3	6832	5623	4801
#5	1	8398	7421	7514
	2	8522	7012	7530
	3	7319	5956	5540

Figure 5.8 shows the variation of maximum amplitudes from the rebars with increasing cover depth for #3 (10 mm) rebar. The maximum amplitudes from the rebar are decreasing with the increase of concrete cover, which was the depth of the rebar in the oil emulsion tank. Similar curves from tank-2 and tank-3 are also plotted in the same graph. It is observed that curves from all three tanks showed similar pattern of changes. The amplitudes in tank-1 at a particular depth was higher than tank-2 and the amplitudes of tank-2 at a particular depth was higher than tank-3. The change was expected due to the gradual increase of dielectric constant from tank-1 to tank-3. Figure 5.9 and 5.10 shows similar behavior for #4 (12 mm) and #5 (16 mm) rebars. The behavior of all the three different diameters of rebar was coherent.

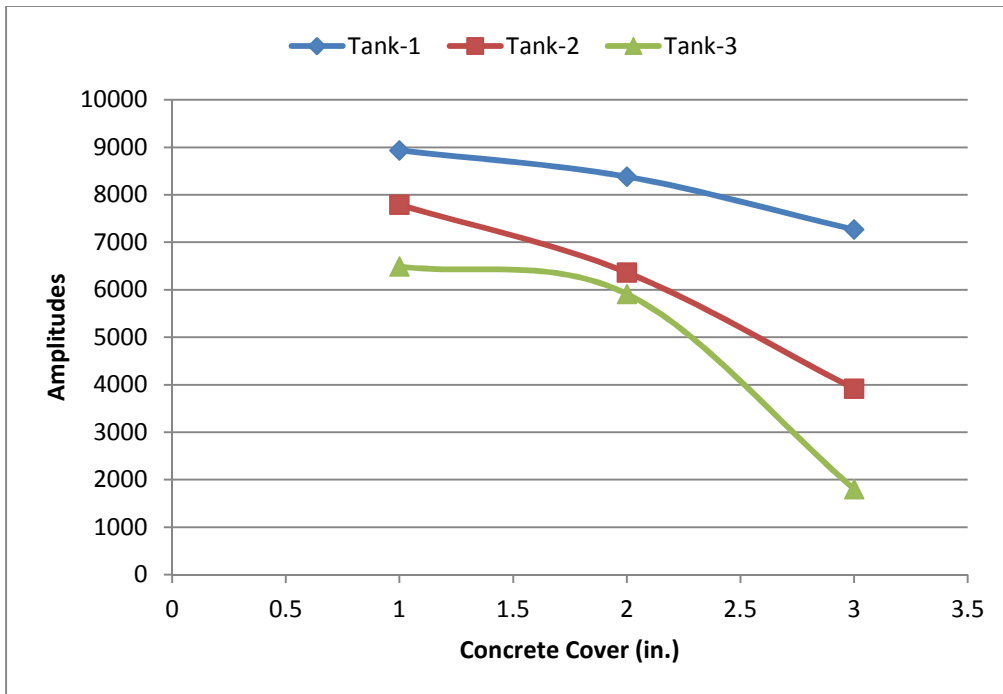


Figure 5-8 Amplitude vs cover depth for #3 (10 mm) rebar

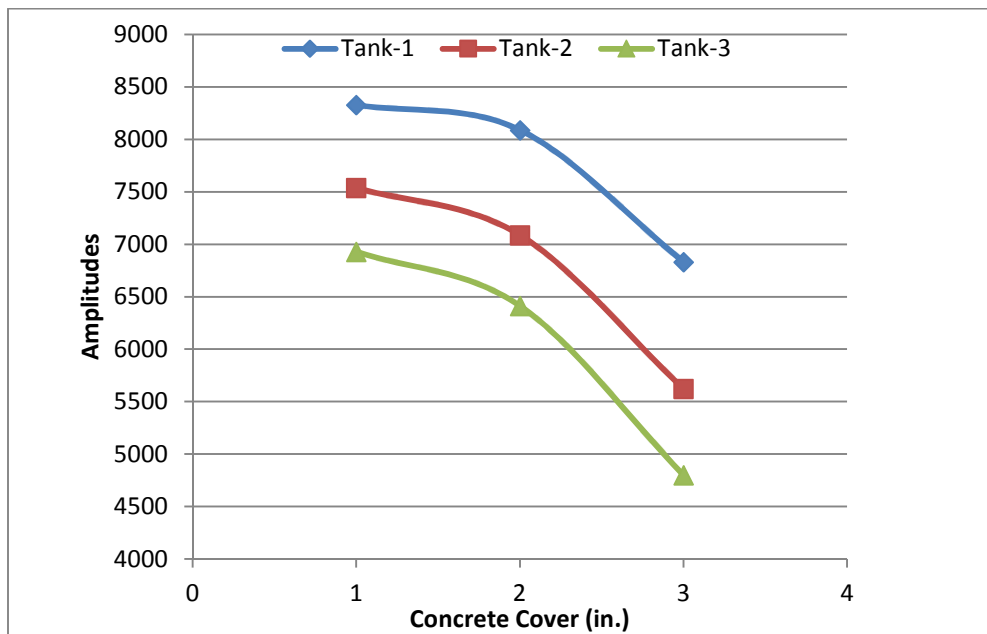


Figure 5-9 Amplitude vs cover depth for #4 (12 mm) rebar

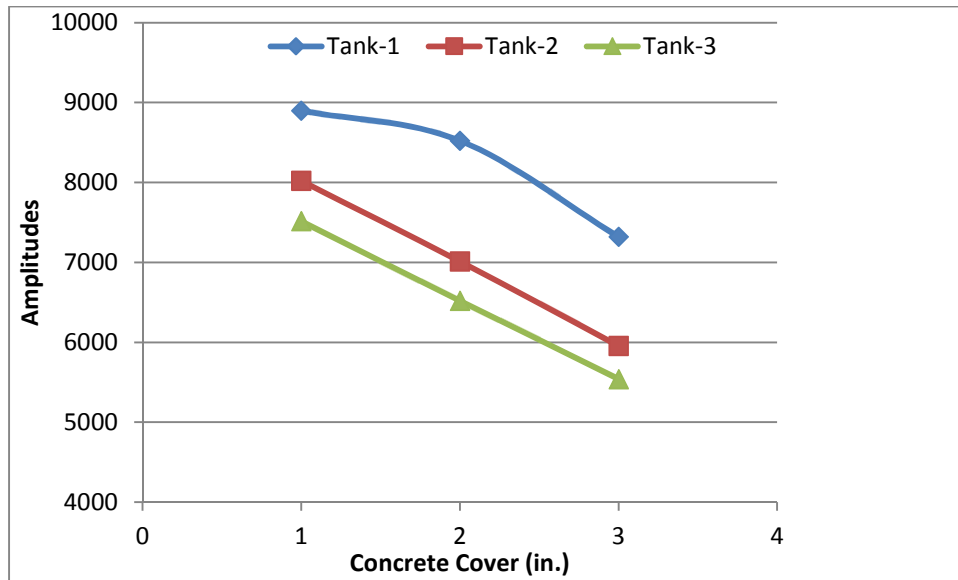


Figure 5-10 Amplitude vs cover depth for #5 (16 mm) rebar

Figure 5.11 shows the change of maximum amplitude from a #3 (10 mm) rebar with different dielectric constants. Similar graphs are produced for #4 (12 mm) rebar and #5 (16 mm) rebar, as shown in Fig. 5.12 and Fig. 5.13. The amplitudes decreased with the increase of dielectric constant at different depths. All three different diameters of rebar showed coherent behavior as displayed in in Fig. 5.11 to Fig. 5.13.

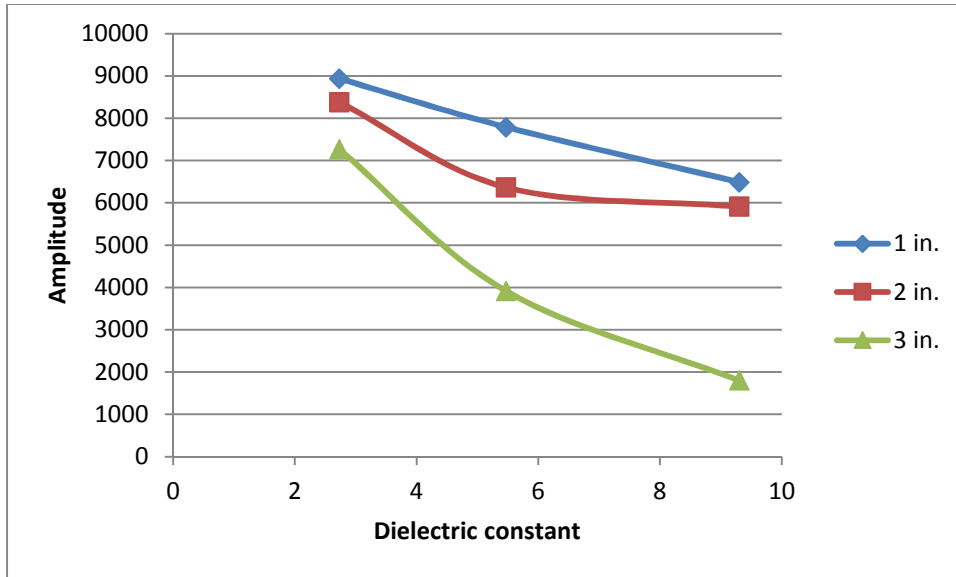


Figure 5-11 Amplitude vs dielectric constant for #3 (10 mm) rebar

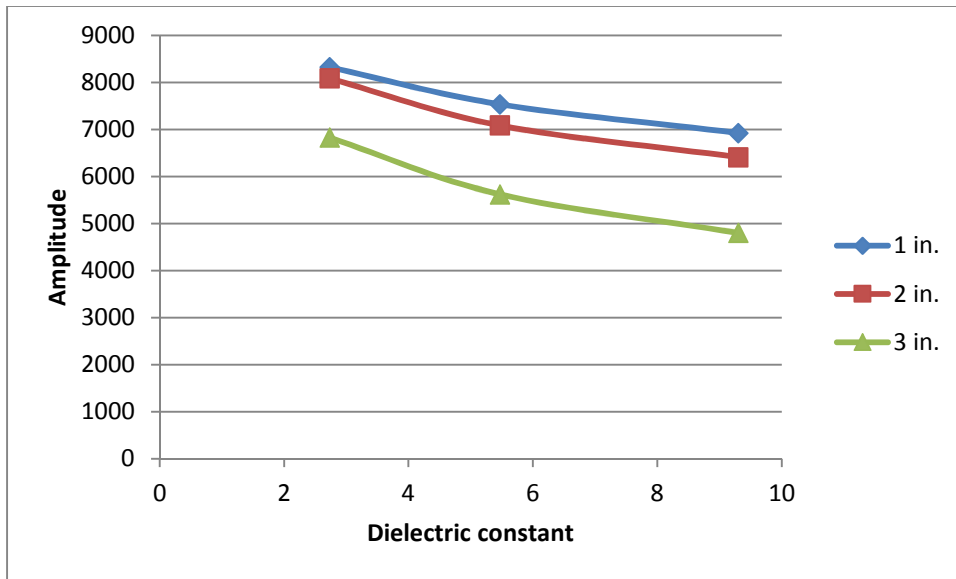


Figure 5-12 Amplitude vs dielectric constant for #4 (12 mm) rebar



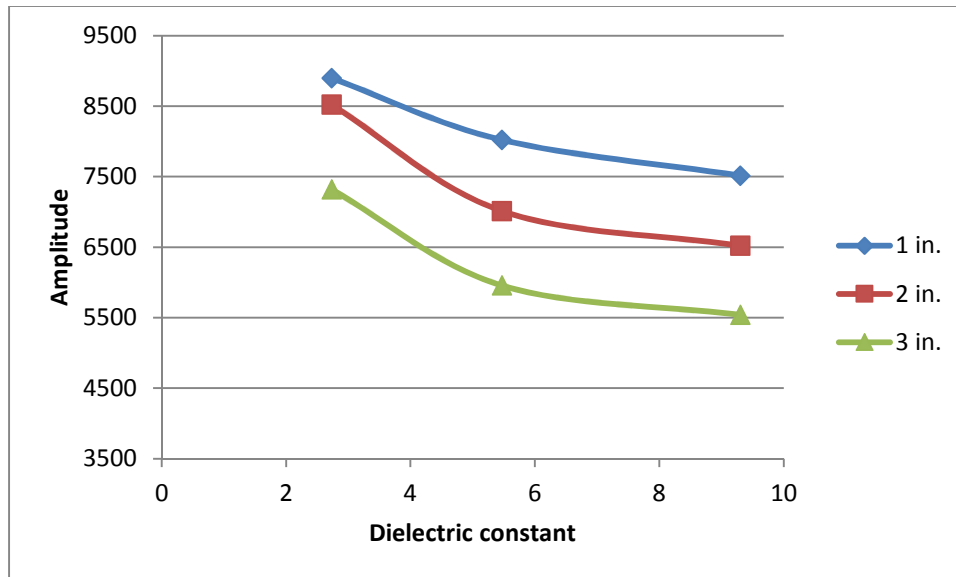


Figure 5-13 Amplitude vs dielectric constant for #5 (16 mm) rebar

#### 5.5 Accelerated corrosion test

In electrochemical corrosion process of steel rebar in concrete, the iron from the rebar is converted to iron oxides or rusts. These iron oxides accumulate around the rebar and the effective core of the rebar gets thinner as the corrosion process continues. The corrosion agent such as chlorides and corrosion products contaminates the concrete in the vicinity of the rebar. This contamination increases the dielectric constant of concrete. During the GPR scanning of a corroded rebar, the GPR electromagnetic wave travels through the concrete towards the rebar. But the RADAR wave has to penetrate through the corrosion product to hit the surface of the non-corroded core of the rebar. The dielectric property of Iron oxide is very different than that of steel. Steel is a very good conductor and almost totally reflects the incident GPR wave. The GPR wave cannot penetrate through steel. The dielectric constant of steel can be assumed to be infinity. The power of reflection wave from the interface of two different materials depends on the contrast of the dielectric constants of the two medium. If the contrast is high, majority of

the incident wave get reflected and a small part of the wave go through the interface. IF the dielectric contrast is low, a small part of the incident wave gets reflected and the majority of the incident wave travels through the interface into the second medium. The dielectric constant of Iron Oxide is 14 which is very close to the dielectric constant of concrete. This close difference of dielectric constant between the steel and concrete indicates that radar wave does not totally reflect from the surface of Iron Oxide. Rather it penetrates through the Iron Oxides (corrosion product) and eventually get reflected from the surface of non-corroded core of the rebar. Therefore It can be concluded that GPR wave can travel through the corrosion products. The changed environment in the vicinity of a corroded rebar can be monitored using GPR. In this phase of the research, the change in GPR responses with respect to the amount of corrosion was studied.

The schematic diagram of GPR scanning of a corroded rebar in concrete is shown in Fig. 5.14. The dielectric constant of the space between the GPR antenna and the non-corroded core of the rebar increases due to the contamination of the concrete by external corrosion agents and the internal development of corrosion products. The thinning of rebar and the increase of the dielectric constant of the concrete are the two major factors that can differentiate the GPR response form a corroded rebar from that of a non-corroded rebar. It was expected that the increase of dielectric constant and decrease of size of the rebar would result in a decrease in the maximum amplitude form the rebar.

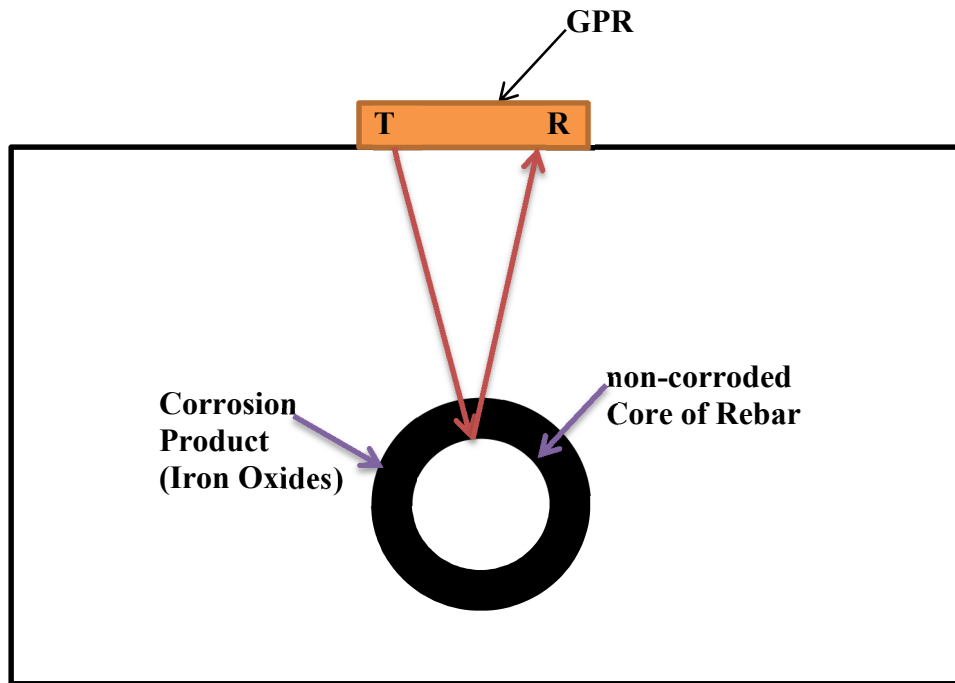


Figure 5-14 Schematic diagram of GPR scanning of corroded rebar

#### 5.6 Corrosion Tank

A corrosion tank was prepared to perform the accelerated corrosion of three #5 dia (16 mm) rebars. The tank was filled with 5% sodium chloride solution. Regular table salt was used for sodium chloride and tap water was used to prepare the solution. The #5 (16 mm) rebars were submerged into the solution to act as anode of an electrochemical cell. Some extra rebar were also submerged in the salt water solution to act as a cathode. A switch board was used to give electrical connections to the cathode. The switches of the switch board were in a parallel connection. The three #5 (16 mm) rebars were connected in series. The series connection ensured that the first of the three rebar will attract more electrical current which created the most amount of electrochemical reaction in the first rebar. The other two rebars, as they were connected in series connection, were having less electrical current resulting in less amount of corrosion. That

was how difference in amount of corrosion in the three different rebars was ensured. A DC current source was used to supply electrical current to the electrochemical cell through anodes and the cathodes. The positive end from the DC source was connected to the anode which is the three #5 (16 mm) rebars that were connected in series. The negative end of the DC power source was connected with the cathode rebars through the switch boards. A 12 Volt potential difference was created between the anode and the cathode rebars using the DC power source. The experimental setup of the accelerated corrosion of the rebars in salt water is shown in Fig. 5.15. The corrosion products are seen floating on the salt water solution. The cathode rebars were connected with 10 K $\Omega$  resistors to protect the circuit. The DC power source and the resistors are shown in Fig 5.16.



Figure 5-15 Corrosion tank for accelerated corrosion

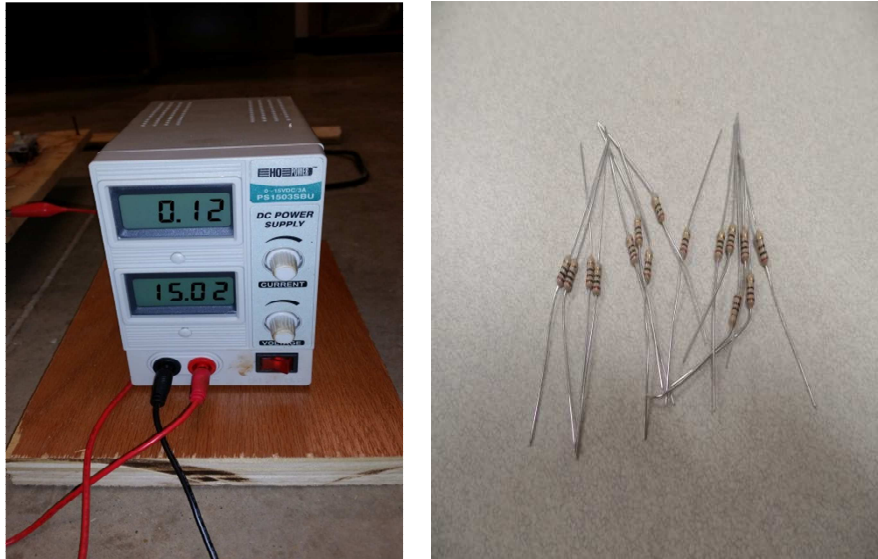


Figure 5-16 DC power source and 10 KΩ resistor

The corrosion process was run for a week. After one week the current flow was stopped and the anode rebars were taken out of the corrosion tank. They were thoroughly cleaned. Figure 5.17 shows the three #5 (16 mm) rebars with a non-corroded rebar on the left side for comparison. It was obvious that the three #5 (16 mm) rebars were corroded in different amount due to the difference in amount of current flow among the rebars.



Figure 5-17 Three corroded rebars with a non-corroded rebar on the left

#### 5.7 Collected Data from the corroded rebars

The corroded rebar were weighed to determine amount the weight loss due to corrosion. The length of the rebars was 12 in. (30.48 cm). Some parts of the rebars were outside of the solution tank and didn't have any corrosion. That part of the rebar was excluded in the calculation of loss of mass. It was assumed that the loss of mass from the rebar was happened uniformly along the length of the rebar. In Table 5.5, the loss of mass was converted to loss of area.

Table 5-5 Amount of mass loss in #5 (16 mm) rebars

Rebar	Initial Mass (g)	Mass after corrosion (g)	Loss (g)	Length of Corroded part of 12 in. long rebar (in.)	Avg. Area Loss %
Rebar-1	472	472	0	0	0
Rebar-2	472	394	78	7	22
Rebar-3	472	363	109	6	31
Reabr-4	472	310	162	6	45

After weighing the rebars, each of them were taken to the oil emulsion tanks as shown in Fig. 4.18. The data collection parameters were similar to as listed in Table 5.3. Each rebar was placed in the emulsion tanks. The placement of the corroded rebar in an emulsion tank was assumed to be similar to a real corroded rebar embedded in concrete. The GPR scanning was performed on each of the corroded rebar as shown in Fig. 5.19. The B-Scans or radargrams for each rebar were recorded for different tanks and different depth at each tank. For each rebar, 9 sets of data were collected. A total of 27 sets of scanning were performed on the corroded rebars. Data were also taken for the non-corroded rebar to compare with the corroded rebars. The GPR B-Scans were taken into RADAN to post-process the data.



Figure 5-18 Oil emulsion tanks for corroded rebar



Figure 5-19 GPR Data collection from the corroded rebar in oil emulsion tank



Background removal function was applied to all the data. The maximum amplitude and the corresponding two way travel times were recorded for each of the scans. The collected data are presented in Table 5.6. According to Table 5.5, Rebar-1 was without any corrosion and the amount of corrosion gradually increased from Rebar-2 to Rebar-4.

Table 5-6 Processed data of the corroded rebars in corrosion tanks

Rebar-1					Rebar-2				
	Scan	TWTT(nS)	Amplitude	Depth(in)		Scan	TWTT(nS)	Amplitude	Depth (in)
Tank-1	71	0.36	17861	1	Tank-1	2267	0.39	13363	1
	460	0.64	11194	2		2681	0.64	8514	2
	871	0.89	7252	3		3095	0.89	5642	3
Tank-2	1153	0.45	13343	1	Tank-2	1159	0.54	8570	1
	1543	0.76	7424	2		1560	0.86	4845	2
	1944	1.08	3153	3		1960	1.14	2560	3
Tank-3	2211	0.57	9326	1	Tank-3	92	0.64	7728	1
	2558	0.98	4960	2		504	1.04	3990	2
	2945	1.42	3506	3		925	1.42	2317	3
Rebar-3					Rebar-4				
	Scan	TWTT(nS)	Amplitude	Depth(in)		Scan	TWTT(nS)	Amplitude	Depth(in)
Tank-1	93	0.42	13215	1	Tank-1	2263	0.43	10696	1
	518	0.67	8130	2		2696	0.67	6922	2
	899	0.92	5583	3		3116	0.93	4716	3
Tank-2	1131	0.54	7662	1	Tank-2	1192	0.51	7586	1
	1500	0.86	4955	2		1580	0.82	4347	2
	1849	1.11	2665	3		1971	1.17	1685	3
Tank-3	2119	0.7	6654	1	Tank-3	98	0.73	5972	1
	2520	1.08	3848	2		508	1.11	3263	2
	2930	1.48	2028	3		901	1.48	1503	3

### 5.8 Effect of corrosion on GPR responses

Two GPR parameters were chosen to relate with the amount of corrosion. They are: two way travel time (TWTT) from the rebar and the maximum positive reflective amplitude from the rebar.

Two way travel times of the rebars were plotted against the depth of rebar in the corrosion tank. Figure 5.20 shows the plot of TWTT vs cover depth for tank-1. It was observed that the TWTT was increasing with the increase of corrosion. The increase of TWTT with the increase of corrosion was observed for all three cover depths. Tank-2 and tank-3 showed similar results as shown in Fig. 5.21 and Fig. 5.22.

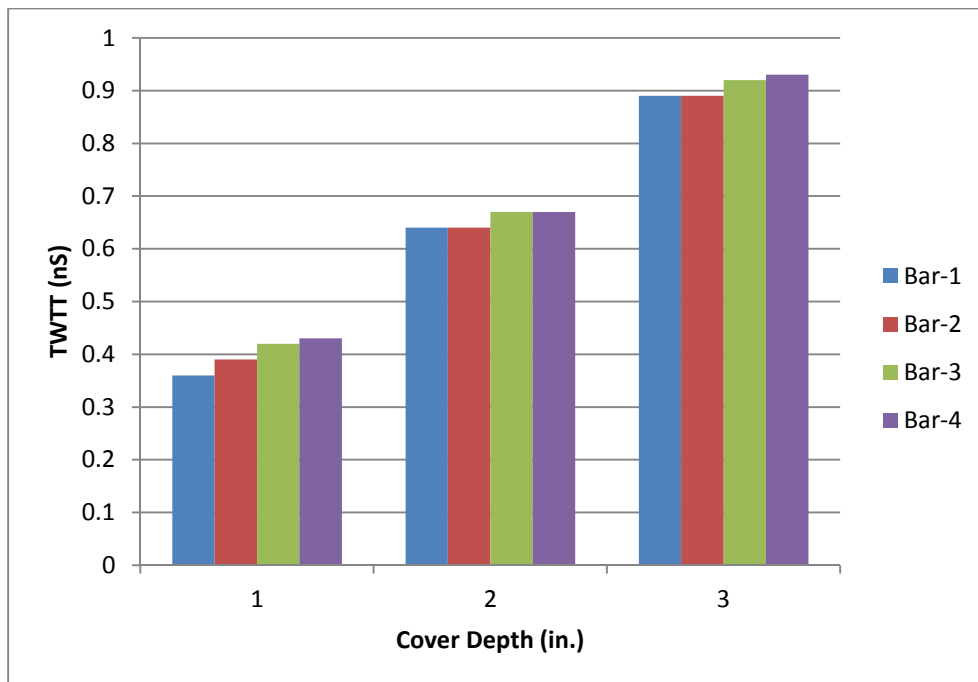


Figure 5-20 TWTT vs cover depth for different corroded rebar in tank-1( $\epsilon=2.73$ )

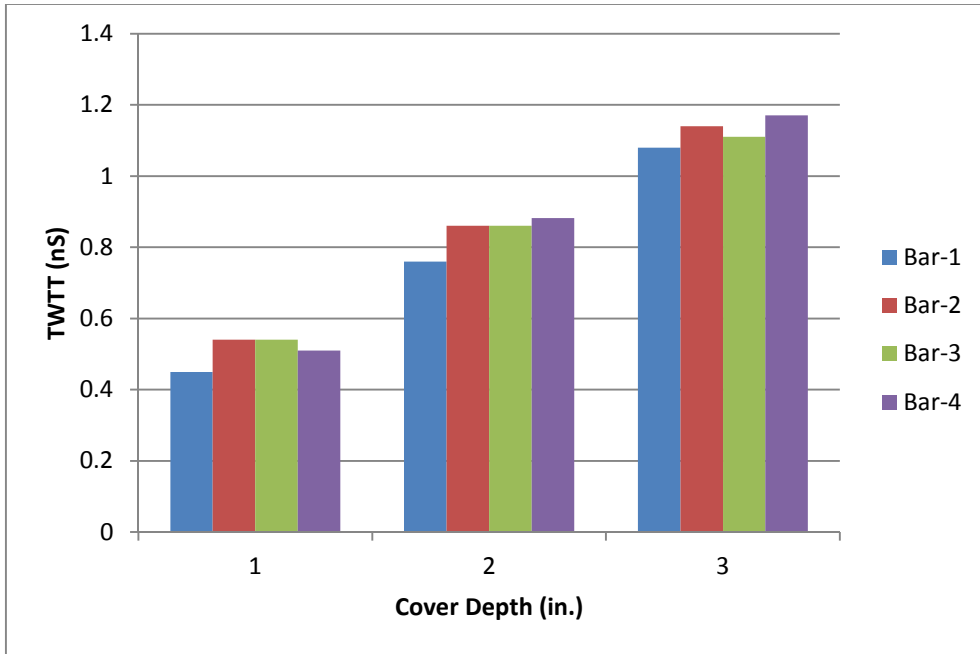


Figure 5-21 TWTT vs cover depth for different corroded rebar in tank-2 ( $\epsilon=5.47$ )

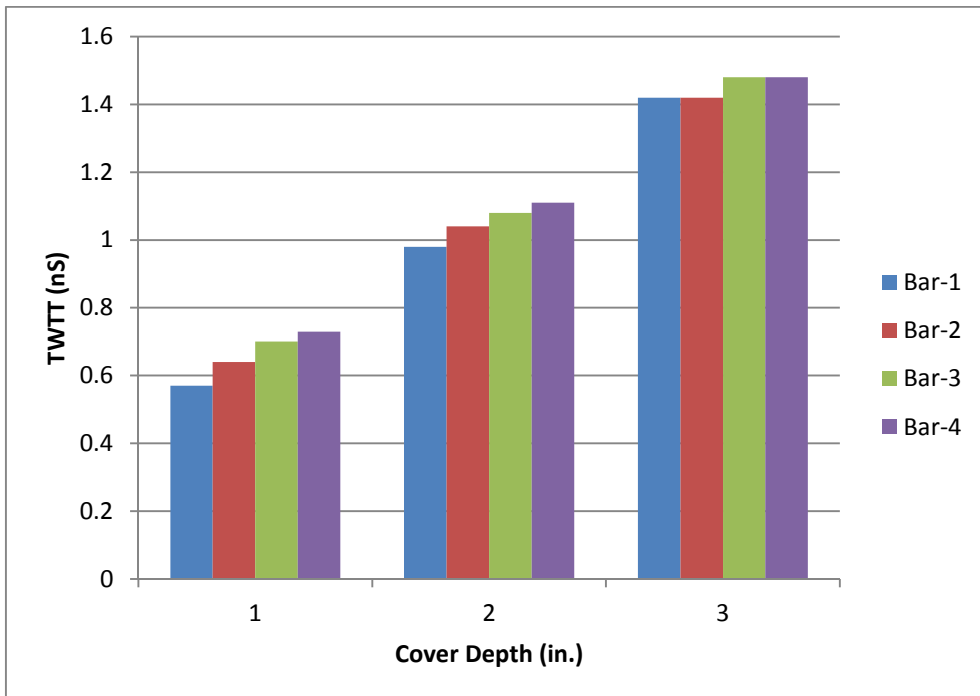


Figure 5-22 TWTT vs cover depth for different corroded rebar in tank-3 ( $\epsilon=9.3$ )

The maximum positive reflection amplitudes of the rebars were plotted against the depth of rebar for each of the corrosion tank. Figure 5.23 shows the plot of maximum amplitude vs cover depth for tank-1. It is observed that the maximum amplitude was decreasing with the increase of corrosion. The decrease of maximum amplitude with the increase of corrosion was observed for all three cover depths. Tank-2 and tank-3 showed similar results as shown in Fig. 5.24 and Fig. 5.25.

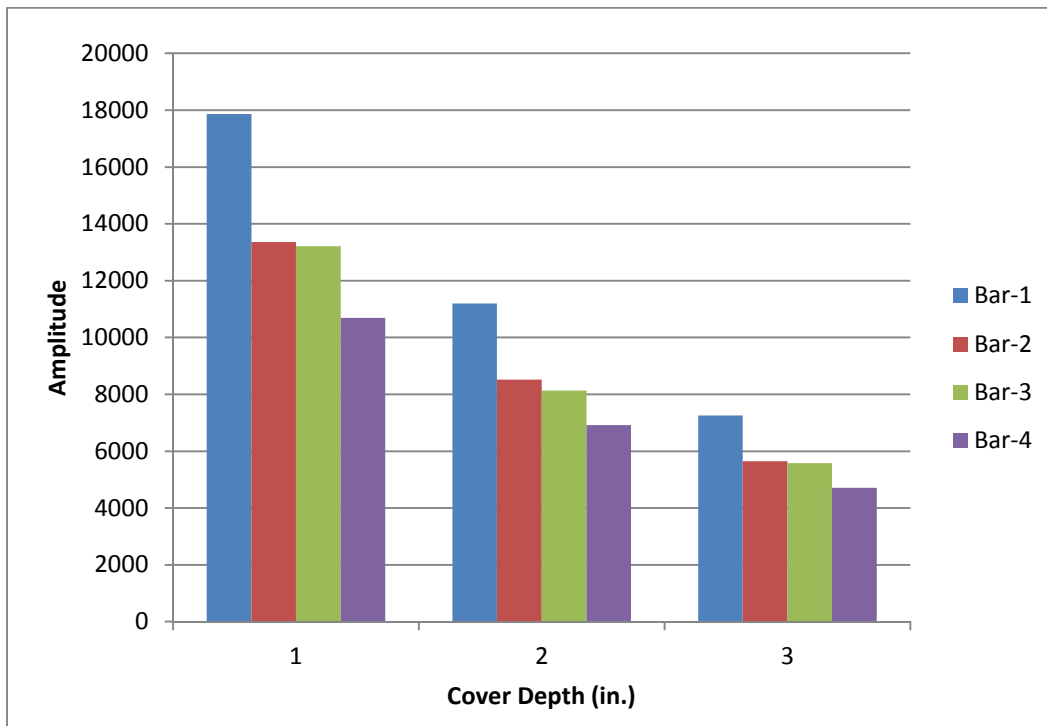


Figure 5-23 Maximum amplitude vs cover depth for different corroded rebar in tank-1 ( $\epsilon=2.73$ )

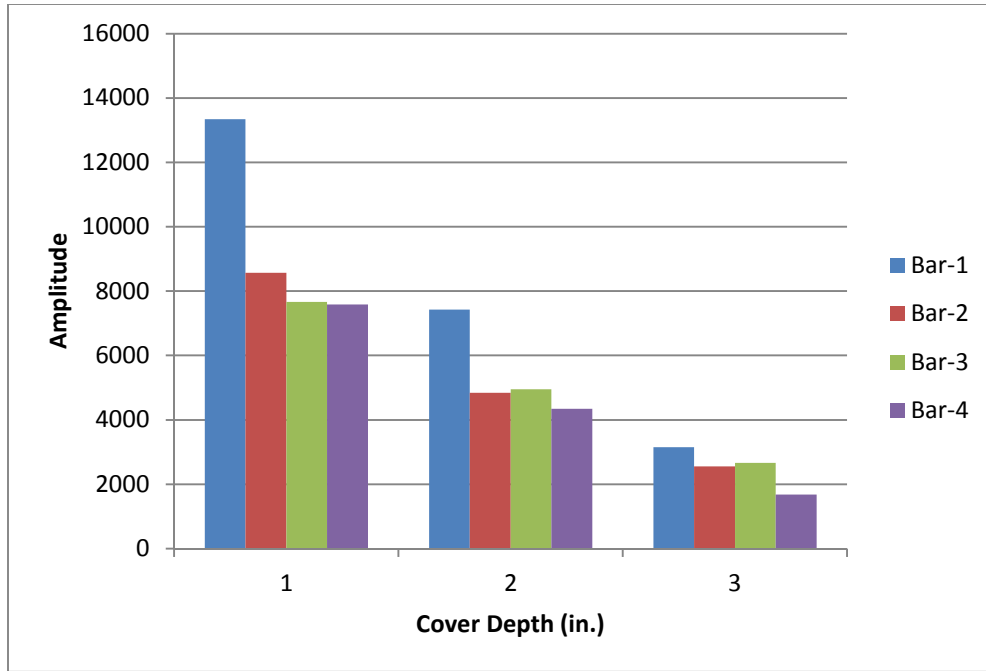


Figure 5-24 Maximum amplitude vs cover depth for different corroded rebar in tank-2 ( $\epsilon=5.47$ )

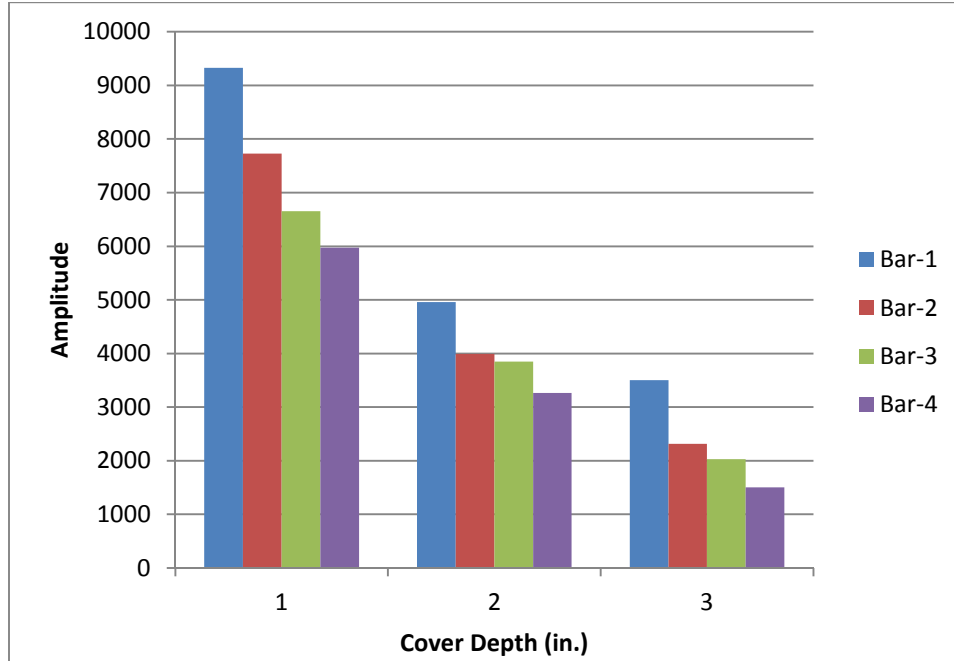


Figure 5-25 Maximum amplitude vs cover depth for different corroded rebar in tank-3 ( $\epsilon=9.3$ )

### 5.9 Relationship between amount of corrosion and GPR responses

In Fig. 5.26, the maximum amplitudes for the rebars with different corrosion level were plotted against corresponding percentage area loss. For each magnitude of the cover depths, the maximum amplitude vs percentage corrosion values were plotted. The points of maximum amplitudes for a particular cover depth were then connected using linear regression. For 1 in. (25 mm) cover, the correlation coefficient is 0.965 which is very close to 1. This high value of correlation coefficient indicates that the linear relationship between the maximum amplitude and the amount of corrosion was valid. The correlation coefficient for 2 in. (50 mm) and 3 in. (75 mm) cover depths are 0.975 and 0.964 respectively. Therefore, the relationship between maximum amplitude and the amount of corrosion is linear irrespective of the cover depth ranging from 1 in. (25 mm) to 3 in. (75 mm). Though the relationship between the maximum amplitude and the amount of corrosion was linear, the rate of changes in maximum amplitudes for a particular amount of corrosion was not the same. This is evident from the different slopes of the equations of regression lines in Fig. 5.26. The slope of the line at 1 in. (25 mm) cover is -155.13. The slope of the line at 2 in. (50 mm) and 3 in. (75 mm) concrete cover is -94.28 and -55.02. Therefore, the rate of change in the maximum amplitude for a particular amount of corrosion is highest at 1 in. (25 mm) cover and lowest in 3 in. (75 mm) concrete cover. At concrete cover depth of 1 in. (25 mm), 10% loss of area resulted in 8.82% decrease in maximum amplitude. The decrease in amplitude for 10% loss of area at 2 in. (50 mm) and 3 in. (75 mm) cover depths are 8.57% and 7.69% respectively.

Similar plots were developed for tank-2 and tank-3 as shown in Fig. 5.27 and Fig. 5.28. The dielectric constant of the medium of Fig. 5.27 is 5.47. The linear regression correlation coefficients in Fig. 5.27 are 0.85, 0.86 and 0.84 which was acceptable. The slopes of the regression line are decreasing with cover depth from 1 in. (25 mm) to 3 in.

(75 mm). For 10% loss of area at 1 in. (25 mm), the maximum amplitude decreased by 10.64%. The change in amplitude for 10% loss of area at 2 in. (50 mm) and 3 in. (75 mm) are 9.63% and 9.16%. The dielectric constant of the medium is 9.3 at Fig. 5.28 In Fig. 5.28, correlation coefficient of the linear regression lines at 1 in. (25 mm), 2 in. (50 mm) and 3 in. (75 mm) concrete cover are 0.984, 0.986 and 0.986 respectively. This high value of correlation coefficient confirms that the relation between the maximum amplitudes and the loss of area is linear. The slope of the regression line at 1 in. (25 mm) depth is highest. The change of maximum amplitudes for 10% loss of area at 1 in. (25 mm), 2 in. (50 mm) and 3 in. (75 mm) cover depths are 8.26%, 7.52% and 12.99% respectively.

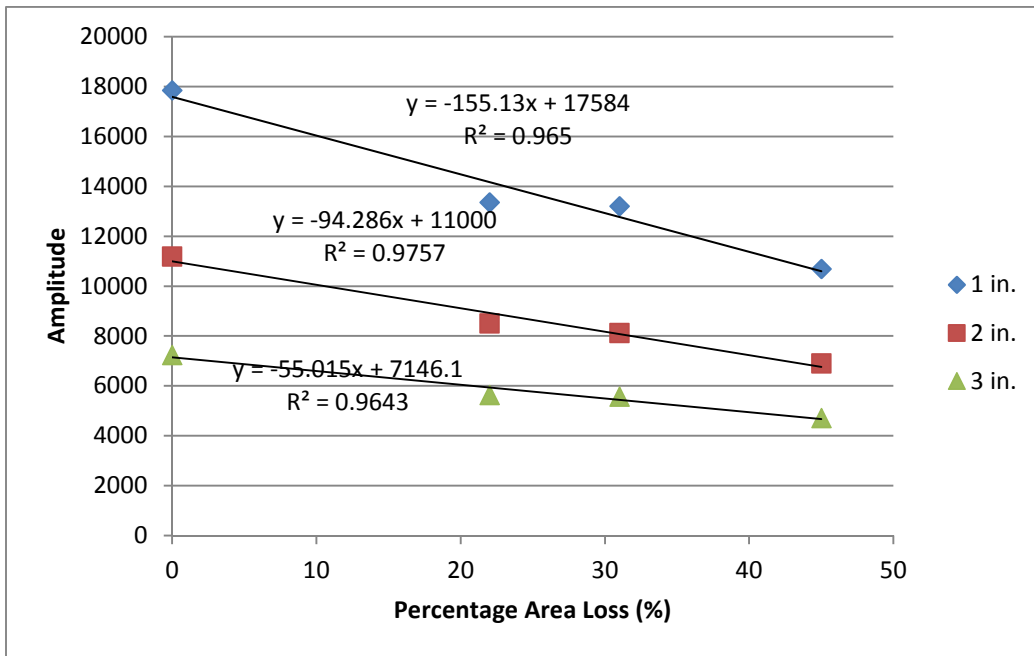


Figure 5-26 Maximum amplitude vs percentage area loss in tank-1 ( $\epsilon = 2.73$ )

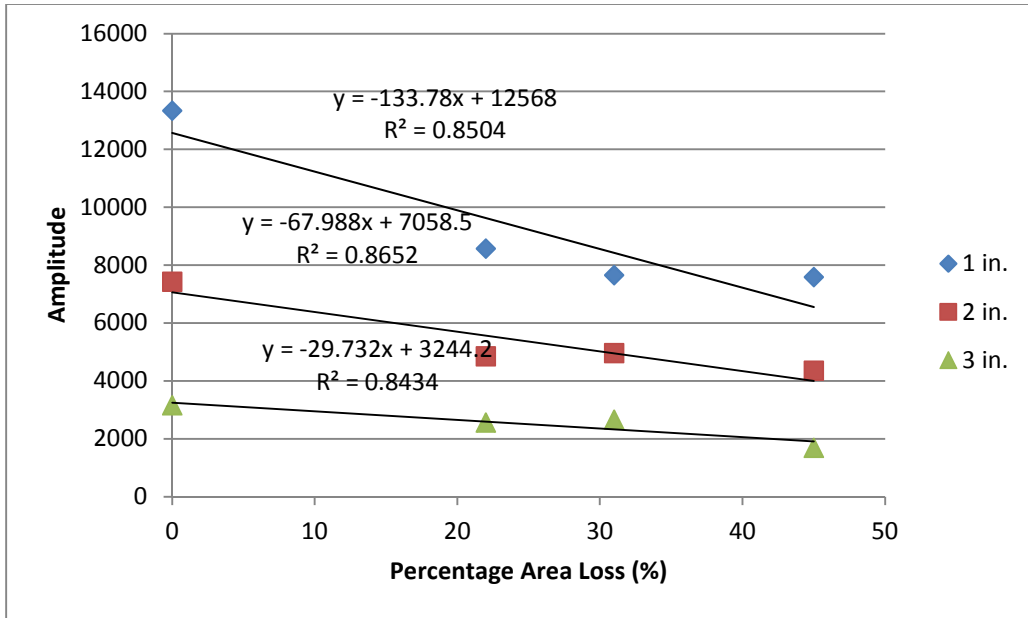


Figure 5-27 Maximum amplitude vs percentage area loss in tank-2 ( $\epsilon = 5.47$ )

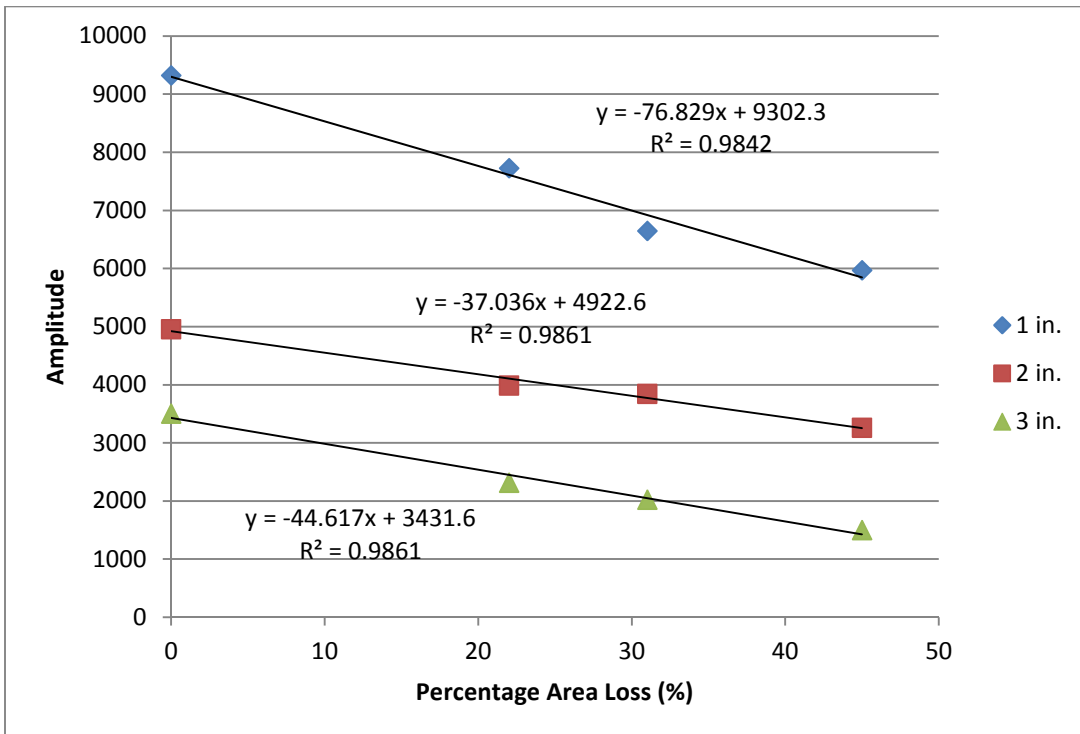


Figure 5-28 Maximum amplitude vs percentage area loss in tank-3 ( $\epsilon = 9.3$ )



#### 5.10 Proposed method to estimate the amount of corrosion

Figure 5.26 to 5.28 are very important relationship between GPR maximum amplitude and the amount of corrosion of the rebar. This relationship can be used to predict the existing amount of corrosion in a damaged structure with the help of GPR scan. The following steps are recommended to estimate the amount of corrosion:

Step-1: Finding the in-situ dielectric constant of the concrete by investigative drilling along with GPR scanning. The TWTT and the depth from drilling will provide the in situ dielectric constant of the concrete.

Step-2: Finding the diameter of the rebar from as built drawing or ferro-scanner. The regression equations of corrosion are given for particular diameter of rebar. This is why knowing the diameter of the rebar is necessary to select the appropriate equation.

Step-3: Performing GPR scan on the concrete and determine the cover depth of concrete and the maximum amplitude from the processed data.

Step-4: Estimating the amount of corrosion for pre-established linear regression equation. Table 5.7 shows the linear regression equations for #5 (16 mm) rebar. Linear interpolation can be applied between two cover depths and two dielectric constants in Table 5.7.

The inputs for estimating the amount of corrosion are:

1. Concrete Cover Depth of the rebar
2. Dielectric Constant of the rebar
3. The variable 'y' in the regression equation which denotes the maximum amplitude from the rebar.

The output of estimating the amount of corrosion is the variable 'x' which means the percentage of mass loss from the rebar.

Table 5-7 Equations for estimation of corrosion from GPR maximum amplitudes for #5 (16 mm) rebar

Dielectric Constant	Cover Depth (in.)	Regression Equations
$\epsilon = 2.73$	1	$y = -155.13x + 17584$
	2	$y = -94.286x + 11000$
	3	$y = -55.015x + 7146.1$
$\epsilon = 5.47$	1	$y = -133.78x + 12568$
	2	$y = -67.988x + 7058.5$
	3	$y = -29.732x + 3244.2$
$\epsilon = 9.3$	1	$y = -76.829x + 9302.3$
	2	$y = -37.036x + 4922.6$
	3	$y = -44.617x + 3431.6$

#### 5.11 Monitoring accelerated corrosion process in a real concrete beam

In section 4.10, a method to estimate the amount of corrosion using GPR was proposed. The corrosion was performed in a salt water solution under an accelerated condition. The rebars were taken into an oil emulsion tank instead of real concrete. In this section a real concrete beam was used to perform the accelerated corrosion and the results will be compared to validate the results obtained in section 4.9.

A concrete beam was cast. The length of the beam was 30 in. (76.2 cm). The width was 9 in. (22.9 cm) and the depth was 6.5 in. (16.5 cm). Four #5 (16 mm) rebars were cast in the concrete beam at 1.5 in. (37.5 mm) depth. The beam was placed in a 100% humidity chamber for 28 days in order to cure the concrete. After 28 days, the beam was taken out of the humidity chamber and the forms were taken out. The rebars

were placed in the beam in such a way that some part of the rebar would extend out of the concrete. This was done intentionally to facilitate electrical connection to the rebar. The beam was placed in a 5% sodium chloride solution as shown in Fig. 5.29.



Figure 5-29 Concrete beam with four #5 (16 mm) rebar in 5% salt water solution

The beam was fully submerged into sodium chloride solution for 3 days. After 3 days, the level of water was lowered just below the rebar. An accelerated corrosion scheme was developed. Out of the 4 rebars in the beam, the middle two rebars were used as anode and the rebars at the corners were used as cathode. As the middle two rebar were anode, corrosion occurred in these two rebars. A 15 V DC current was passed through the anode and the cathode. The positive end of the power source was connected with the middle two rebars that were acting as anode. The negative end of the power source was connected to the cathode through the switch board as discussed in section 4.8. The experimental set-up for the accelerated corrosion is shown in Fig. 5.30.

After the corrosion started, GPR scanning of the concrete beam was performed every 24 hours for 25 days continuously. Figure 5.31 shows the GPR scanning of the beam using the GSSI 2600 MHz antenna. A typical B-Scan that was recorded on daily

basis is shown in Fig. 5.31. The four rebars were seen as hyperbolic signature in the radargram.



Figure 5-30 Experimental set-up of accelerated corrosion

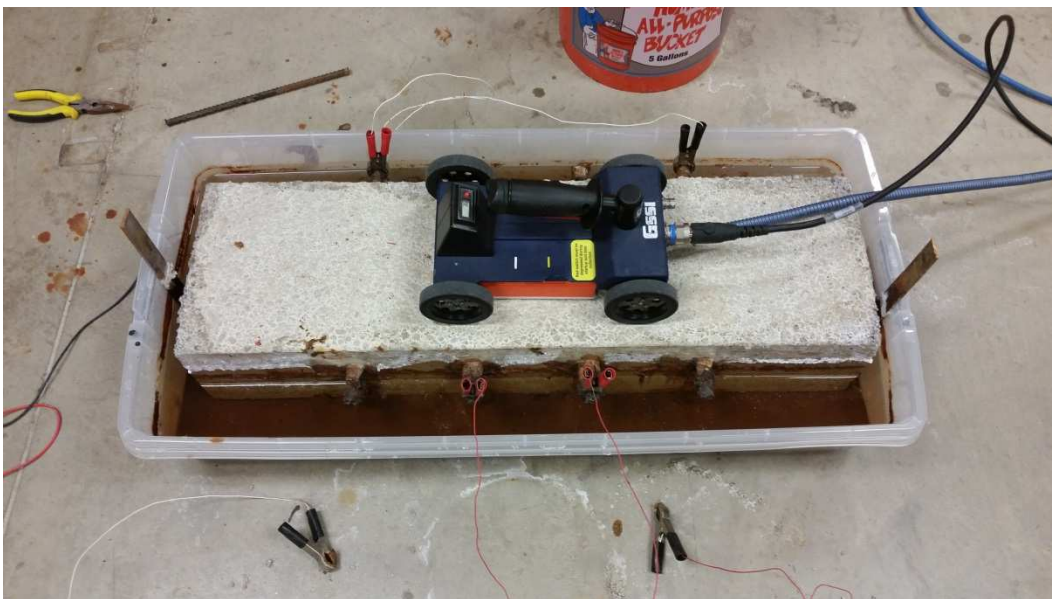


Figure 5-31 Daily data collection to monitor corrosion

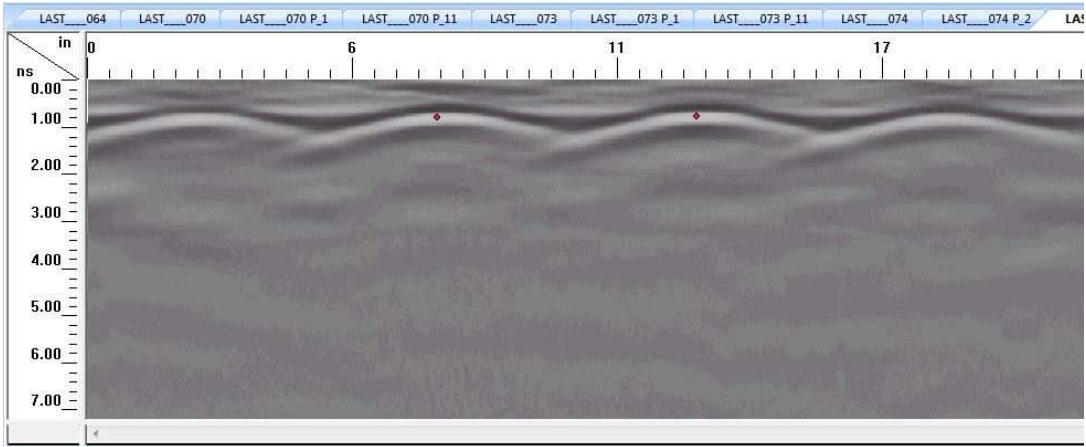


Figure 5-32 Typical GPR Scan of the sample beam

#### 5.12 Results of accelerated corrosion in a real concrete beam

The corrosion products were accumulating around the rebars. The concrete was also getting damaged and its color was changed with time possibly due to chloride ion ingress. The corroded state of the rebars at the end of 30 days is shown in Fig. 5.33.



Figure 5-33 The corroded state of the two rebars in the middle after 30 days

The maximum amplitudes from the two anode rebars were recorded every day for 25 days. Figures 5.34 and Fig 5.35 show the maximum amplitude vs time plot for the two rebars. It was observed that the maximum amplitude decreased with the increase in time. It indicated that the amplitude decreased with the increase of corrosion. The correlation coefficient ( $R^2$ ) of the linear regression curve for rebar-1 is 0.87 and the rebar-2 is 0.90. This high magnitude of correlation coefficient confirms that the change in amplitude with corrosion is linear. This behavior supports the results developed in section 4.8.

The TWTT increased from 0.78 nanoseconds in day one to 0.98 nanoseconds on day 25. This indicated that the dielectric constant of the concrete increased from 9.72 to 14.96. Therefore 52% increase in dielectric constant decreased the maximum amplitude by 20%. The corrosion in the rebar was not uniform along the length. The majority of the corrosion happened at the outer side of the rebar. This change in dielectric constant can be attributed to salt water ingress in concrete and the dissemination of corrosion products from the rebar to the surrounding concrete matrix through pores and cracks.

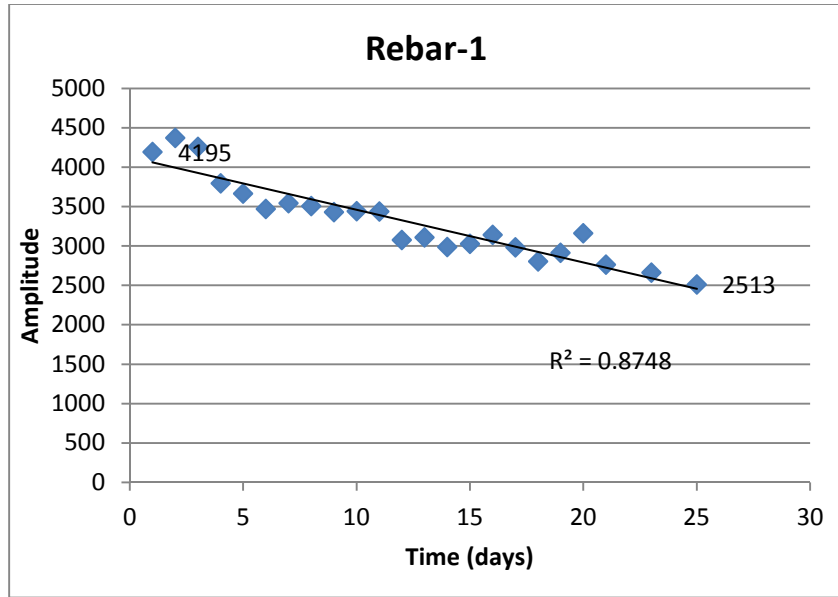


Figure 5-34 Maximum amplitude vs time for rebar-1

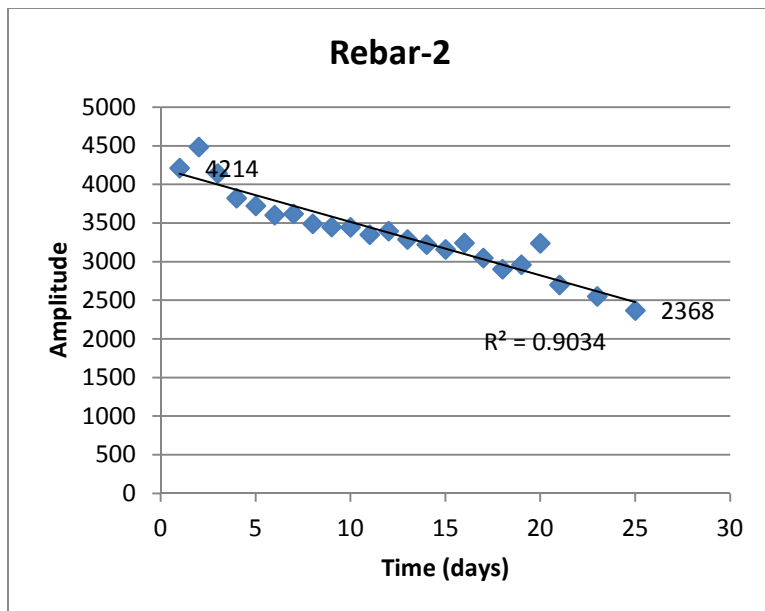


Figure 5-35 Maximum amplitude vs time for rebar-2

### 5.13 Discussion

In this chapter, a novel method to simulate long term corrosion in laboratory was discussed. Oil emulsion tank was used as a substitute of concrete specimen. The performance of oil emulsion tanks as a substitute of concrete beam specimen was verified from the GPR scans. The performance of the oil tank under different diameter of the rebar and at different concrete depth was similar to real concrete beam. The dielectric property of the tank was varied by controlling the amount of water in the emulsion. Three oil water emulsion tanks were prepared with dielectric constants of 2.73, 5.47 and 9.3. These tanks were used to observe the effect of dielectric constant on GPR response.

Accelerated corrosion of the rebar was performed in a 5% NaCl solution using electrochemical method. The rebars were corroded at different corrosion level ranging from 0% to 45%. The corroded rebars were placed in the oil emulsion tanks and GPR scan was performed.

It was observed that the maximum amplitudes from the rebar decreased with the increase of the amount of corrosion. Linear regression models were developed to correlate between the maximum amplitudes and the percentage loss of area or corrosion. The linear regression models were developed for three different dielectric constants (2.73, 5.47 and 9.3) and three different concrete cover depths [1 in. (25 mm), 2 in. (50 mm) and 3 in. (75 mm)].

For dielectric constant of 2.73 and at concrete cover depth of 1 in. (25 mm), 10% loss of area resulted in 8.82% decrease in maximum amplitude. The decrease in amplitude for 10% loss of area at 2 in. (50 mm) and 3 in. (75 mm) cover depths are 8.57% and 7.69% respectively. For dielectric constant of 5.47 and for 10% loss of area at 1 in. (25 mm), the maximum amplitude decreased by 10.64%. The change in amplitude



for 10% loss of area at 2 in. (50 mm) and 3 in. (75 mm) are 9.63% and 9.16%. For dielectric constant of 9.3, the change of maximum amplitudes for 10% loss of area at 1 in. (25 mm), 2 in. (50 mm) and 3 in. (75 mm) cover depths are 8.26%, 7.52% and 12.99% respectively.

Based on the regression model developed in this study, a method was proposed to determine the amount of corrosion in the field. By using the cover depth, dielectric constant and the maximum GPR amplitude as input, the quantitative amount of corrosion can be calculated using the regression equations.

The behavior of the simulated corrosion experiment was studied by performing another accelerated corrosion experiment using a real concrete beam. GPR maximum amplitudes were collected for 25 days. It was observed that the maximum amplitude decreased with time. Fifty two percent increase in dielectric constant decreased the maximum amplitude by 20%.

## Chapter 6

### Numerical modeling

#### 6.1 Introduction

GPR numerical modeling is very useful to develop understanding of the buried object before actual scan is performed. The main purpose in GPR numerical modeling is to solve the Maxwell's electromagnetic equations. The Finite Difference Time Domain (FDTD) method is one of the popular methods in solving the Maxwell's equation (Giannopoulos, 1997, 2005; Taflov, A (1995); Kunz, K.S. (1993) & Yee, K.S. (1966). The software package used in this study is called GPRMAX (Giannopoulos, 2005). This software package uses the FDTD method to simulate the GPR Scan. This software is open source and available free of cost for research purposes. The experimental data presented in chapter 3 are from complex and heterogeneous material of concrete. The GPR responses can be affected due to this heterogeneity of concrete. In order to understand the GPR responses in a simplistic manner, numerical modeling was performed for the rebar in concrete where the properties of concrete were homogenous and isotropic.

#### 6.2 Basic concepts of GPR modeling

Any electromagnetic wave such as the RADAR wave can be expressed by the Maxwell equations. These equations are differential equations that describe the relationship between electrical and magnetic field quantities and their variation with respect to the distance from the source of the electromagnetic wave. The equations are presented in Eq. 6.1 to Eq. 6.4:

$$\nabla \times E = -\frac{\partial B}{\partial t} \quad (6.1)$$

$$\nabla \times H = -\frac{\partial D}{\partial t} + J_c + J_s \quad (6.2)$$

$$\nabla \cdot H = 0 \quad (6.3)$$

$$\nabla \cdot D = q_v \quad (6.4)$$

where,

E = electric field,

B = magnetic field,

J = current density,

t = time ,

$q_v$  = electric charge density,

D = displacement field, and

H = magnetizing field.

In order to simulate the GPR responses of a rebar embedded in concrete, the above numerical equations need to be solved. The geometry of the medium and the boundary conditions are also required for solution. The nature of the problem of the above differential equations is initial value- open boundary problem (Giannopoulos, 2005). In order to perform the solution, an excitation function of the GPR antenna has to be defined. The excitation function will define the initial condition. The resulting electromagnetic field has to be continued until it reaches a value of zero. So there is no specific boundary that limits the geometry of the problem. There is no known value of electromagnetic field at any distance from the source. So this is a challenge perform the solution within a finite space.

GPRMAX uses the finite difference time domain (FDTD) approach to solve the Maxwell equations. This method discretizes the space and time. The space is discretized spatially into elements having finite dimensions of  $\Delta x$ ,  $\Delta y$  and  $\Delta z$  and the time is discretized into finite  $\Delta t$  time units. The smaller are the spatial and temporal units; the closer is the FDTD solution to the real solution. The FDTD approach reduces the problem into a finite space and finite time window. The discretized elements are modeled according to Kane Yee who introduces this method. The element that is used to mesh the geometry of the model is called Yee cell (Yee, 1966) as show in Fig. 6.1.

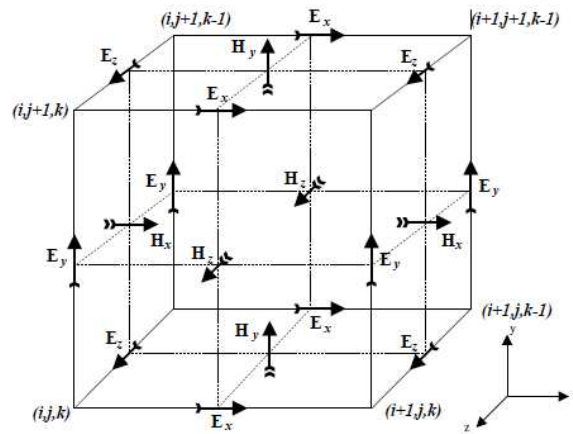


Figure 6-1 Yee cell used in FDTD method (Giannopoulos, 2005)

Appropriate constitutive properties are assigned in each of the joints of Yee cell. Complex types of shapes can be included in the model. Any curved shape will be a staircase model as the elements are rectangular. The numerical solution is obtained by using a discretized version of Maxwell equation. As the electromagnetic field advances through each of the FDTD grid, a corresponding time if  $\Delta t$  is assumed to be elapsed. Thus the FDTD solution simulates the electric and magnetic field for a given time window.

The value of  $\Delta x$ ,  $\Delta y$ ,  $\Delta z$  and  $\Delta t$  cannot be assigned independently because the process of FDTD is conditionally stable. The stability of the FDTD method is controlled by the following Eq. 6.5;

$$\Delta t \leq \frac{1}{c \sqrt{\frac{1}{(\Delta x)^2} + \frac{1}{(\Delta y)^2} + \frac{1}{(\Delta z)^2}}} \quad (6.5)$$

Where,  $c$  is the speed of light. It is obvious that  $\Delta t$  is controlled by the value of  $\Delta x$ ,  $\Delta y$  and  $\Delta z$ .

In FDTD method, the concrete is modeled as an electromagnetic half space where the surface of the concrete is the starting line of the half space. The boundary of the concrete beam is taken as fully absorbing boundary condition (ABC). So any electromagnetic wave coming to the boundary is totally absorbed and no reflection take place. This is why while modeling the beam, all the features inside the concrete has to be within the ABC. Figure 6.2 shows how the source and the targets are encased within the ABC in a FDTD forward model.

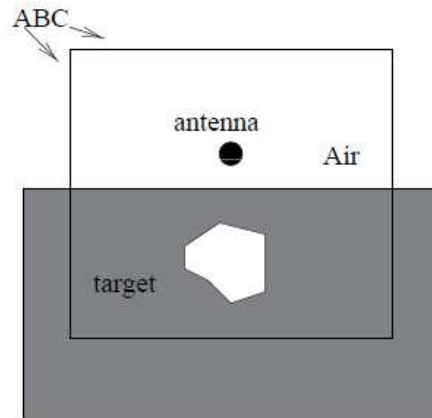


Figure 6-2 GPRMAX model of a half space with ABC (Giannopoulos, 2005)

### 6.3 Assumption of GPR modeling using GPRMAX

The following assumptions are made while doing numerical simulation of GPR using GPRMAX. These assumptions are mainly based on saving computational space.

- The media is linear and isotropic
- The antenna that transmits the radar wave is a line source
- The constitutive properties of the medium (dielectric property, electrical conductivity etc.) do not vary with the frequency of the antenna.

Concrete is not an isotropic material. So modeling of concrete using GPRMAX has limitation on this regard. The antenna is assumed as a line source which is not true for a real antenna. Real antenna transmits a cone shaped beam of electromagnetic wave where the apex of the cone is at the point of transmitting antenna. For constructing the model in 2D, line source is a good assumption.

Choosing the size of mesh in FDTD method can be done by using a rule of thumb (Giannopoulos, 2005). The rule states that the discretization step will be one tenth of the wavelength of the antenna as shown in the following Eq. 6.6;

$$\Delta l = \frac{\lambda}{10} \quad (6.6)$$

So if the frequency of the antenna is 2600 GHz, then the minimum size of the element used in the FDTD model will be at least 12 mm. A free space of at least 15 to 20 cells above the source is needed to ensure the absorbing boundary condition.

### 6.4 Input file commands

In order to build a model, an input file command is required. This file can be in notepad or similar text file format. The input file consists of the commands that are needed to build the geometry of the problem, defining the source antenna, assigning appropriate constitutive properties to the geometry and commands that are needed to run the model

and to get desired types of output. The file then can be run in any windows operating system using the 'run' command. The output is normally as ASCII file format. The main commands to write an input file are discussed in the following sections.

#### 6.4.1 Units

All the units that are used to express a physical dimension in GPRMAX are in meters. The unit of time used in the input file will be in seconds. The frequency of the source antenna will be Hertz. The origin of the coordinate system that defines the geometry of the problem is (0, 0) and it is the lower left corner of the model.

#### 6.4.2 Media and object construction

The medium of the model, i.e. concrete is defined by the following command.

```
# medium: f1 f2 f3 f4 f5 f6 str1
```

- f1 = Dielectric constant or relative permittivity of the medium
- f2 = relative permittivity at infinite frequency
- f3 = relaxation time of the medium
- f4 = DC conductivity of the medium
- f5 = relative permittivity of the medium
- f6 = magnetic conductivity of the medium
- str1 is used to name the medium or as a identifier of the defined medium.

If water is a medium, then by using the electric and magnetic property of water, the GPRMAX media command can be written as:

```
#medium: 82.3 5.5 10.9e-12 0.0 1.0 0.0 water
```

To define a rectangular concrete beam, the #box command is used. The syntax of #box command is written as:

```
#box: f1 f2 f3 f4 str1
```

where f1 and f2 is the lower left coordinates of the medium in meters. Similarly the upper

left of the medium is defined by the coordinate f3 and f4. The command str1 is used here to assign property of the box that is already assigned using a medium command.

Any rebar or cylindrical object can be modeled using the # cylinder command.

The cylinder command is written as:

```
#cylinder: f1 f2 f3 str1
```

where f1 and f2 are the x and y coordinate of the center of the cylinder and f3 is the radius of the cylinder. The command str1 is the medium identifier. If the object is a perfectly conducting metal target like a rebar in concrete then the str1 command is written as 'pec'.

#### 6.4.3 Antenna modeling

The modeling of the antenna can be done by the #line-source command as shown below:

```
#line_source: f1 f2 str1 str2
```

where f1 and f2 are the amplitude in amperes of the line source's current and the frequency in Hertz of the antenna. The parameter str1 indicates the type of excitation function. The command str2 is used to give a user defined name to the excitation function. The excitation function can be of many types which includes sine, Gaussian, ricker or user defined function. The help file of the GPRMAX has the detail of the excitation functions. An example of the excitation function command or antenna command is:

```
#line_source 1.0 600e6 ricker Mysource
```

which specifies that the name of the antenna is Mysource. It has a frequency of 600 MHz and it produces a ricker wavelet with a amplitude of 1. In this study the ricker excitation function is used.

The #tx command is used to define the transmitter of the antenna. It is written as:



```
#tx: f1 f2 str1 f3 f4
```

where f1 and f2 are the x and y coordinates in meters of the transmitter source of the antenna. The str1 command is used to define the type of the source as discussed earlier as ricker wavelet. The command f3 and f4 indicate delay and removal of the source.

The #rx command indicates the receiver of the antenna and it is written as:

```
#rx: f1 f2
```

where f1 and f2 indicates the coordinate of the receiver of the antenna.

#### *6.4.4 Domain and time window*

The command #domain is used to indicate the size of the model in meters. The command is written as:

```
# domain: f1 f2
```

where f1 and f2 are the x and y dimension of the domain in meters. The command #dx\_dy is used to define the size of the mesh of the discretized model. The #dx\_dy command is written as:

```
#dx_dy: f1 f2
```

where f1 and f2 are dimension of the mesh in x and y direction.

The command #time\_window indicates the duration of the simulation. The syntax used to define the time window is:

```
#time_window: f1
```

where f1 is the time of the simulation in seconds. Because of the very high speed of electromagnetic wave, this quantity is normally very small and often falls within the range of nanoseconds.

The command #analysis is used to run the analysis and save the output file. The termination of the simulation is done using the #end\_analysis command. The output

signal from the FDTD simulation is normally a ASCII file. The geometry of the model and the B-Scan of the model can also be produced using the output commands.

#### 6.5 Creating command file and running the model

In this stage of the study, a physical model of a reinforced concrete beam was developed. The dimension of the beam was 0.6 m long and 0.3 m deep. As it was a 2D model, the depth can be infinity. A 16 mm dia (0.625 in.) rebar was embedded in the concrete under a concrete over of 50 mm (2 in.). The steps of building the model input file is described below:

Step-1: The medium was defined with the constitutive parameters.

```
#medium: 7.0 0.0 0.0 0.01 1.0 0.0 concrete
```

Here the medium was defined as concrete with a dielectric constant or relative permittivity of 7.0. Other electrical and magnetic properties were also defined in the command line.

Step-2: The source type was determined. Here our source was a 2600 GHz antenna. The type of the source was selected as ricker wave. Ricker wave is the first derivative of Gaussian waveform. A normalized version of the ricker wave is shown in Fig. 6.3.

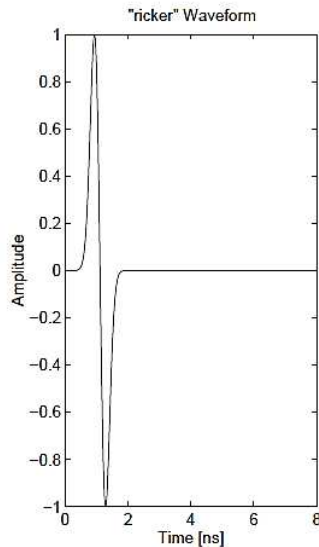


Figure 6-3 Normalized ricker excitation function (Giannopoulos, 2005)

The ricker wavelet is stored in the GPRMAX as a built in function. Choosing the frequency of the antenna is also crucial to indicate the size of the discretized elements as discussed in section 5.2. The minimum size of the element has to be at least one tenth of the minimum wavelength of the excitation function. The frequency that is attributed to a GPR antenna is normally the center frequency of the band of frequencies emanating from the antenna. The maximum frequency from an antenna is normally three times the center frequency. So the maximum frequency of a 2600 MHz antenna will be  $3 \times 2600 = 7800$  MHz. The corresponding wavelength will be 14.5 mm. So each of the element has to be at least 1.45 mm. But in order to smoothen the curved surface of the cylinder, 1 mm was used as the dimension of the discretized element in both x and y direction.

Step-3: The dimensions of the discretized element was

$$\Delta x = \Delta y = 0.001\text{m}$$

Step-4: The discretized time was determined.

$$\Delta t = \frac{0.001}{3e8\sqrt{2}} = 2.36 \text{ ps}$$

The value of  $\Delta t$  was 2.36 picoseconds. Therefore a 6 nanoseconds time window produced 2542 iterations.

Step-5: The domain and the time window command were written.

```
#domain: 0.6 0.3
```

```
#dx_dy: 0.001 0.001
```

```
#time_window: 6.0e-9
```

The concrete box and the cylindrical rebar commands were also written.

```
#box: 0.0 0.0 0.6 0.25 concrete
```

```
#cylinder: 0.3 0.192 0.00695 pec
```

Step-6: The antenna was defined using the appropriate command. The distance between transmitter and receiver were also provided according to GSSI antenna specification. The command to run the input file and to end the analysis was also included.

After finishing up all the input commands, the input file was written on a notepad file. The complete input file for the modeling of a concrete beam with a 16 mm (0.625 in.) rebar embedded in it was composed as:

```
#medium: 7.0 0.0 0.0 0.01 1.0 0.0 concrete
```

-----

```
#domain: 0.6 0.3
```

```
#dx_dy: 0.001 0.001
```

```
#time_window: 6.0e-9
```

```
-----  
#box: 0.0 0.0 0.6 0.25 concrete  
#cylinder: 0.3 0.192 0.00695 pec  
-----  
#line_source: 1.0 2600e6 ricker MyLineSource  
#analysis: 1 rebar.txt a  
#tx: 0.155 0.2525 MyLineSource 0.0 6.0e-9  
#rx: 0.195 0.2525  
#end_analysis:  
#title: Model of rebar in concrete  
#messages: y  
#geometry_file: rebar.geo
```

## 6.6 Output of Simulation

The input file as shown in the previous chapter was run using GPRMAX2D. The output signal was as ASCII file in text format. The geometry of the simulation was stored using .geo file. The simulation was run multiple times horizontally simulating a typical GPR scan. The resulting B-Scan was also saved in the output as .sca file. The output ASCII file is included in Appendix A. MATLAB code were used to plot the geometry of the model from .geo file and the B-Scan of the simulation from the .sca file. The MATLAB code that was used in this study was generated by Bostanudin (2013). The MATLAB codes are given in Appendix B as generated by Bostanudin (2013). The MATLAB file in Appendix B was used in conjunction with the MATLAB file provided with GPRMAX2D software package to generate the geometry and the B-Scan.

Figure 6.4 shows the geometry of the model. The rendition of the model confirmed that the dimensions were correct and the rebar were placed at correct location

in the concrete beam. Figure 6.5 shows the B-Scan of the simulation. It was observed that the B-Scan exactly emulated the typical B-Scan plot as collected by GSSI SIR-30 with a hyperbola as a response from the rebar. The B-Scan confirmed that the model was run correctly.

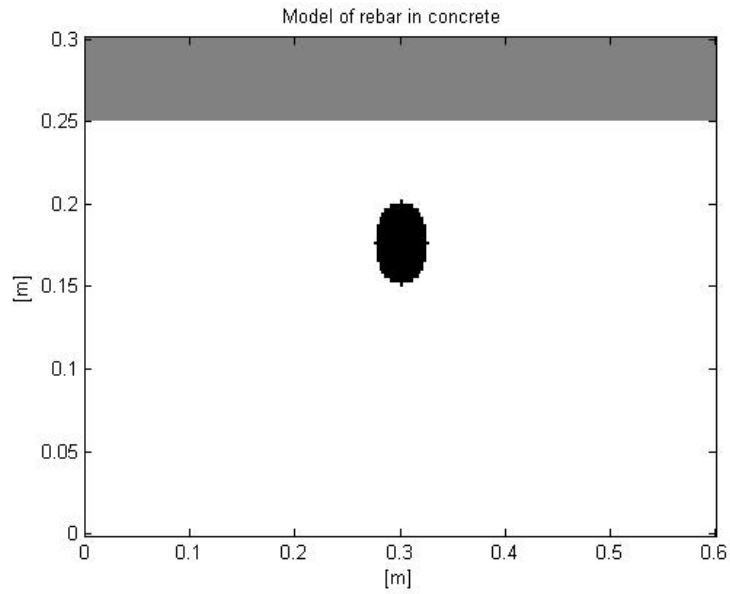


Figure 6-4 Geometry of the physical model generated in MATLAB

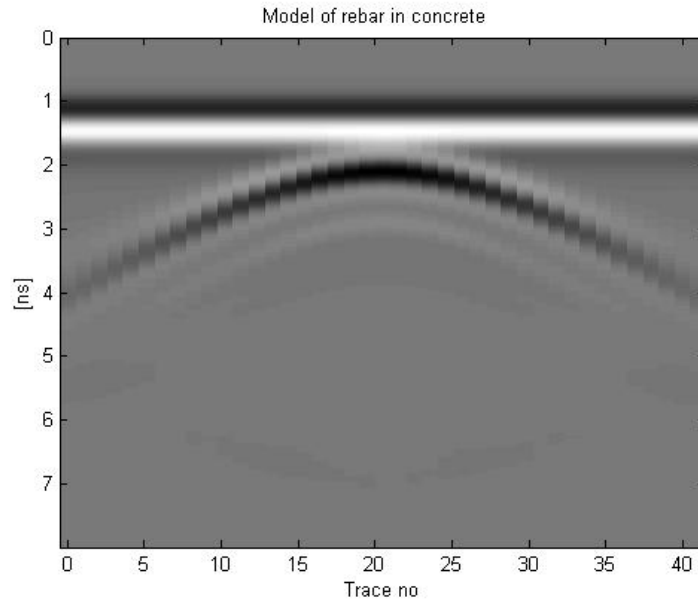


Figure 6-5 B-Scan of the model generated in MATLAB

The A-Scan output from the simulation was plotted in excel spreadsheet. The X axis of the plot indicated the time axis and the Y axis of the plot indicated the amplitude in V/m unit as shown in Fig. 6.6. The location of the antenna for the scan was varied over the concrete surface until an A-Scan similar to real data was achieved. The distance between the transmitter and the receiver was 40mm (1.57 in.) according to GSSI specification of 2600 MHz antenna. In Fig. 6.6, the first big reflected wave was from the surface of the concrete as shown. After entering into the concrete medium, the electromagnetic radar wave travelled to the cylindrical rebar. The second peak was from the rebar as shown in the Fig. 6.6. This peak from the rebar was between 2 ns to 3 ns which indicated the two way travel time of the radar wave for the cylindrical target. This simulated GPR trace qualitatively was in good agreement with a typical trace recorded by

the real GPR antenna through SIR-30. So, it was proved that the simulated model was acting coherently with respect to real GPR data.

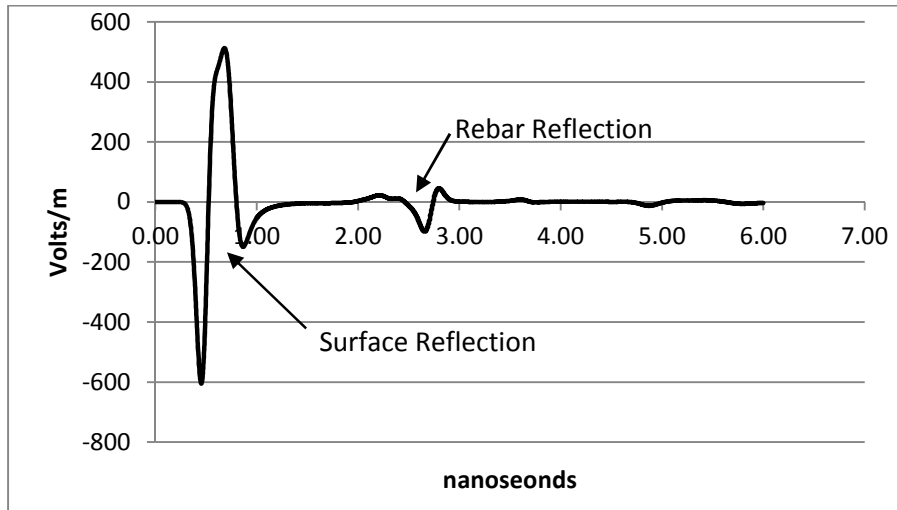


Figure 6-6 The A-Scan trace from the GPR Simulation of a rebar in concrete

#### 6.7 Effect of size of the rebar and dielectric permittivity on simulated GPR Response

From the previous section, it was shown that the behavior of a GPR trace from the simulated model using GPRMAX was coherent with real GPR trace. In this section the effect of the size of the rebar on the simulated GPR response were studied.

Six input file were drafted for simulation in GPRMAX. The geometry of the test model was a simple rectangular beam with a single cylindrical rebar embedded in it. Each of the models was having a same dielectric constant of 7 and same concrete cover of 50 mm. This dielectric constant and the cover depth were similar to that of the beam specimens of chapter 2. The diameters of the rebar in each of the input files were 10 mm (#3), 12 mm (#4), 16 mm (#5), 19 mm (#6), 25 mm (#8) and 35 mm (#11). The location of the antenna was similar to as presented in section 5.5 and the center frequency of the antenna was 2600 MHz. After finishing the input files, each of the files was run by



GPRMAX and the output traces were recorded. The output ASCII files were then converted to excel files and each of the A-Scan traces was normalized and plotted in a single graph. The two way travel time was on X axis and the normalized amplitude was on the Y axis in the plot. The resulting plot is shown in Fig. 6.7. It was observed that the amplitude of the surface reflections or direct waves were same for all six traces. But the differences in reflections from the rebars were prominent. The part from Fig. 6.7 that shows the reflection from the rebar is highlighted by a circle. The circled part of Fig. 6.7 is blown up and shown in Fig. 6.8. From Fig. 6.8 it was obvious that the higher was the diameter of the rebar, the higher was the normalized reflection amplitude. The 35 mm (#11) rebar was showing larger reflection amplitude than the 25 mm (#8) rebar. Similarly the 25 mm (#8) rebar was showing larger reflection amplitude than the 19 mm (#6) rebar and so forth. These responses from the simulated model were in good agreement with real GPR traces as discussed in chapter 3 and chapter 4.

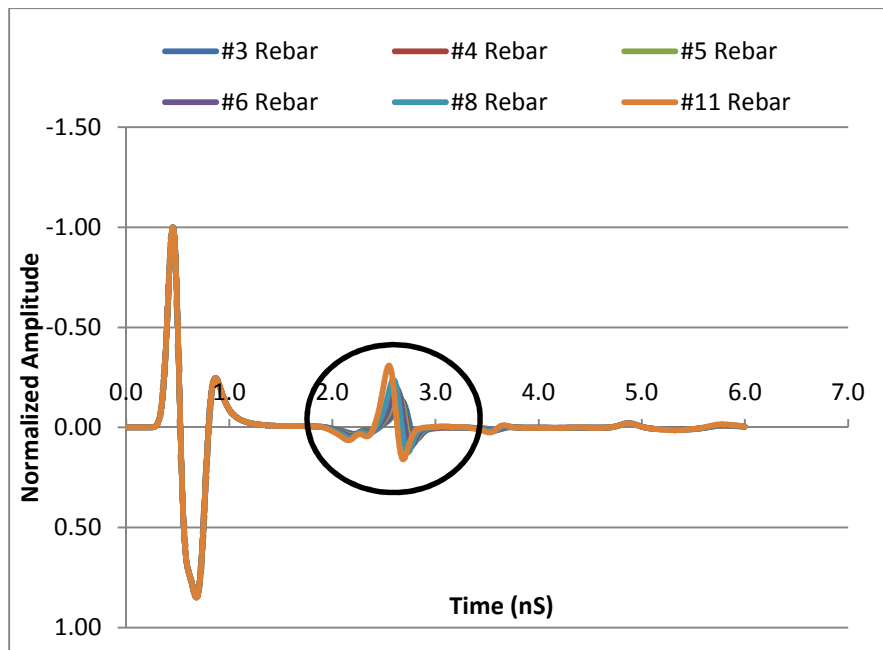


Figure 6-7 Simulated GPR traces from six different rebars by GPRMAX

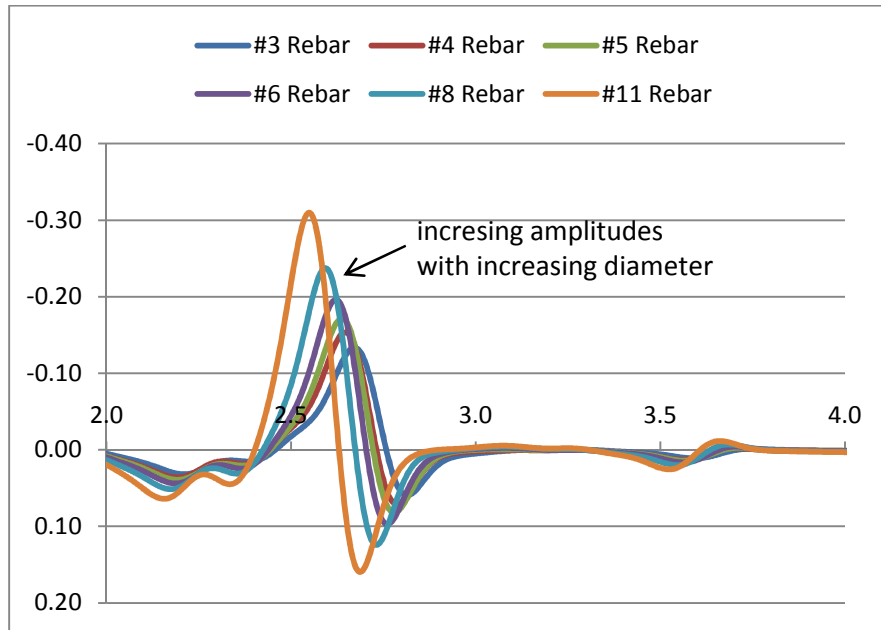


Figure 6-8 Normalized amplitude traces from rebars of different sizes from numerical model

#### 6.8 Validation of the numerical model compared to real GPR data

The normalized amplitudes of from each of the six different rebars in numerical model were recorded. Now, the GPR scans of the beam specimens that were shown in chapter 3 were opened. There were six different beam specimens. The diameters of the rebars in the beams specimens were identical with the rebar diameters as shown in section 5.7. The GPR scans of the beam specimens at 50 mm (2 in.) concrete cover were selected and opened in RADAN. Background removal filter were applied to each of the GPR scans of the beam specimen. Then the maximum positive normalized amplitudes from the rebars were recorded. The maximum normalized reflective amplitudes form the simulated model and form the beams specimen are shown in Table 6.1. For a particular diameter of the rebar, the maximum normalized amplitude from the numerical and the experimental were very close.

Table 6-1 Max normalized amplitudes from simulated and experimental model

Rebar Dia	Dia (in.)	Simulated Max Amplitude	Experimental Max Amplitude
#3	0.375	0.1335	0.149108
#4	0.5	0.153325	0.161808
#5	0.625	0.1714	0.214042
#6	0.75	0.19607	0.242103
#8	1	0.237412	0.277971
#11	1.375	0.309715	0.298882

A statistical hypothesis testing was performed. The null hypothesis was there is no significant differences between the maximum normalized amplitudes from the theoretical and the experimental data with a confidence interval of 95%. The null hypothesis  $H_0$  and the alternative hypothesis  $H_A$  can be expressed by Eq. 6.7 and 6.8:

$$H_0: \mu_1 = \mu_2 \quad (6.7)$$

$$H_A: \mu_1 \neq \mu_2 \quad (6.8)$$

A pooled t-test (Montgomery et al, 2010) were performed to test the hypothesis.

The test statistics t can be expressed by the following Eq. (6.9):

$$t = \frac{\bar{X}_1 - \bar{X}_2}{s_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} \quad (6.9)$$

Where,

$\bar{X}_1$  = average of the simulated data,

$\bar{X}_2$  = average of the experimental data,

$n_1$  = number of samples for simulated data,

$n_2$  = number of samples for experimental data.

The pooled variance  $s_p^2$  is expressed by the following Eq. 6.11:

$$s_p^2 = \frac{(n_1-1)s_1^2 + (n_2-1)s_2^2}{n_1+n_2-2} \quad (6.11)$$

Where,

$s_1^2$  = variance of the simulated data,

$s_2^2$  = variance of the experimental data.

The test statistics  $t$  was calculated as -0.54 from Eq. 6.9. The rejection criteria was determined from the  $t$ -table (Montgomery et al, 2010) for the degree of freedom and expected level of significance. The rejection criteria for the null hypothesis was  $t > 2.228$  and  $t < -2.228$ .

The test statistics  $t$ , was not falling in the rejection region. So we failed to reject the null hypothesis.

Therefore we accept the null hypothesis.

Based on the pooled  $t$ -test, it was concluded that there was no significant difference between the numerical and the experimental data with a confidence interval of 95%.

## 6.8 Effect of dielectric permittivity on simulated GPR Response

To test the effect of dielectric constant on simulated GPR model, three input files were prepared. The geometry of the file consisted of rectangular concrete space with 16 mm (#5) rebar embedded in it. The antenna was having a frequency of 2600 MHz. The only differences among the three input files were the dielectric constant. The three input files were having a dielectric constant of 7, 10 and 13 respectively. After running the input files in GPRMAX, the output traces were plotted. All three traces were plotted in a single

plot to understand the effect of dielectric constant. The resulting plot is shown in Fig. 6.9. It was obvious that the higher is the dielectric constant, the higher was the two way travel time and the reflection amplitude of the rebar had shifted to the right with the increase of dielectric constant. The magnitude of the maximum amplitude from the rebar for a dielectric constant of 7 was 69 V/m. The maximum amplitude for dielectric constant of 7 and 10 was 43 V/m and 30 V/m respectively. Though physically all three rebar were placed at a same location, their traces are appeared at different time space in the plot. This behavior of the simulated trace was perfectly consistent with real GPR traces. Because the higher the dielectric constant, the slower is the speed of electromagnetic wave. The slower velocity of the wave resulted in higher two way travel time. The reflected amplitude of the rebars were also decreasing with increasing dielectric constant. The surface reflection amplitude was also different for different dielectric constant. The smaller was the dielectric constant, the higher was the surface reflection amplitude.

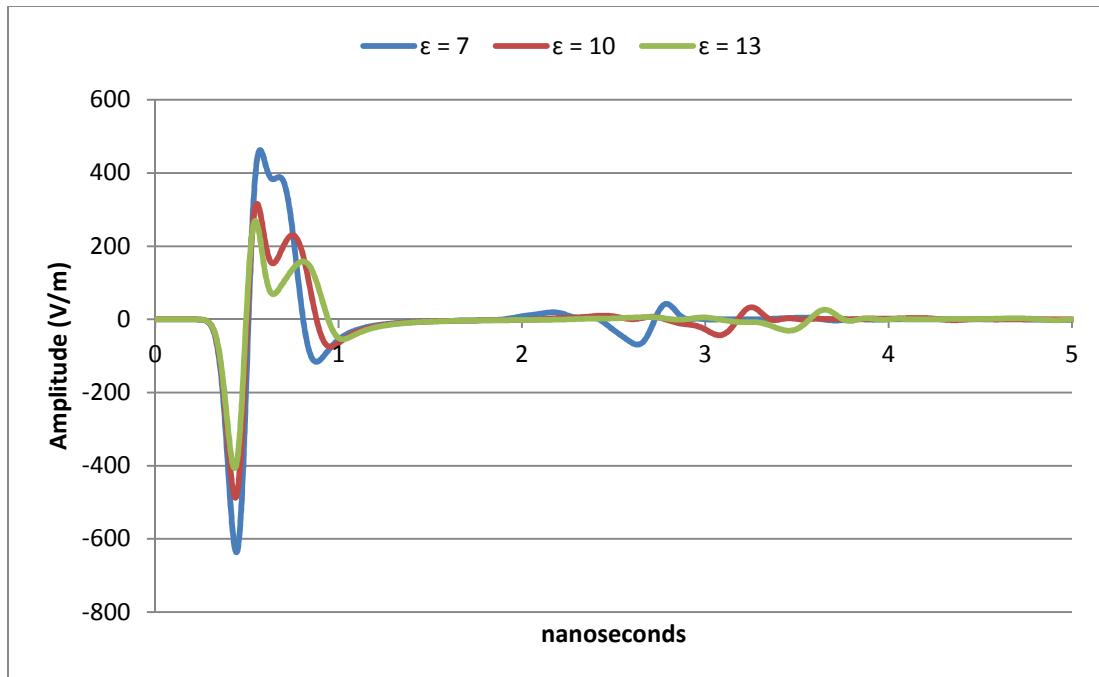


Figure 6-9 Simulated GPR traces of 16 mm (#5) rebar at different dielectric medium

In fig. 6.10, the amplitudes in Fig. 6.9 were normalized. The normalized surface reflection or direct wave amplitudes were different in Fig. 6.10 but there were no changes in the normalized maximum amplitudes from the rebars.

From the results that is displayed in Fig. 6.10, it was concluded that there was no effect of the dielectric constant of the medium in the value of normalized maximum amplitudes when the concrete cover depth and the bar diameters were constant.

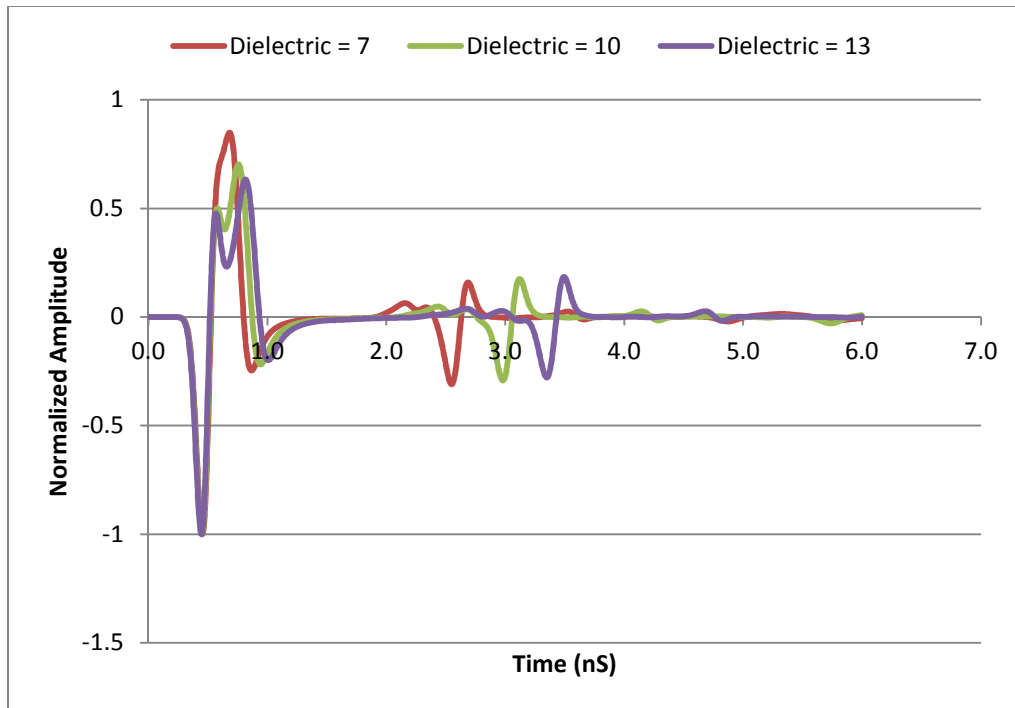


Figure 6-10 Simulated normalized GPR traces of 16 mm (#5) rebar at different dielectric medium

### 6.8 Effect of frequency and the size of the element

To study the effect of frequency on the maximum amplitudes from the model, four input files were generated for GPRMAX. The rebar diameter in the model was 16 mm (#5) and the dielectric constant was 7. The concrete cover was 50 mm (2 in.). Four different antenna frequencies were used for the four different numerical models. The selected frequencies of the antenna were 900 MHz, 1600 MHz, 2600 MHz and 3600 MHz. The normalized amplitudes vs travel time plots for the different frequencies are shown in Fig. 6.11.

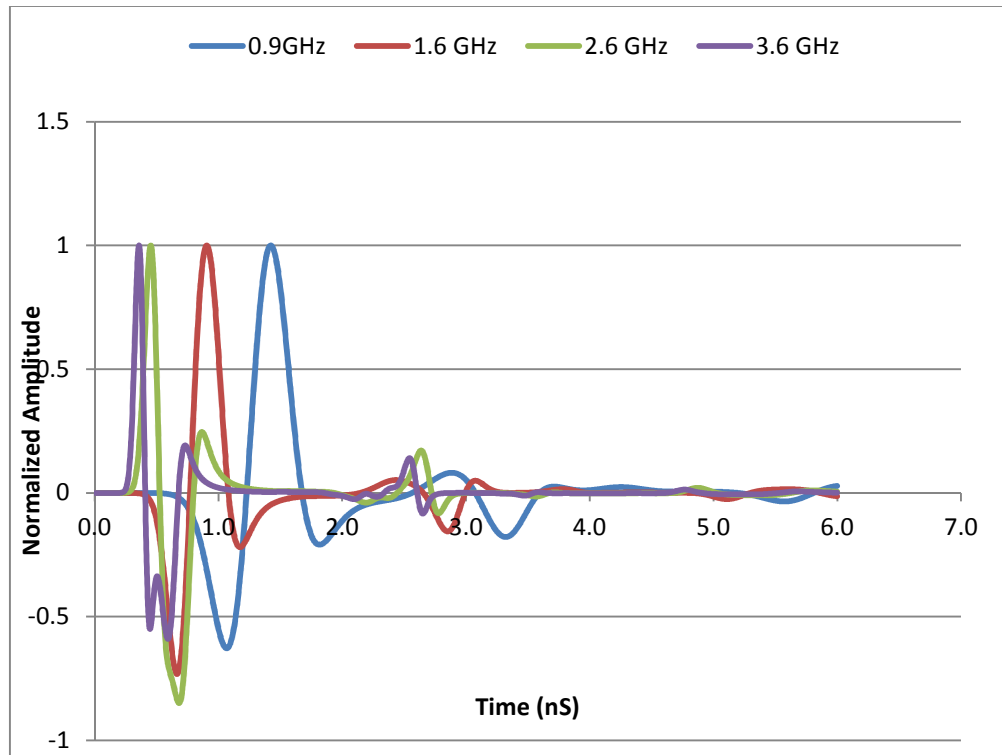


Figure 6-11 Amplitude vs travel time for different frequencies

Figure 6.11 shows that the peak amplitudes from the rebars were decreasing with increasing antenna frequencies. The wavelengths of the rebar reflection waves were higher for smaller frequencies and lower for higher frequencies. The values of peak amplitudes from the rebar with respect to antenna frequencies are presented in Fig. 6.12. For a 0.6 GHz antenna, the maximum amplitude from the rebar was 203.58 V/m. For 1.6 GHz antenna, the maximum amplitude was 148.21 V/m. This rate of change decreases with the increase of antenna frequency as shown in Fig. 6.12. The shape of the curve in Fig. 6.12 is parabolic.



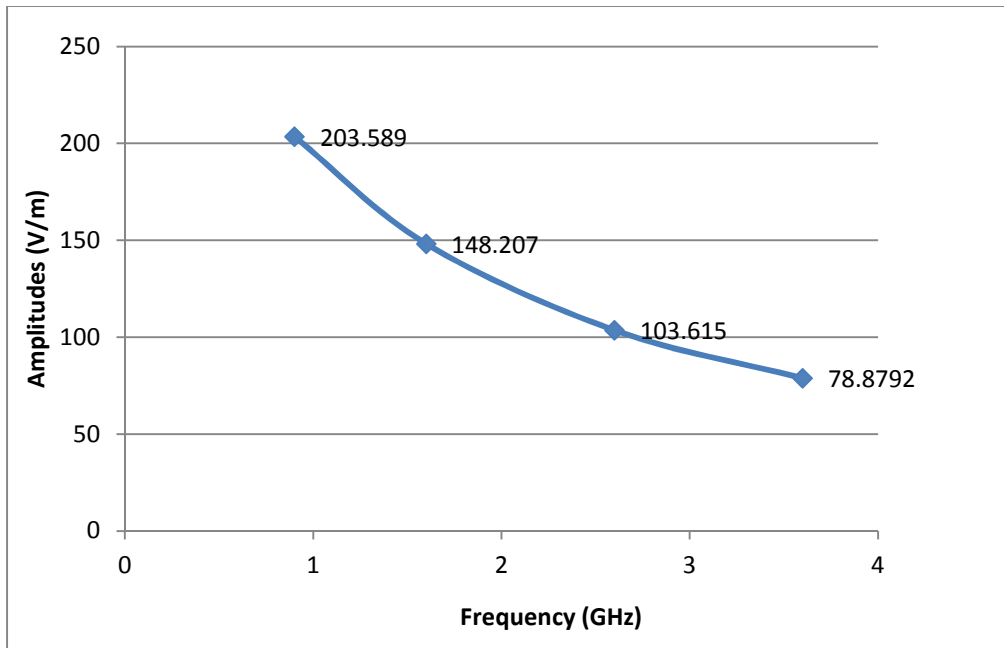


Figure 6-12 Maximum amplitude vs antenna frequency from the numerical model

The size of the mesh in the finite difference model was studied. Four different element sizes were chosen. They were 0.003 m (0.118 in.), 0.002 m (0.0787 in.), 0.001 m (0.03937 in.) and 0.0005 m (0.01968 in.). The total number of elements in the numerical model and the time step were also controlled by the minimum size of the element. For an element size of 0.003 m (0.118 in.), the total number of element in the numerical model was 848. For an element size of 0.0005 m (0.01968 in.), the total number of element in the numerical model was 5088. The time steps were also decreased with the increase in number of elements. For element size of 0.003 m (0.118 in.), the time step for the FDTD model was 7.0759 picoseconds. For element size of 0.0005 m (0.01968 in.), the time step for the FDTD model was 1.1793 picoseconds. The input files were prepared for the four different sizes of elements. The bar diameter in the input files were 16 mm (#5), the dielectric constant was 7 and the concrete cover was 50 mm ( 2 in.). The inputs files were run in GPR max and the maximum amplitudes form the

rebars were recorded. Figure 6.13 shows the GPR A-Scan outputs for the input files. Figure 6.14 shows the circled part of Fig. 6.13 that shows the reflection amplitudes from the rebars.

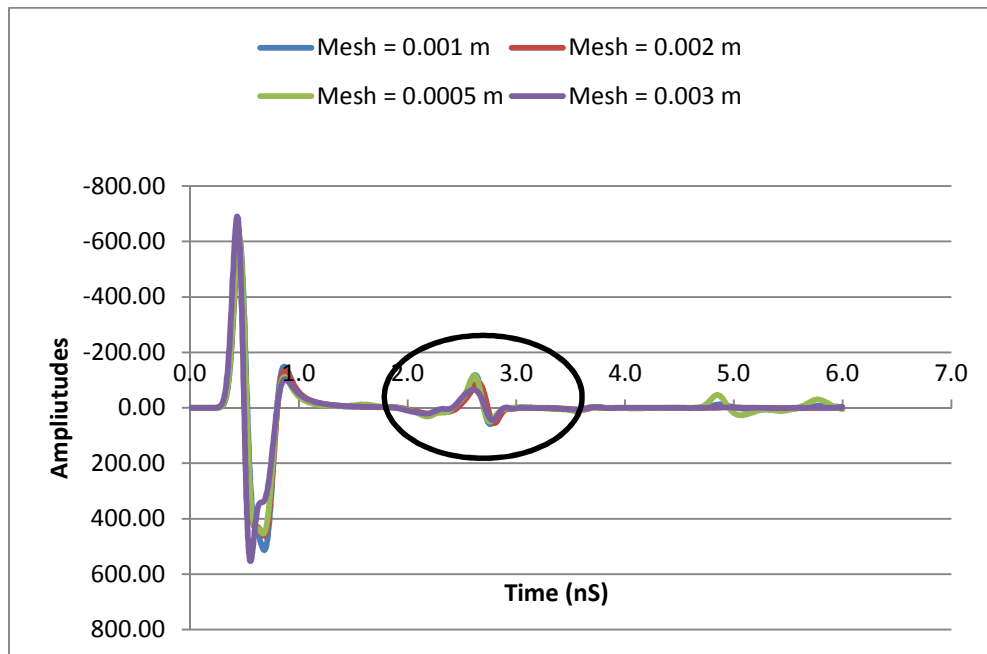


Figure 6-13 Amplitude vs time traces for different mesh sizes of the numerical model

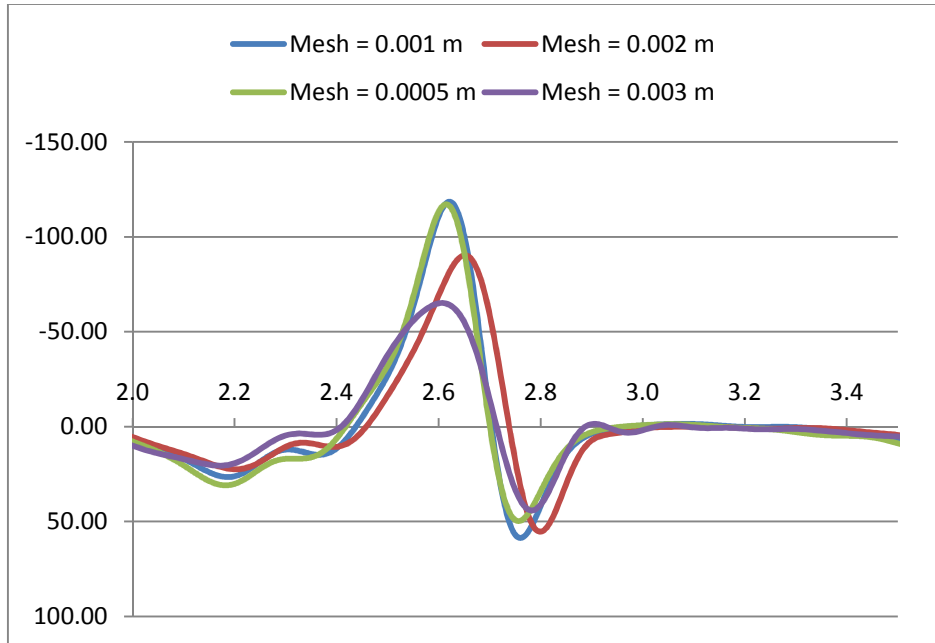


Figure 6-14 Reflection amplitudes from rebar for different sizes of elements in the numerical model

The maximum reflection amplitudes from the rebar for different element sizes are listed in Table 6.2. The maximum amplitudes were plotted against the size of the elements and shown in Fig. 6.15. It was observed that the maximum amplitudes from the rebars were increasing linearly with the decreasing size of the rebar. But after the element size was 0.001 m ( 0.03937 in.), the maximum amplitude was not increasing with decreasing size of the element. Therefore, it was concluded that the model converged once the size of the element is 0.001 m ( 0.03937 in.) or smaller.

Table 6-2 Maximum Amplitudes form rebars for different element sizes

Element Size (m)	Total Elements	Time Steps (picoseconds)	Max Amp V/m
0.003	848	7.0759	65.14
0.002	1272	4.7173	90.3
0.001	2544	2.3586	118.53
0.0005	5088	1.1793	118.81

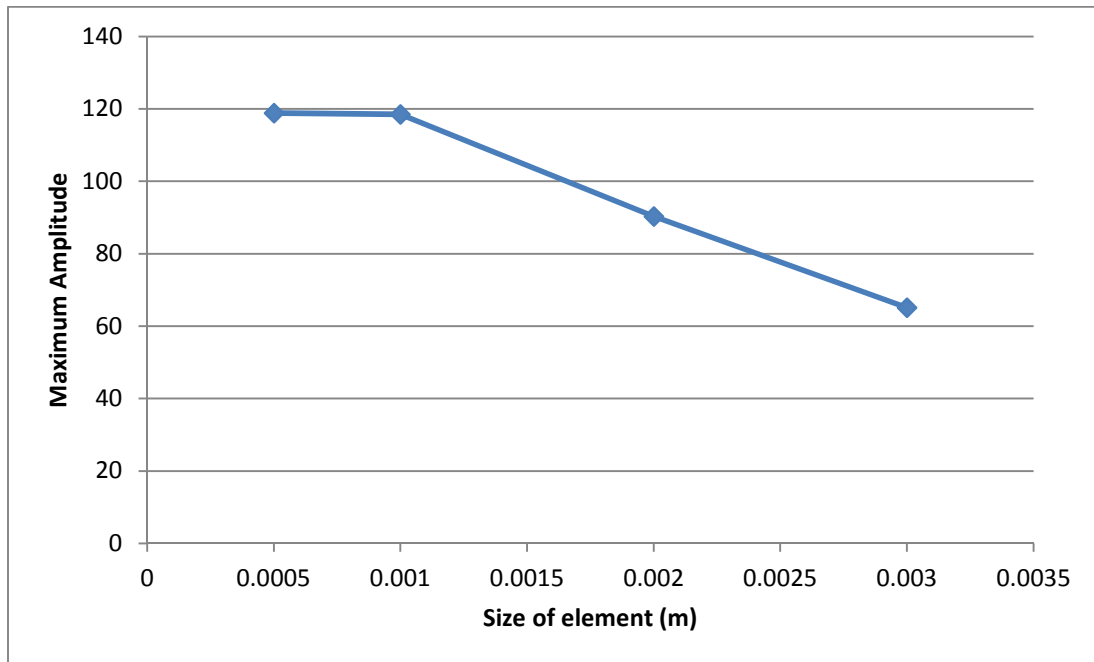


Figure 6-15 Maximum amplitudes vs size of the element in numerical model

### 6.9 Discussion

In this chapter a numerical model was developed using GPRMAX. The parameter of the numerical model was the antenna frequency, rebar diameter, concrete cover depth and dielectric constant of the concrete. Six different diameters of rebar ranging from 10 mm (#3) to 35 mm (#11) were used in the numerical simulations. The relationship between the maximum normalized amplitudes and the rebar diameter was established from the numerical model. The numerical model was calibrated with the experimental results. Statistical hypothesis testing was performed on the numerical and experimental values of maximum rebar amplitudes. It was shown that there was no significant difference between the numerical and experimental amplitudes with a confidence level of 95%. The calibrated model was then used to find the effect of dielectric constant and antenna frequency. It was shown that the normalized amplitudes

from the rebar did not change with the change of dielectric constants from 7 to 13 at a particular cover depth of 50 mm (2in.). The maximum amplitudes from the rebar were decreasing when the frequency of the antenna was increased from 0.9GHz to 3.6 GHz. An element size analysis was also done to ensure the convergence of the numerical model. It was found that the model converged when the element size of 0.001 m (0.03937 in.) was used in the numerical model.

## Chapter 7

### Conclusions and Recommendations

#### 7.1 Introduction

In this chapter, the summary of the findings of the research is presented and the recommendation of the future study is made. In this study GPR was used as non-destructive testing equipment to estimate the diameter of the rebar and to estimate the quantitative loss of rebar area at different stages of corrosion. The diameters of the rebar in concrete from GPR scan was estimated using two different approaches. The effects of parameters such as rebar size, dielectric constant of concrete and concrete cover depth were investigated in estimating the rebar diameter. Accelerated electrochemical corrosion of steel rebars was performed in the laboratory at different level of corrosion. The loss of mass from the rebars at different corrosion levels was estimated. The relation between the GPR responses and quantitative amount of corrosion was established. The effect of concrete dielectric constant and cover depth on the estimation of corrosion was also studied. A FDTD numerical model of rebar in concrete was developed. The numerical model was used to verify the experimental GPR data.

#### 7.2 Conclusions

In this study, two methods were used to estimate the rebar diameter using GPR. First, three GPR parameters were investigated and their effect on the size of the rebar was studied. The three parameters were:

- a) Maximum positive reflection amplitude of GPR wave form normal antenna orientation,
- b) Maximum positive reflection amplitude of GPR wave form 90° polarized antenna orientation,

c) Ratio of amplitude mentioned in (a) and (b) above.

The results presented in this chapter showed that the normal antenna orientation displayed a steady relation between the maximum amplitude and the size of the rebar at 1 in. (25 mm) and 2 in. (25 mm) depth. The polarized orientation of the antenna showed inconsistent response at 1 in. (25 mm) and 2 in. (25 mm) depth. The parameter of ratio between maximum amplitude in two perpendicular antenna orientations was not suitable for the ranges of diameter that was used. It was showing consistent behavior at deeper concrete cover.

The diameter of the rebar was estimated using two different methods. First, the rebar diameters were measured by establishing a relationship between the maximum positive amplitude from the rebar and the rebar diameter. Both the numerical and experimental data were very close and showed good correlations. Second, the rebar diameters were measured using an empirical approach using digital image processing. It was observed that this method is sensitive to the antenna frequency and the antenna used in this study was good for the diameter of #4 (12 mm) and #5 (16mm). For rebar diameter greater than #5 (16mm), a lower frequency antenna was recommended. For rebar diameter less than #4 (12 mm), a higher frequency antenna was recommended.

In next phase of this study, the change in cross sectional area in a rebar due to corrosion is investigated using GPR. Based on the results shown in this chapter, the maximum positive amplitude of the reflected wave from rebar was taken as the principal GPR parameter that was sensitive to size of the rebar.

A novel method to simulate long term corrosion in laboratory was discussed. Oil emulsion tank was used as a substitute of concrete specimen. The performance of oil emulsion tanks as a substitute of concrete beam specimen was verified from the GPR scans. The performance of the oil tank under different diameter of the rebar and at

different concrete depth was similar to real concrete beam. The dielectric property of the tank was varied by controlling the amount of water in the emulsion. Three oil water emulsion tanks were prepared with dielectric constants of 2.73, 5.47 and 9.3. These tanks were used to observe the effect of dielectric constant on GPR response.

Accelerated corrosion of the rebar was performed in a 5% NaCl solution using electrochemical method. The rebars were corroded at different corrosion level ranging from 0% to 45%. The corroded rebars were placed in the oil emulsion tanks and GPR scan was performed.

It was observed that the maximum amplitudes from the rebar decreased with the increase of the amount of corrosion. Linear regression models were developed to correlate between the maximum amplitudes and the percentage loss of area or corrosion. The linear regression models were developed for three different dielectric constants (2.73, 5.47 and 9.3) and three different concrete cover depths [1 in. (25 mm), 2 in. (50 mm) and 3 in. (75 mm)].

For dielectric constant of 2.73 and at concrete cover depth of 1 in. (25 mm), 10% loss of area resulted in 8.82% decrease in maximum amplitude. The decrease in amplitude for 10% loss of area at 2 in. (50 mm) and 3 in. (75 mm) cover depths are 8.57% and 7.69% respectively. For dielectric constant of 5.47 and for 10% loss of area at 1 in. (25 mm), the maximum amplitude decreased by 10.64%. The change in amplitude for 10% loss of area at 2 in. (50 mm) and 3 in. (75 mm) are 9.63% and 9.16%. For dielectric constant of 9.3, the change of maximum amplitudes for 10% loss of area at 1 in. (25 mm), 2 in. (50 mm) and 3 in. (75 mm) cover depths are 8.26%, 7.52% and 12.99% respectively.

Based on the regression model developed in this study, a method was proposed to determine the amount of corrosion in the field. By using the cover depth,



dielectric constant and the maximum GPR amplitude as input, the quantitative amount of corrosion can be calculated using the regression equations.

The behavior of the simulated corrosion experiment was studied by performing another accelerated corrosion experiment using a real concrete beam. GPR maximum amplitudes were collected for 25 days. It was observed that the maximum amplitude decreased with time. Fifty two percent increase in dielectric constant decreased the maximum amplitude by 20%.

A numerical model was developed using GPRMAX. The parameter of the numerical model was the antenna frequency, rebar diameter, concrete cover depth and dielectric constant of the concrete. Six different diameters of rebar ranging from 10 mm (#3) to 35 mm (#11) were used in the numerical simulations. The relationship between the maximum normalized amplitudes and the rebar diameter was established from the numerical model. The numerical model was calibrated with the experimental results. Statistical hypothesis testing was performed on the numerical and experimental values of maximum rebar amplitudes. It was shown that there was no significant difference between the numerical and experimental amplitudes with a confidence level of 95%. The calibrated model was then used to find the effect of dielectric constant and antenna frequency. It was shown that the normalized amplitudes from the rebar did not change with the change of dielectric constants from 7 to 13 at a particular cover depth of 50 mm (2in.). The maximum amplitudes from the rebar were decreasing when the frequency of the antenna was increased from 0.9GHz to 3.6 GHz. An element size analysis was also done to ensure the convergence of the numerical model. It was found that the model converged when the element size of 0.001 m (0.03937 in.) was used in the numerical model.

### 7.3 Future Research

In this study, the diameter of the rebar in concrete and the quantitative amount of corrosion in terms of loss of mass was estimated. The following recommendations are proposed for future research:

- The frequency of the antenna in this study was 2.6 GHz manufactured by GSSI. The emission properties of the antenna are manufacturer specific. It is suggested to use antennas from other providers and establish a method that is independent of the antenna design or manufacturer.
- The behavior of the GPR response depends greatly on the frequency of the antenna. For diameter estimation, it is suggested to use antennas with a practical range of frequencies. For corrosion damage estimation it is suggested to use an antenna with a frequency higher than 2.6 GHz.
- The relationship between the GPR responses and the amount of corrosion that is presented in this study was performed in the laboratory. It is suggested to apply the proposed method in a real structure preferably an old bridge deck right before demolition. The physical amount of corrosion can be determined after the demolition. This actual amount of corrosion can be used to determine the accuracy of the proposed method in this study.
- The numerical model that is developed in this study is based on some assumptions such as homogenous property of concrete. It is suggested to develop a heterogeneous numerical model for concrete with separate dielectric properties for aggregates and cement paste matrix. The numerical simulation of corroded rebar and the surrounding cracked and

damaged concrete will also be an excellent addition to understand the GPR responses from corroded concrete.

Appendix A  
GPRMAX2D Output Signal

```

"#GprMax2D, Ver"      2
#title:  None
#iterations: 2544
#dx: 0.001 met re
#dy: 0.001 met re
#dt: 2.35865e-12 secs
#Number of Steps: 1
#Number of tx: 1
#Number of rx: 1
#Number of rx_box: 0
#tx: Number 1
#tx: Initial position 155 252 (cell coords)
#tx: ID MyLine Source
#tx: Delay 0 secs
#tx: Removed at 6e-09 secs
#rx: 195 252 ( cell coords)
"#tx_steps: 0," 0 (cell coords)
"#rx_steps: 0," 0 (cell coords)

```

TIME(NS)	EZ(V/m)	HX(A/m)	HY(A/m)
0.00E+00	0.00E+00	0.00E+00	0.00E+00
9.91E-02	-1.78E-15	-2.42E-16	9.61E-15
1.01E-01	-2.69E-12	4.73E-15	7.12E-15
2.00E-01	-1.45E-02	3.51E-05	5.57E-05
3.00E-01	-9.29E+00	2.76E-02	3.47E-02
3.02E-01	-1.05E+01	3.13E-02	3.91E-02
4.01E-01	-3.51E+02	1.38E+00	1.39E+00
5.00E-01	-3.07E+02	1.67E+00	2.52E+00
6.01E-01	4.31E+02	-4.15E+00	-8.34E-01
7.01E-01	4.98E+02	-1.19E+00	-3.44E+00
8.02E-01	-1.14E+01	1.91E+00	-5.20E-01
9.08E-01	-1.24E+02	3.71E-01	4.73E-01
1.00E+00	-5.38E+01	3.22E-02	1.95E-01
1.20E+00	-1.35E+01	-1.76E-02	4.27E-02
1.20E+00	-1.33E+01	-1.76E-02	4.21E-02
1.21E+00	-1.32E+01	-1.76E-02	4.15E-02
1.30E+00	-8.18E+00	-1.61E-02	2.46E-02
1.30E+00	-8.09E+00	-1.60E-02	2.43E-02
1.31E+00	-8.01E+00	-1.60E-02	2.40E-02
1.40E+00	-5.46E+00	-1.28E-02	1.54E-02
1.41E+00	-5.41E+00	-1.27E-02	1.52E-02
1.41E+00	-5.37E+00	-1.26E-02	1.51E-02
1.50E+00	-4.34E+00	-7.65E-03	1.13E-02
1.51E+00	-4.33E+00	-7.47E-03	1.12E-02
1.51E+00	-4.33E+00	-7.28E-03	1.12E-02
1.61E+00	-4.56E+00	2.14E-03	1.12E-02
1.61E+00	-4.56E+00	2.35E-03	1.12E-02
1.61E+00	-4.56E+00	2.56E-03	1.12E-02
1.71E+00	-4.07E+00	6.59E-03	9.80E-03
1.71E+00	-4.05E+00	6.59E-03	9.74E-03
1.71E+00	-4.02E+00	6.59E-03	9.69E-03
1.81E+00	-3.17E+00	5.26E-03	7.59E-03

1.81E+00	-3.15E+00	5.22E-03	7.55E-03
1.81E+00	-3.13E+00	5.18E-03	7.51E-03
1.91E+00	-1.93E+00	1.82E-03	8.18E-03
1.91E+00	-1.87E+00	1.60E-03	8.33E-03
1.92E+00	-1.81E+00	1.37E-03	8.48E-03
2.01E+00	4.15E+00	-2.51E-02	2.79E-02
2.01E+00	4.35E+00	-2.61E-02	2.87E-02
2.02E+00	4.55E+00	-2.71E-02	2.95E-02
2.11E+00	1.33E+01	-5.58E-02	7.63E-02
2.12E+00	1.36E+01	-5.59E-02	7.80E-02
2.12E+00	1.38E+01	-5.59E-02	7.97E-02
2.21E+00	2.27E+01	6.51E-03	1.45E-01
2.22E+00	2.26E+01	9.41E-03	1.45E-01
2.22E+00	2.26E+01	1.23E-02	1.45E-01
2.32E+00	1.11E+01	4.27E-02	7.45E-02
2.32E+00	1.09E+01	4.06E-02	7.32E-02
2.32E+00	1.08E+01	3.85E-02	7.20E-02
2.42E+00	1.01E+01	-6.07E-03	8.08E-02
2.42E+00	9.73E+00	-3.93E-03	8.07E-02
2.42E+00	9.36E+00	-1.58E-03	8.05E-02
2.52E+00	-1.86E+01	2.40E-01	3.72E-03
2.52E+00	-1.95E+01	2.47E-01	-2.20E-04
2.52E+00	-2.03E+01	2.55E-01	-4.34E-03
2.62E+00	-8.20E+01	2.80E-01	-4.07E-01
2.62E+00	-8.38E+01	2.68E-01	-4.20E-01
2.63E+00	-8.55E+01	2.55E-01	-4.33E-01
2.72E+00	-3.23E+01	-4.59E-01	-2.41E-01
2.72E+00	-2.83E+01	-4.64E-01	-2.18E-01
2.73E+00	-2.43E+01	-4.67E-01	-1.95E-01
2.82E+00	3.98E+01	-3.26E-02	2.31E-01
2.83E+00	3.88E+01	-2.42E-02	2.26E-01
2.83E+00	3.77E+01	-1.64E-02	2.20E-01
2.92E+00	4.89E+00	2.82E-02	3.00E-02
2.93E+00	4.62E+00	2.71E-02	2.83E-02
2.93E+00	4.37E+00	2.61E-02	2.68E-02
3.03E+00	1.01E+00	3.65E-03	5.38E-03
3.03E+00	9.89E-01	3.47E-03	5.24E-03
3.03E+00	9.69E-01	3.30E-03	5.11E-03
3.13E+00	3.57E-02	-1.89E-03	-1.44E-03
3.13E+00	1.88E-02	-2.07E-03	-1.57E-03
3.13E+00	2.89E-03	-2.25E-03	-1.69E-03
3.23E+00	1.12E-01	-5.23E-03	-1.02E-03
3.23E+00	1.15E-01	-5.11E-03	-9.79E-04
3.23E+00	1.17E-01	-4.99E-03	-9.39E-04
3.33E+00	8.28E-02	-2.55E-03	-2.64E-03
3.33E+00	1.05E-01	-2.69E-03	-2.65E-03
3.34E+00	1.30E-01	-2.85E-03	-2.67E-03
3.43E+00	2.04E+00	-1.89E-02	8.82E-05
3.43E+00	2.09E+00	-1.94E-02	2.03E-04
3.44E+00	2.14E+00	-1.99E-02	3.23E-04
3.53E+00	5.40E+00	-3.07E-02	1.63E-02
3.54E+00	5.54E+00	-3.05E-02	1.71E-02

3.54E+00	5.67E+00	-3.02E-02	1.79E-02
3.63E+00	6.98E+00	1.45E-02	2.95E-02
3.64E+00	6.81E+00	1.58E-02	2.86E-02
3.64E+00	6.62E+00	1.70E-02	2.76E-02
3.74E+00	-1.18E+00	1.30E-02	-2.07E-02
3.74E+00	-1.22E+00	1.22E-02	-2.11E-02
3.74E+00	-1.25E+00	1.13E-02	-2.14E-02
3.84E+00	1.86E-01	-1.42E-03	-1.33E-02
3.84E+00	2.07E-01	-1.38E-03	-1.32E-02
3.84E+00	2.27E-01	-1.35E-03	-1.30E-02
3.94E+00	4.18E-01	-1.43E-03	-9.92E-03
3.94E+00	4.23E-01	-1.47E-03	-9.84E-03
3.94E+00	4.29E-01	-1.50E-03	-9.76E-03
4.04E+00	8.14E-01	-1.63E-03	-5.45E-03
4.04E+00	8.22E-01	-1.60E-03	-5.35E-03
4.05E+00	8.30E-01	-1.57E-03	-5.26E-03
4.14E+00	1.01E+00	-7.01E-04	-2.54E-03
4.14E+00	1.01E+00	-6.97E-04	-2.48E-03
4.15E+00	1.01E+00	-6.94E-04	-2.43E-03
4.24E+00	1.11E+00	-3.18E-04	-4.31E-04
4.25E+00	1.11E+00	-2.90E-04	-3.94E-04
4.25E+00	1.11E+00	-2.60E-04	-3.58E-04
4.34E+00	9.39E-01	1.73E-03	2.84E-04
4.35E+00	9.33E-01	1.78E-03	2.80E-04
4.35E+00	9.27E-01	1.83E-03	2.75E-04
4.45E+00	5.31E-01	2.91E-03	-1.28E-03
4.45E+00	5.17E-01	2.89E-03	-1.35E-03
4.45E+00	5.03E-01	2.87E-03	-1.42E-03
4.55E+00	3.05E-01	-6.67E-04	-2.43E-03
4.55E+00	3.15E-01	-7.57E-04	-2.36E-03
4.55E+00	3.27E-01	-8.42E-04	-2.28E-03
4.65E+00	4.67E-01	-8.14E-04	1.20E-03
4.65E+00	4.41E-01	-8.13E-04	1.22E-03
4.65E+00	4.14E-01	-8.20E-04	1.24E-03
4.75E+00	-3.51E+00	-1.06E-02	2.08E-03
4.75E+00	-3.69E+00	-1.12E-02	2.15E-03
4.76E+00	-3.88E+00	-1.17E-02	2.23E-03
4.85E+00	-1.22E+01	-3.46E-02	5.50E-03
4.85E+00	-1.22E+01	-3.49E-02	5.52E-03
4.86E+00	-1.23E+01	-3.51E-02	5.54E-03
4.95E+00	-7.05E+00	-2.20E-02	2.31E-03
4.96E+00	-6.81E+00	-2.14E-02	2.18E-03
4.96E+00	-6.56E+00	-2.07E-02	2.06E-03
5.05E+00	1.48E+00	-7.88E-04	-1.98E-03
5.06E+00	1.61E+00	-4.56E-04	-2.04E-03
5.06E+00	1.74E+00	-1.29E-04	-2.10E-03
5.16E+00	4.78E+00	9.00E-03	-2.96E-03
5.16E+00	4.81E+00	9.14E-03	-2.94E-03
5.16E+00	4.84E+00	9.28E-03	-2.92E-03
5.26E+00	5.23E+00	1.20E-02	-3.39E-04
5.26E+00	5.24E+00	1.20E-02	-2.26E-04
5.26E+00	5.24E+00	1.20E-02	-1.09E-04

5.36E+00	5.53E+00	1.10E-02	6.98E-03
5.36E+00	5.55E+00	1.10E-02	7.20E-03
5.36E+00	5.56E+00	1.11E-02	7.42E-03
5.46E+00	5.56E+00	1.72E-02	1.46E-02
5.46E+00	5.53E+00	1.75E-02	1.47E-02
5.47E+00	5.50E+00	1.77E-02	1.47E-02
5.56E+00	2.91E+00	2.74E-02	1.03E-02
5.56E+00	2.82E+00	2.75E-02	1.01E-02
5.57E+00	2.72E+00	2.76E-02	9.99E-03
5.66E+00	-1.89E+00	2.87E-02	1.01E-02
5.67E+00	-2.01E+00	2.86E-02	1.03E-02
5.67E+00	-2.13E+00	2.85E-02	1.04E-02
5.76E+00	-5.91E+00	1.73E-02	1.31E-02
5.77E+00	-5.94E+00	1.69E-02	1.30E-02
5.77E+00	-5.98E+00	1.65E-02	1.28E-02
5.87E+00	-5.35E+00	4.33E-03	3.92E-03
5.87E+00	-5.31E+00	4.16E-03	3.68E-03
5.87E+00	-5.27E+00	3.99E-03	3.44E-03
5.97E+00	-3.42E+00	7.96E-04	-4.42E-03
5.97E+00	-3.38E+00	7.73E-04	-4.55E-03
5.97E+00	-3.33E+00	7.50E-04	-4.68E-03



Appendix B  
MATLAB CODES FOR GPRMAX2D

These Matlab codes were generated by Bostanudin, N. (2013)

```
filename = 'beam1.txt';
geo = '.geo';
sca = '.sca';
geofile = [filename geo];
scafile = [filename sca];
[mesh,header,media] = gprmax2g(geofile);
modeltitle = header.title;
dx = header.dx; % cell size in x direction - horizontal for GprMax
dy = header.dy; % cell size in y direction - vertical for GprMax
nx = header.nx;
ny = header.ny;
x = nx*dx;
y = ny*dy;
% Scan data
[Header,Fields]=gprmax(scafile);
modeltitle = Header.title;
    Nsteps = Header.NSteps;

figure(1);
imagesc(0:dx:x, 0:dy:y, mesh);
set(gca,'YDir','normal')
colormap(gray);
xlabel('[m]');
ylabel('[m]');
title(modeltitle);
% Scan
figure(2);
imagesc(0:Nsteps, (0:dt:timew)*10^9, ez); % *10^9 to get time in ns
colormap(gray);
xlabel('Trace no');
ylabel('[ns]');
title(modeltitle);
%% Display GPR scan image after mean removal
ezmr = mrem(ez);
figure(3);
imagesc(ezmr);
colormap(gray);
xlabel('[m]');
ylabel('[ns]');
%
```

## References

- Ahmad, S. (2003). Reinforcement corrosion in concrete structures, its monitoring and service life prediction—a review. *Cement and Concrete Composites*, 25(4), 459-471.
- ASTM C876-09. (2014). Standard test method for half-cell potentials of uncoated reinforcing steel in concrete. West Conshohocken: American Society for Testing and Materials.
- ASTM WK-37880. (2012). New Test Method for Measuring the Surface Resistivity of Hardened Concrete Using the Wenner Four-Electrode Method. West Conshohocken: American Society for Testing and Materials.
- Bertolini, L., Bolzoni, F., Pastore, T., & Pedferri, P. (1996). Behaviour of stainless steel in simulated concrete pore solution. *British Corrosion Journal*, 31(3), 218-222.
- Bostanudin, N. (2013). *Computational methods for processing ground penetrating radar data* (Doctoral dissertation, University of Portsmouth).
- Chang, C. W., Lin, C. H., & Lien, H. S. (2009). Measurement radius of reinforcing steel bar in concrete using digital image GPR. *Construction and Building Materials*, 23(2), 1057-1063.
- Duffó, G., Gaillard, N., Mariscotti, M., & Ruffolo, M. (2015). Application of gamma-ray radiography and gravimetric measurements after accelerated corrosion tests of steel embedded in mortar. *Cement and Concrete Research*, 74, 1-9.
- Garboczi, E. J., Stutzman, P. E., Wang, S., Martys, N. S., Hassan, A., Duthinh, D., & Stiles, M. D (2010). Corrosion Detection in Concrete Rebars Using a Spectroscopic Technique.
- Giannopoulos A. (2005) GprMax2D/3D: [/http://www.gprmax.orgS](http://www.gprmax.orgS).

- Giannopoulos, A. (1997) The investigation of transmission-line matrix and finite-difference time-domain methods for the forward problem of ground probing radar. Ph.D. thesis, University of York, UK.
- Giannopoulos, A. (2005). "Modelling ground penetrating radar by GprMax." *Construction and building materials* 19.10 (2005): 755-762.
- Hong, S., Lai, W. W. L., Wilsch, G., Helmerich, R., Helmerich, R., Günther, T., & Wiggerhauser, H. (2014). Periodic mapping of reinforcement corrosion in intrusive chloride contaminated concrete with GPR. *Construction and Building Materials*, 66, 671-684.
- Hubbard, S. S., Zhang, J., Monteiro, P. J., Peterson, J. E., & Rubin, Y. (2003). Experimental detection of reinforcing bar corrosion using nondestructive geophysical techniques. *ACI Materials Journal*, 100(6).
- Kim, S., Surek, J., & Baker-Jarvis, J. (2011). Electromagnetic metrology on concrete and corrosion. *Journal of Research of the National Institute of Standards and Technology*, 116(3), 655-669.
- Kunz, K.S., Luebbers RJ (1993). The finite-difference time-domain method for electromagnetics. Boca Raton: CRC Press.
- Lai, W. L., Kind, T., Stoppel, M., & Wiggerhauser, H. (2012). Measurement of accelerated steel corrosion in concrete using ground-penetrating radar and a modified half-cell potential method. *Journal of Infrastructure Systems*, 19(2), 205-220.
- Leucci, G. (2012). Ground Penetrating Radar: an Application to Estimate Volumetric Water Content and Reinforced Bar Diameter in Concrete Structures. *Journal of Advanced Concrete Technology*, 10(12), 411-422.
- Martino, N., Maser, K., Birken, R., & Wang, M. (2014). Determining Ground Penetrating Radar Amplitude Thresholds for the Corrosion State of Reinforced Concrete

- Bridge Decks. *Journal of Environmental and Engineering Geophysics*, 19(3), 175-181.
- Millard, S., & Sadowski, L. (2009). Novel method for linear polarisation resistance corrosion measurement. *e-Journal of Nondestructive Testing & Ultrasonics*, 14.
- Montgomery, D. C., & Runger, G. C. (2010). *Applied statistics and probability for engineers*. John Wiley & Sons.
- Parrillo, R., Roberts, R.L., and Haggan, A. (2005) "Bridge Deck Condition Assessment Using Ground Penetrating Radar", International Bridge Conference, Pittsburgh, PA, June 13-15
- RADAN 7 (2014 ) [Computer software]. Salem, NH, Geophysical Survey Systems (GSSI).
- Shihab, S., & Al-Nuaimy, W. (2005). Radius estimation for cylindrical objects detected by ground penetrating radar. *Subsurface Sensing Technologies and Applications*, 6(2), 151-166.
- Standard, A. S. T. M. (2003). G1-03. *Standard Practice for preparing, cleaning, and evaluating corrosion test specimens, Annual Book of ASTM Standards*, 3, 17-25.
- Standard, A. S. T. M. (2009). G59-97: Standard Test Method for Conducting Potentiodynamic Polarization Resistance Measurements. *West Conshohocken, PA: ASTM International*.
- Taflove, A. (1995). *Computational electrodynamics: the finite-difference timedomain method*. Artech House.
- The Helpful Engineer (2010), "Carbonation of concrete(corrosion)"  
[http://thehelpfulengineer.com /index.php/2010/10/carbonation-of-concrete-corrosion](http://thehelpfulengineer.com/index.php/2010/10/carbonation-of-concrete-corrosion) accessed Nov, 2014.

- Utsi, V., & Utsi, E. (2004, June). Measurement of reinforcement bar depths and diameters in concrete. In *Ground Penetrating Radar, 2004. GPR 2004. Proceedings of the Tenth International Conference on* (pp. 659-662). IEEE.
- Washer, G. A. (2013). Concrete reinforcement detection and assessment. *The NDT Technician*, 12(2), 1-5.
- Yee K. S., (1966), Numerical Solution of Initial Boundary Value Problems Involving Maxwell's equations in Isotropic Media., *IEEE Transactions on Antennas and Propagation*, Vol. 14, pp. 302-307
- Zanzi, L., & Arosio, D. (2013). Sensitivity and accuracy in rebar diameter measurements from dual-polarized GPR data. *Construction and Building Materials*, 48, 1293-1301.
- Zhan, B. J., Lai, W. L., Kou, S. C., Poon, C. S., & Tsang, W. F. (2011). Correlation between accelerated steel corrosion in concrete and ground penetrating radar parameters. In C. Leung, & K. WAN (Eds.), *International RILEM Conference on Advances in Construction Materials Through Science and Engineering* (pp. 563-571). RILEM Publications SARL.
- Zou, X., Schmitt, T., Perloff, D., Wu, N., Yu, T. Y., & Wang, X. (2015). Nondestructive corrosion detection using fiber optic photoacoustic ultrasound generator. *Measurement*, 62, 74-80.

### Biographical Information

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